

TESTING QUANTUM MECHANICS
TOWARDS THE LEVEL OF EVERYDAY LIFE:
RECENT PROGRESS AND
CURRENT PROSPECTS

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MESO/MACROSCOPIC TESTS OF QM: MOTIVATION

At microlevel: (a) $|\uparrow\rangle + |\downarrow\rangle$ quantum superposition ✓
 \neq (b) $|\uparrow\rangle$ OR $|\downarrow\rangle$ classical mixture ✗

how do we know? **Interference**

At macrolevel: (a)  +  quantum superposition }
 OR (b)  OR  macrorealism }

⚠: Decoherence **DOES NOT** reduce (a) to (b)!

Can we tell whether (a) or (b) is correct?

Yes, if and only if they give **different experimental predictions**. But if decoherence \rightarrow no interference, then predictions of (a) and (b) identical.

\Rightarrow must look for **QIMDS**
 ↑
 quantum interference of macroscopically distinct states

What is “macroscopically distinct”?

(a) “extensive difference” Λ

(b) “disconnectivity” D

↑
 \sim large number of particles behave differently in two branches

Initial aim of program: interpret raw data in terms of QM, test (a) vs (b).



WHY HAS (MUCH OF) THE QUANTUM MEASUREMENT LITERATURE SEVERELY **OVERESTIMATED** DECOHERENCE?

(“electron-on-Sirius” argument: $\Delta\epsilon \sim a^{-N} \sim \exp - N \leftarrow \sim 10^{23}$)

\Rightarrow Just about any perturbation $\gg \Delta\epsilon \Rightarrow$ decoherence)

1. Matrix elements of S-E interaction couple only a very restricted set of levels of S.
2. “Adiabatic” (“**false**”) decoherence:

Ex.: spin-boson model

$$\hat{H} = \hat{H}_s + \hat{H}_E + \hat{H}_{S-E}$$

$$\hat{H}_s = \Delta \sigma_x$$

$$\hat{H}_E = \text{set of SHO's with lower frequency cutoff } \omega_{\min} \gg \Delta$$

$$\hat{H}_{S-E} = \hat{\sigma}_z \sum_{\alpha} C_{\alpha} \hat{x}_{\alpha} \leftarrow \text{oscillator coords.}$$

$$\Psi_{\text{un}}(t=0) = |+\rangle |\chi_+\rangle \leftarrow \text{displaced state of oscillation}$$

$$\hat{\rho}_s(t=0) = \begin{pmatrix} 1 & 0 \\ 0 & 0 \end{pmatrix} \text{ (trivially)}$$

\Downarrow

$$\Psi_{\text{un}}(t \sim \hbar / \Delta_{\text{un}}) \cong \frac{1}{\sqrt{2}} (|+\rangle |\chi_+\rangle + |-\rangle |\chi_-\rangle),$$

$$\langle \chi_+ | \chi_- \rangle = \exp - F \cong 0 \quad \text{FC factor}$$

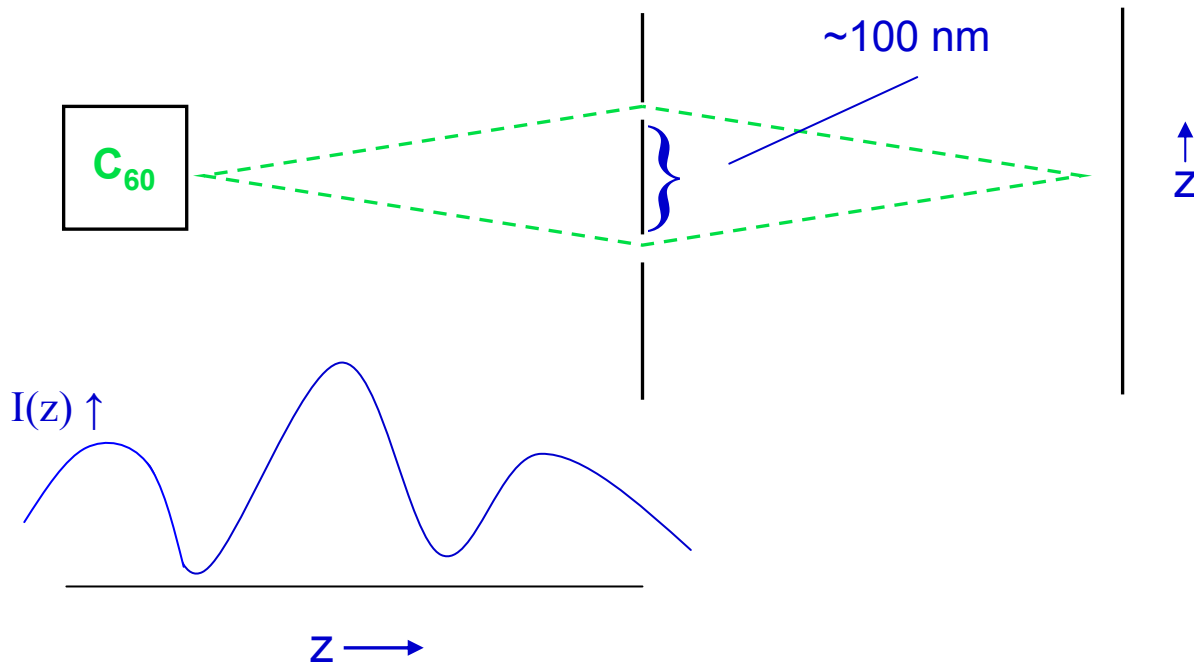
$$\Rightarrow \hat{\rho}_s(t \sim \hbar / \Delta_{\text{un}}) \cong \begin{pmatrix} \frac{1}{2} & 0 \\ 0 & \frac{1}{2} \end{pmatrix}$$

decohered?? (cf. neutron interferometer)



The Search for QIMDS

1. Molecular diffraction*



Note: (a.) Beam does not have to be monochromated

$$f(\nu) = A\nu^3 \exp\left[-(\nu - \nu_o)^2 / \nu_m^2\right] \quad (\nu_o \sim 1.8\nu_m)$$

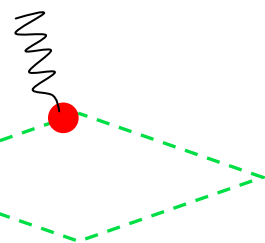
(b.) “Which-way” effects?

Oven is at 900–1000 K

\Rightarrow many vibrational modes excited

4 modes infrared active \Rightarrow

absorb/emit several radiation quanta on passage through apparatus!

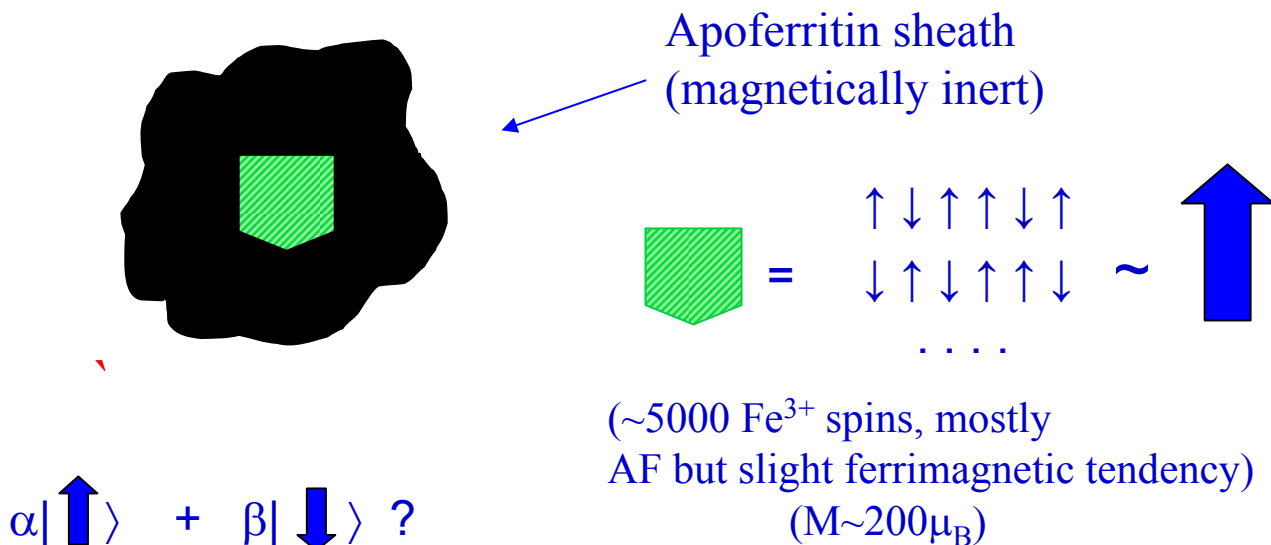


Why doesn't this destroy interference?

*Arndt et al., Nature 401, 680 (1999); Nairz et al., Am. J. Phys. 71, 319 (2003).

The Search for QIMDS (cont.)

2. Magnetic biomolecules*



$$AF: \Delta \sim \hbar \omega_o \exp - N \sqrt{K/J}$$

no. of spins
uniaxial anisotropy
(isotropic)
exchange en.

Raw data: $\chi(\omega)$ and noise spectrum

above ~200 mK, featureless

below ~300 mK, sharp peak at ~ 1 MHz (ω_{res})

$$\omega_{res}^2 \cong \omega_o^2 + M^2 H^2$$

$$\ln \omega_o \sim a - bN \quad \leftarrow \text{no. of spins, exptly. adjustable}$$

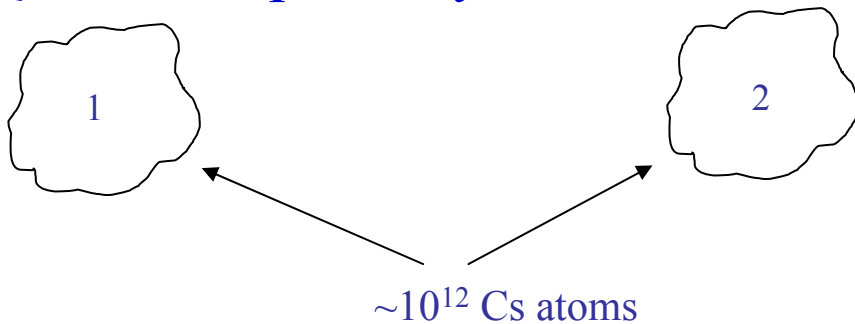
Nb: data is on **physical** ensemble, i.e., only total magnetization measured.

*S. Gider et al., Science 268, 77 (1995).



The Search for QIMDS (cont.)

3. Quantum-optical systems*



for each sample separately, and also for total

$$\begin{aligned} & [J_x, J_y] = iJ_z \\ \Rightarrow & \langle \delta J_{x1} \delta J_{y1} \rangle \geq |J_{z1}| \\ & \langle \delta J_{x2} \delta J_{y2} \rangle \geq |J_{z2}| \\ & \langle \delta J_{x \text{ tot}} \delta J_{y \text{ tot}} \rangle \geq |J_{z \text{ tot}}| \end{aligned}$$

so, if set up a situation s.t.

$$J_{z1} = -J_{z2}$$

must have

$$\begin{aligned} \langle \delta J_{x1} \delta J_{y1} \rangle &> 0 \\ \langle \delta J_{x2} \delta J_{y2} \rangle &> 0 \end{aligned}$$

but may have

$$\langle \delta J_{x \text{ tot}} \delta J_{y \text{ tot}} \rangle = 0$$

(anal. of EPR)

*B. Julsgaard et al., Nature 41, 400 (2001); E. Polzik, Physics World 15, 33 (2002)



Interpretation of idealized expt. of this type:

$$(\text{QM theory} \Rightarrow) \quad \langle \delta J_{x1} \delta J_{y1} \rangle \geq |J_{z1}| \sim N$$

$$\Rightarrow |\delta J_{x1}| \gtrsim N^{1/2}$$

But,

$$(\text{expt} \Rightarrow) \quad \langle \delta J_{xtot} \delta J_{ytot} \rangle \cong 0 \quad (\#)$$

$$\Rightarrow |\delta J_{xtot}| \sim 0$$

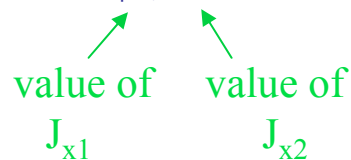
$$\Rightarrow \delta J_{x1} \text{ exactly anticorrelated with } \delta J_{x2}$$

\Rightarrow state is either superposition or mixture of $|n, -n\rangle$

but mixture will not give (#)

\Rightarrow state must be of form

$$\sum_n c_n |n, -n\rangle$$



 value of J_{x1} value of J_{x2}

with appreciable weight for $n \leq N^{1/2}$. \Rightarrow high disconnectivity

Note:

(a) QM used essentially in argument

(b) $D \sim N^{1/2}$ not $\sim N$.

(prob. generic to this kind of expt.)



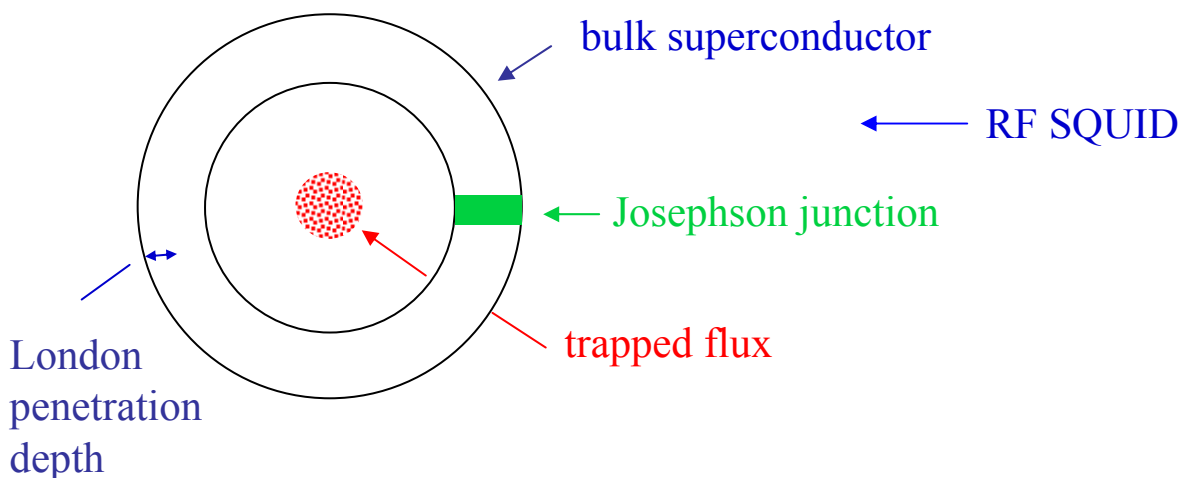
The Search for QIMDS (cont.)

4. Superconducting devices

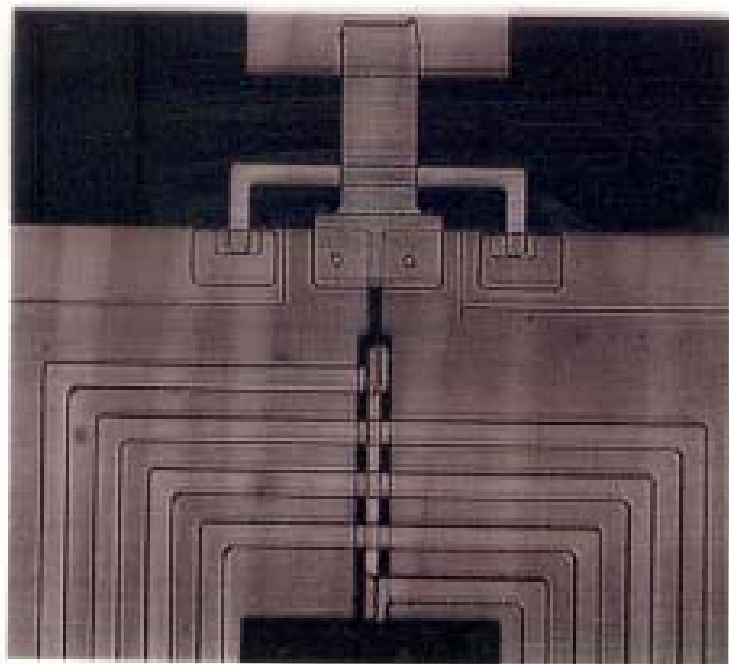
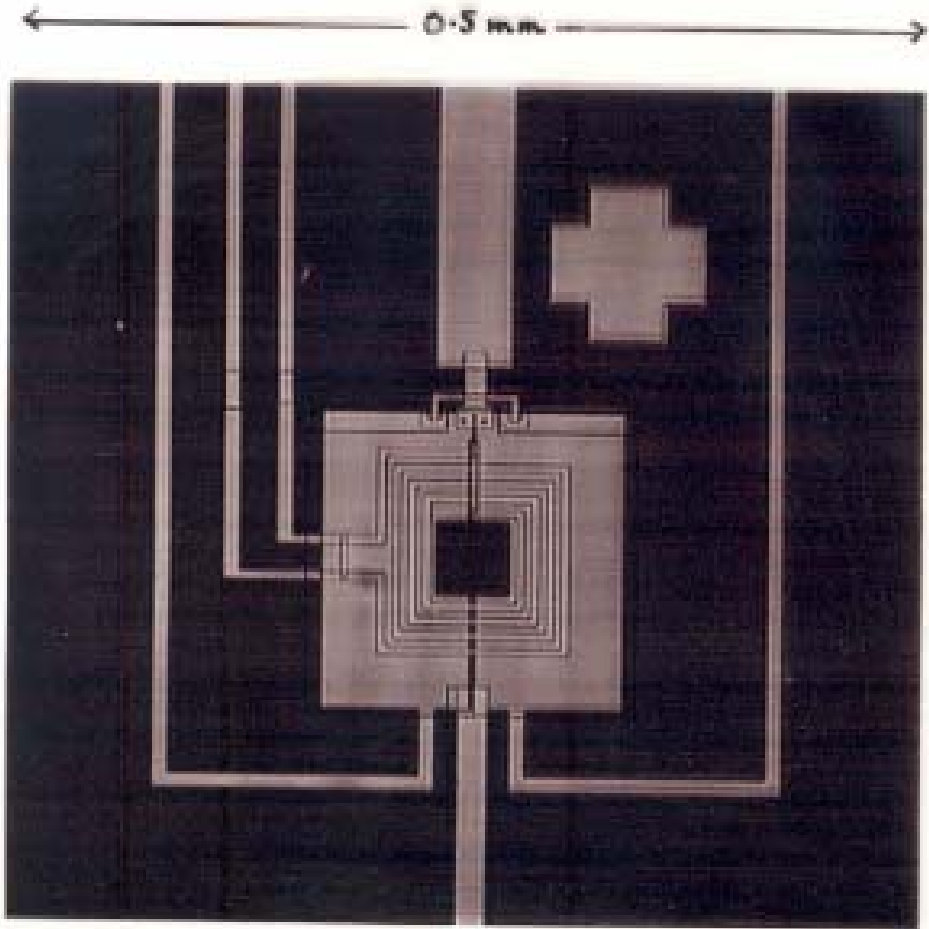
(∇ : not all devices which are of interest for quantum computing are of interest for QIMDS)

Advantages:

- classical dynamics of macrovariable v. well understood
- intrinsic dissipation (can be made) v. low
- well developed technology
- (non-) scaling of S (action) with D.



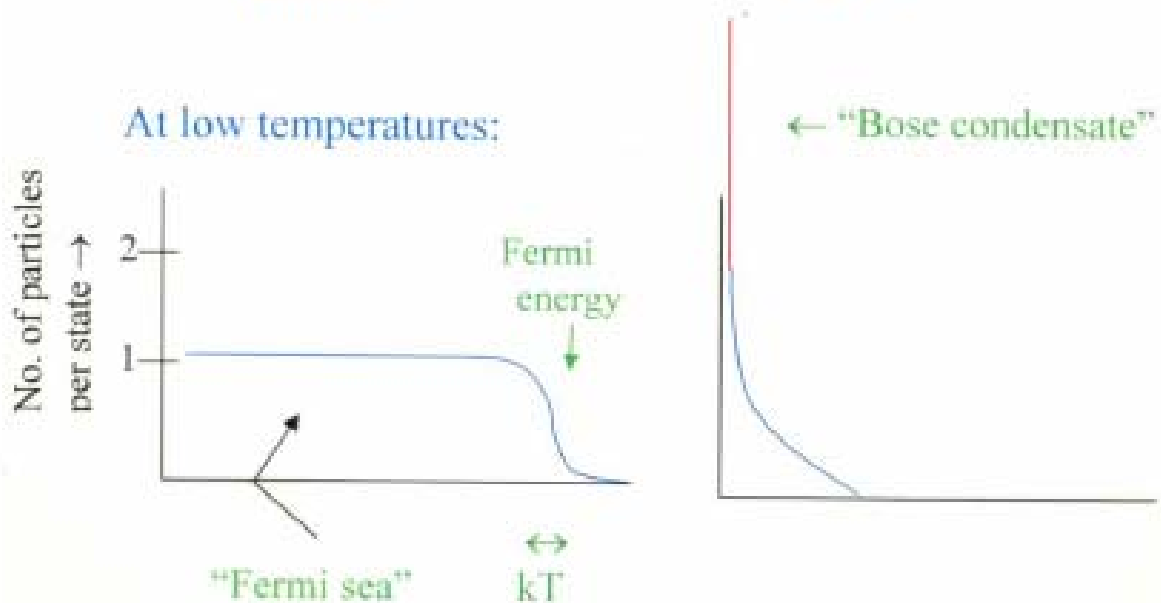
“Macroscopic variable” is trapped flux Φ
[or circulating current I]



PHYSICS OF SUPERCONDUCTIVITY

“Spin” of elementary particles = $\frac{n}{2} \hbar$

0, 1, 2, ... bosons
 $\frac{1}{2}, \frac{3}{2}, \frac{5}{2}, \dots$ fermions



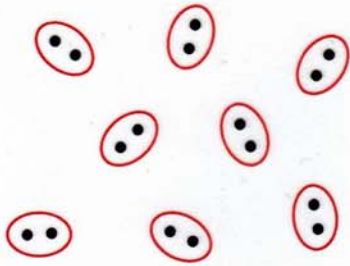
Electrons in metals: spin $\frac{1}{2} \Rightarrow$ fermions

But a compound object consisting of an **even** no. of fermions has spin 0, 1, 2 ... \Rightarrow boson.

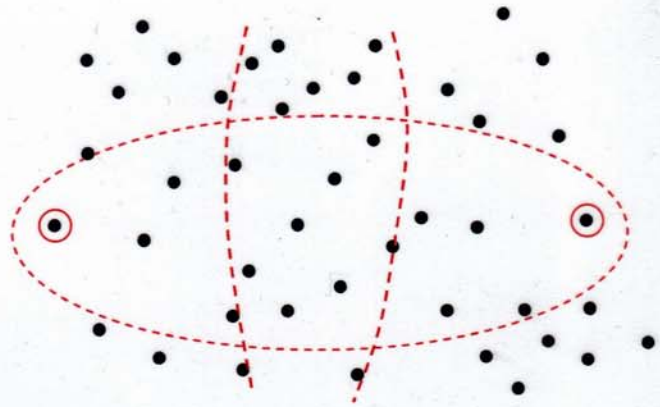
(Ex: $2p + 2n + 2e = {}^4\text{He}$ atom)

\Rightarrow can undergo Bose condensation

Pairing of electrons:



“di-electronic molecules”



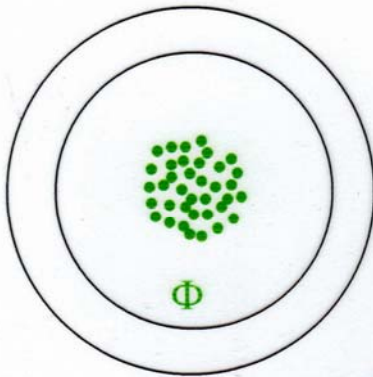
Cooper Pairs

In simplest (“BCS”) theory, Cooper pairs, once formed, must automatically undergo Bose condensation!

⇒ must all do exactly the same thing at the same time (also in nonequilibrium situation)



SUPERCONDUCTING RING IN EXTERNAL MAGNETIC FLUX:



$$E \propto K^2$$

Quantization condition for
“particle” of charge $2e$ (Cooper
pair):

$$K \equiv \oint \mathbf{v} \cdot d\mathbf{l} = \frac{h}{2m} (n - \Phi/\Phi_0)$$

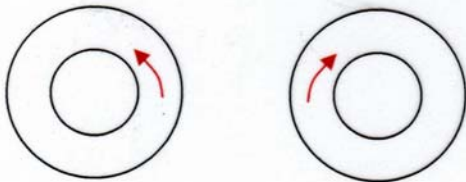
integer
“flux quantum”
 $h/2e$

A. $\Phi = 0$: groundstate unique ($n = 0$)

\Rightarrow all pairs at rest.

B. $\Phi = 1/2 \Phi_0$: groundstate doubly degenerate

($n = 0$ or $n = 1$)



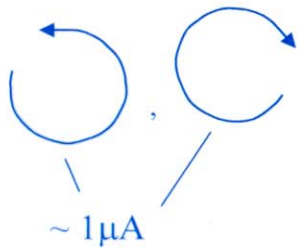
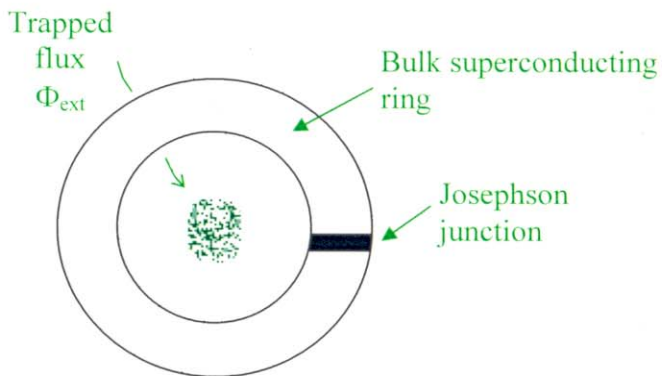
Either all pairs rotate clockwise

Or all pairs rotate anticlockwise

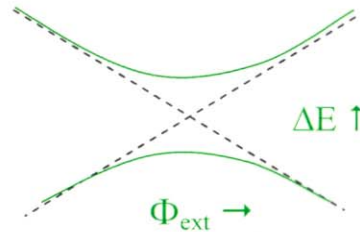
Note: state with 50% ↘ and 50% ↗

strongly forbidden by energy considerations

Josephson circuits



$$\Psi = 2^{-1/2} (|\downarrow\rangle + |\uparrow\rangle)$$

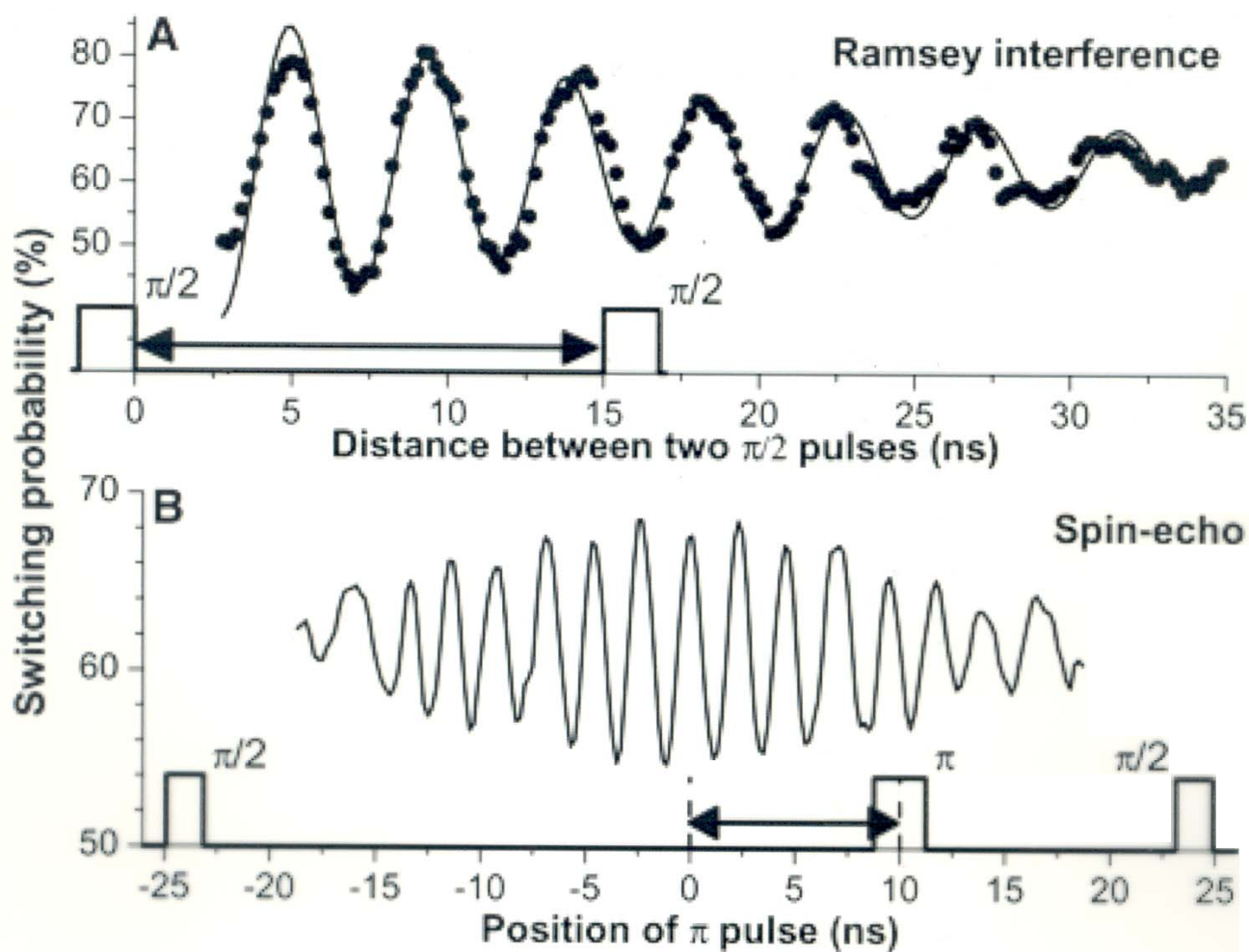


Evidence: (a) spectroscopic:
(SUNY, Delft 2000)

(b) real-time oscillations (like NH_3)

between \downarrow and \uparrow

(Saclay 2002, Delft 2003) ($Q_\varphi \sim 50-350$)



From I. Chiorescu, Y. Nakamura, C.J.P. Harmans, and J. E. Mooij, *Science*, **299**, 1869 (2003)

WHAT IS THE DISCONNECTIVITY “D” (“SCHRÖDINGER’S-CATTINESS”) OF THE STATES OBSERVED IN QIMDS EXPERIMENTS?

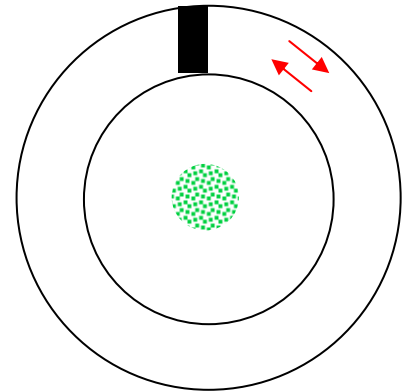
i.e., how many “microscopic” entities are “behaving differently” in the two branches of the superposition?

Fullerene (etc.) diffraction experiments: straightforward, number of “elementary” particles in C_{60} (etc.) (~ 1200)

Magnetic biomolecules: number of spins which reverse between the two branches (~ 5000)

Quantum-optical experiments
SQUIDS } matter of definition

e.g. SQUIDS (SUNY experiment):



(a) naïve approach: no. of C. pairs

$$\Psi_{\curvearrowright} \sim \chi_{\curvearrowright}^{N/2}, \quad \Psi_{\curvearrowleft} = \chi_{\curvearrowleft}^{N/2}$$

mutually orthogonal C. pair w.f.

$$\Rightarrow D \sim N \sim 10^9 - 10^{10} \quad \uparrow: \text{Fermi statistics!}$$

(b) how many single electrons do we need to displace in momentum space to get from Ψ_{\curvearrowright} to Ψ_{\curvearrowleft} ? (Korsbakken et al., preprint, Nov. 08)

$$\Rightarrow D \sim N(\nu_s / \nu_F) \sim 10^3 - 10^4 \quad \uparrow: \text{intuitively, severe underestimate in “BEC” limit (e.g. Fermi alkali gas)}$$

(c) macroscopic eigenvalue of 2-particle density matrix (corresponding to (fairly) orthogonal states in 2 branches):

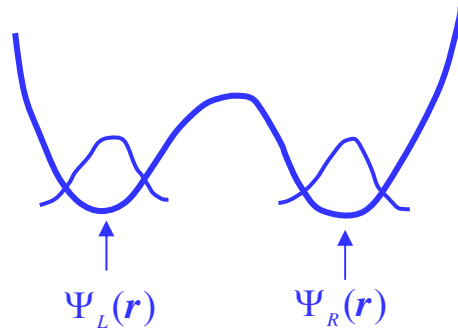
$$\Rightarrow D \sim N(\Delta / \varepsilon_F) \sim 10^6 - 10^7$$

<u>SYSTEM</u>	<u>“EXTENSIVE DIFFERENCE”</u>	<u>DISCONNECTIVITY/ ENTANGLEMENT</u>
Single e^-	1	1
Neutron in interferometer	$\sim 10^9$	1
QED cavity	~ 10	$\lesssim 10$
Cooper-pair box	$\sim 10^5$	2
C_{60}	~ 1100	~ 1100
Ferritin	~ 5000 (?)	~ 5000
Aarhus quantum- optics expt.	$\sim 10^6$ ($\propto N^{1/2}$)	$\sim 10^6$
SUNY SQUID expt.	$\sim 10^9 - 10^{10}$ ($\propto N$)	($10^4 - 10^{10}$)
Smallest visible dust particle	$\sim 10^{19}$	($10^3 - 10^{15}$)
Cat	$\sim 10^{34}$	$\sim 10^{25}$

More possibilities for QIMDS:

(a) BEC's of ultracold alkali gases:

Bose-Einstein condensates



(Gross-Pitaevskii)



Ordinary GP state:

$$\Psi_N = (a\psi_L(\mathbf{r}) + b\psi_R(\mathbf{r}))^N$$

“Schrödinger-cat” state (favored if interactions attractive):

$$\Psi_N = a(\psi_L(\mathbf{r}))^N + b(\psi_R(\mathbf{r}))^N$$

problems:

(a) extremely sensitive to well asymmetry ΔE
 (energy stabilizing arg (a/b) $\sim t^N \sim \exp - NB/\hbar$)

so ΔE needs to be
 \exp' ly small in N

↑
 single-particle tunnelling
 matrix element

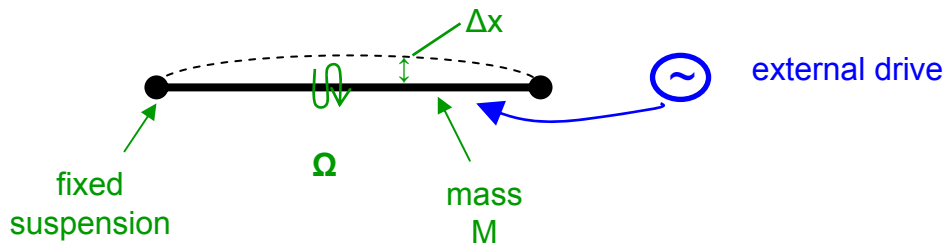
(b) detection: tomography unviable for $N \gg 1$,
 \Rightarrow need to do time-sequence experiments (as in SQUIDS), but
 period v. sensitive e.g. to exact value of N

More possibilities for QIMDS (cont):

(b) MEMS

← micro-electromechanical systems

Naïve picture:



$M \sim 10^{-18}$ kg (NEMS)

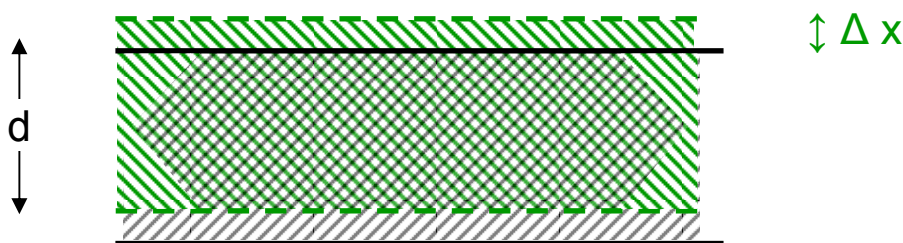
$\sim 10^{-21}$ kg (C nanotube)

$\Omega \sim 2\pi \cdot 10^8$ Hz

$\Rightarrow T_{\text{eq}} \equiv \hbar \Omega / k_B \sim 5$ mK, $x_0 \sim 10^{-12}$ m

↑ rms groundstate displacement

Actually:



In practice, $\Delta x \ll d$.

⚠ Problem: simple harmonic oscillator!

(One) solution: couple to strongly nonlinear microscopic system, e.g. trapped ion. (Wineland)

Can we test GRWP/Penrose dynamical reduction theories?

WHAT HAVE WE SEEN SO FAR?

1. If we interpret raw data in QM terms, then can conclude we have a **quantum superposition rather than a mixture** of meso/macrospectically distinct states.

However, “only 1 degree of freedom involved.”

2. Do data exclude **general** hypothesis of macrorealism?

NO

3. Do data exclude **specific** macrorealistic theories?

e.g. GRWP ← **Ghirardi, Rimini, Weber, Pearle**

NO (fullerene diffraction: N not large enough, SQUIDS:
no displacement of COM between branches)

Would MEMS experiments (if in agreement with QM) exclude GRWP?

alas: $\Gamma_{coll} \propto \Delta x,$ $\Gamma_{dec} \propto (\Delta x)^2$

↑ ↑

collapse rate decoherence rate

in GRWP theory acc. to QM

⇒ do not gain by going to larger Δx
(and small Δx may not be enough to test GRWP)



HOW CONFIDENT ARE WE ABOUT (STANDARD QM'I) DECOHERENCE RATE?

Theory:

- (a) model environment by oscillator bath (may be questionable)
- (b) Eliminate environment by standard Feynman-Vernon type calculation (seems foolproof)

Result (for SHO):

$$\Gamma_{dec} \sim \Gamma \left(\frac{k_B T}{\hbar \Omega} \right) \cdot \left(\frac{\Delta x}{x_0} \right)^2$$

provided $k_B T \gg \hbar \Omega$

energy relaxation rate (Ω/Q)

zero-point rms displacement

ARE WE SURE THIS IS RIGHT?

Tested (to an extent) in cavity QED: never tested (?) on MEMS.

Fairly urgent priority!

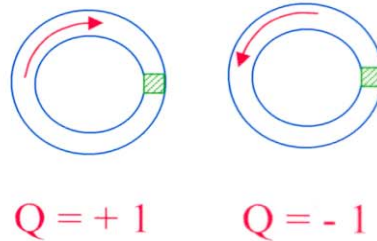


Where do we go from here?

1. Larger values of Λ and/or D ?
(Diffraction of virus?)
2. Alternative Dfs. of “Measures” of Interest
 - More sophisticated forms of entanglement?*
 - Biological functionality (e.g. superpose states of rhodopsin?)
 - Other (e.g. GR)

* 3. Exclude Macrorealism

Suppose: Whenever
observed, $Q = \pm 1$.



Df. of “MACROREALISTIC” Theory:

- “COMMON SENSE”?
- I. $Q(t) = \pm 1$ at (almost) $\forall t$,
whether or not observed.
 - II. Noninvasive measurability
 - III. Induction

Can test with existing SQUID Qubits!

*S. Aaronson, STOC 2004, p. 118.

Df:

$$K \equiv K(t_1 t_2 t_3 t_4) \equiv \langle Q(t_1) Q(t_2) \rangle_{\text{exp}} + \langle Q(t_2) Q(t_3) \rangle_{\text{exp}} \\ + \langle Q(t_3) Q(t_4) \rangle_{\text{exp}} - \langle Q(t_1) Q(t_4) \rangle_{\text{exp}}$$

Take $t_2 - t_1 = t_3 - t_2 = t_4 - t_3 = \pi/4\Delta$ ← tunnelling frequency

Then,

- (a) Any macrorealistic theory: $K \leq 2$
- (b) Quantum mechanics, ideal: $K = 2.8$
- (c) Quantum mechanics, with all the real-life complications: $K > 2$ (but < 2.8)

Thus: to extent analysis of (c) within quantum mechanics is reliable, **can force nature to choose between** macrorealism and quantum mechanics!

Possible outcomes:

- (1) Too much noise $\Rightarrow K_{\text{QM}} < 2$
- (2) $K > 2 \Rightarrow$ macrorealism refuted
- (3) $K < 2$: ? !

