

# **THE PHYSICS OF YBCO (and other high-temperature superconductors)**

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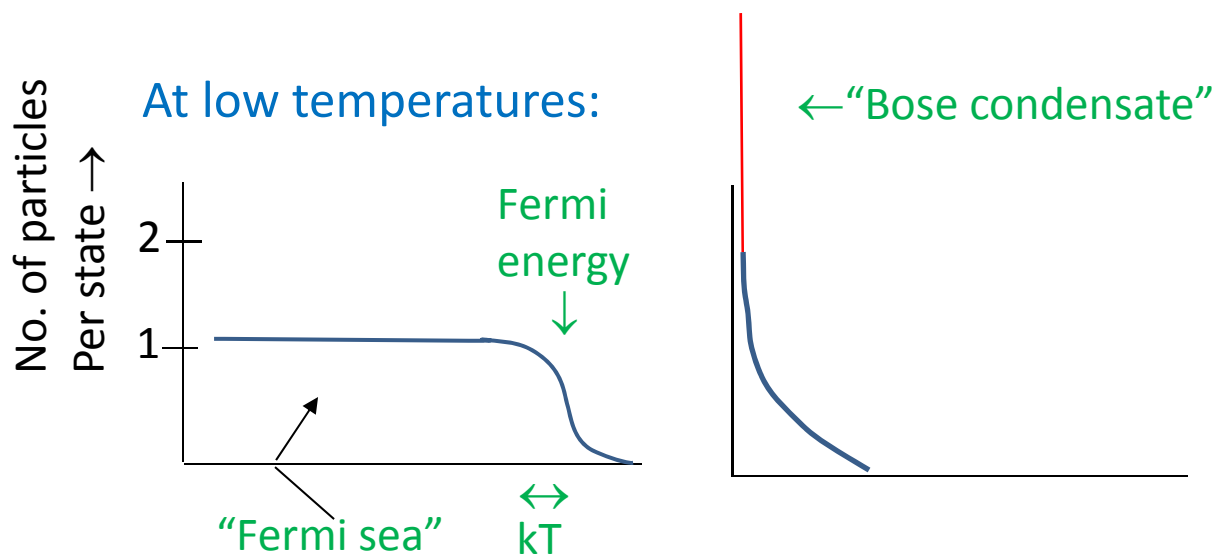
17 November 2014



## PHYSICS OF SUPERCONDUCTIVITY

“Spin” of elementary particles =  $\frac{n}{2} \frac{h}{2\pi}$

0, 1, 2....	bosons
$\frac{1}{2}, \frac{3}{2}, \frac{5}{2}, \dots$	fermions



Electrons in metals: spin  $\frac{1}{2} \Rightarrow$  fermions

But a compound object consisting of an **even** number of fermions has spin 0, 1, 2 ...  $\Rightarrow$  boson.

(Ex:  $2p + 2n + 2c = {}^4\text{He}$  atom)

$\Rightarrow$  can undergo Bose condensation





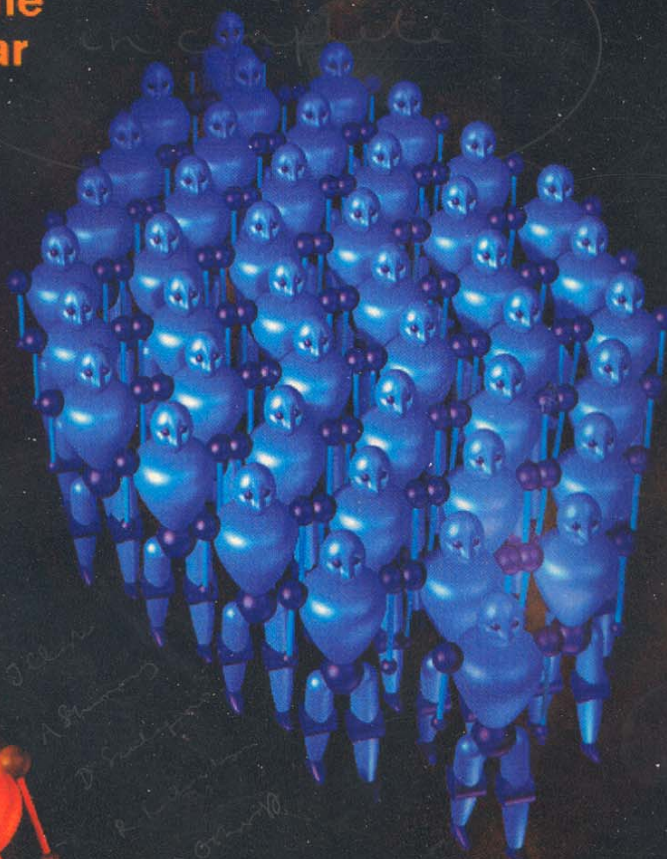
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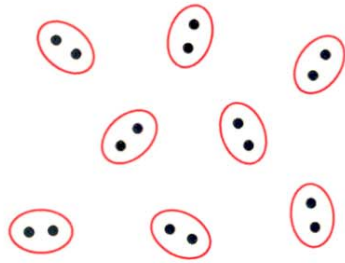
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Molecule  
of the  
Year

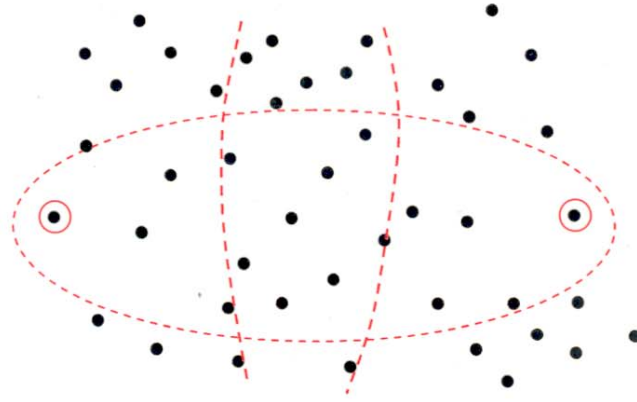


the  
Bose-Einstein  
Condensate

Pairing of electrons:



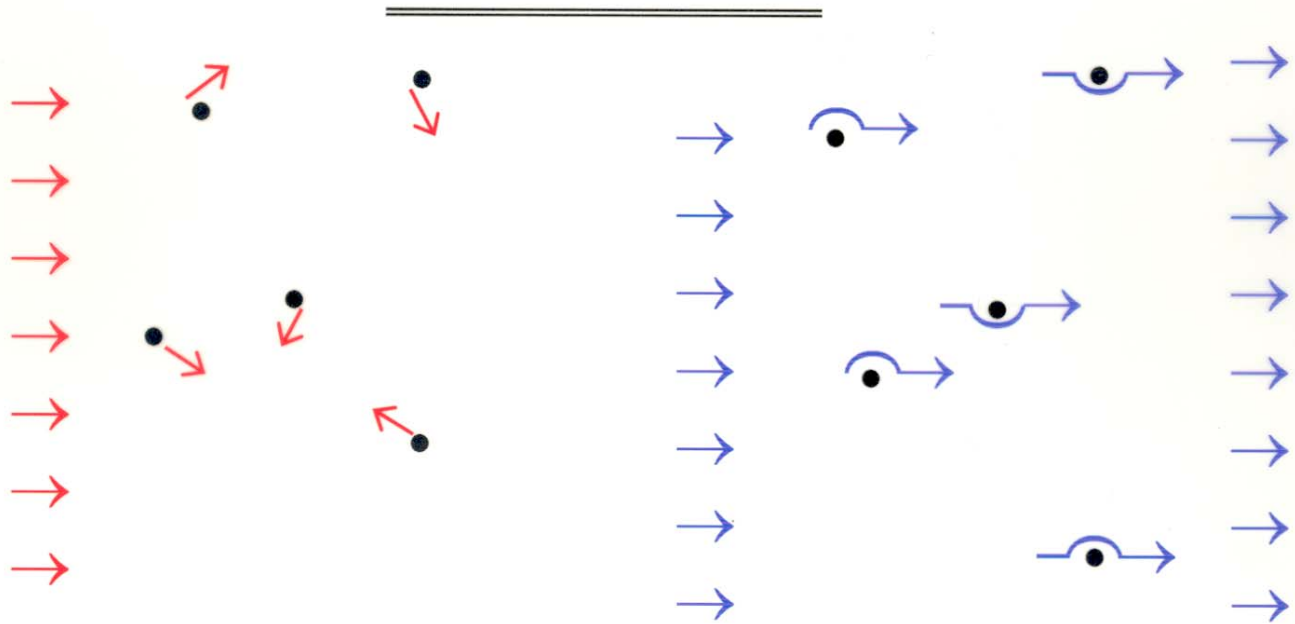
“di-electronic molecules”



Cooper Pairs

In simplest (“BCS”) theory, Cooper pairs, once formed, must automatically undergo **Bose condensation!**

⇒ must all do **exactly the same thing at the same time** (also in nonequilibrium situation)

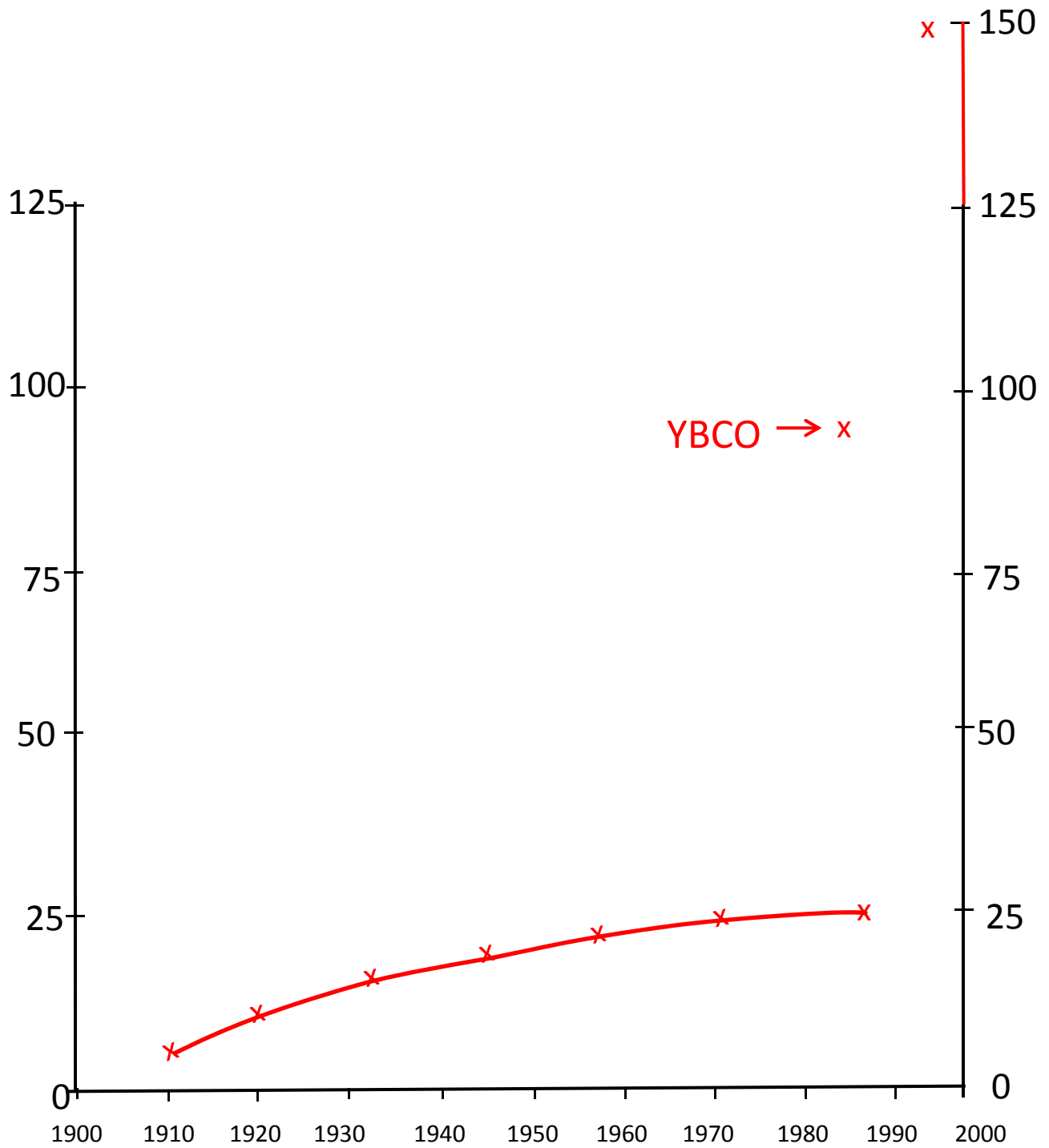


Single electrons in  
normal metal

Cooper pairs in  
superconductor

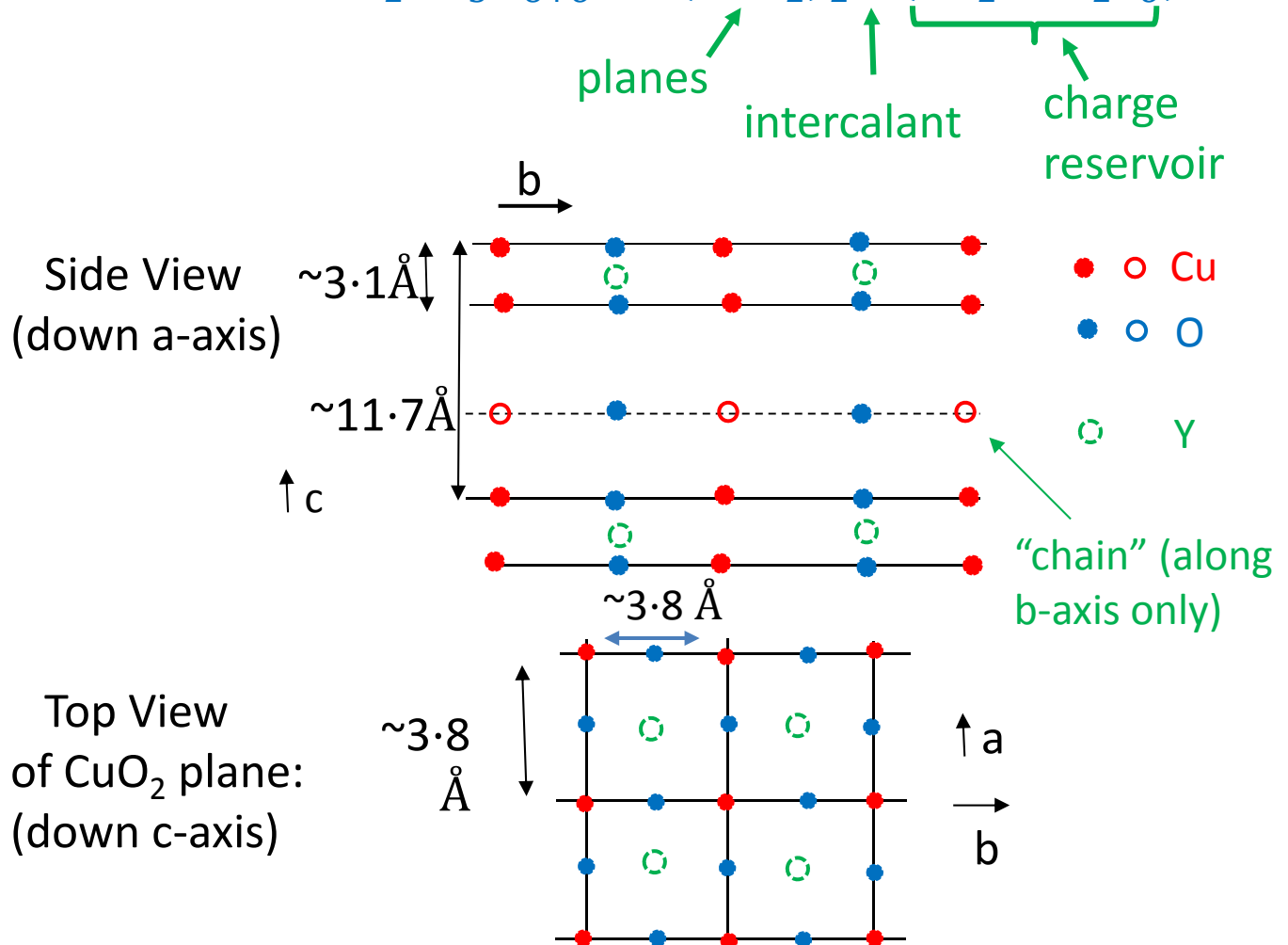


HISTORY OF THE HIGHEST TEMPERATURE  
("T<sub>c</sub>") AT WHICH SUPERCONDUCTIVITY KNOWN





# YBCO– THE “E. COLI” (?) OF CUPRATE SUPERCONDUCTIVITY



Some idiosyncracies of *YBCO* among cuprates:

1. Relation between nonstoichiometry ( $\delta$ ) and doping of planar unit cell ( $p$ ) complicated (contrast e.g.



2. No homologues (contrast e.g.  $Tl_2Ba_2Ca_nCu_{n+1}O_{4+3n+2}$ )

3. Very non-negligible effect of chains

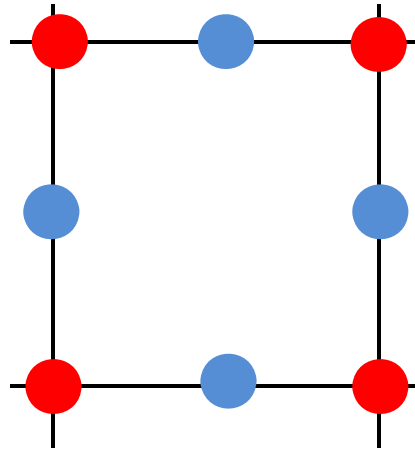
(e.g.  $b$ -axis conductivity  $\cong 2.5$   $a$ -axis one  $\Rightarrow$  one chain



contributes as much as both planes!)

## ELECTRON STATES IN THE $\text{CuO}_2$ PLANES

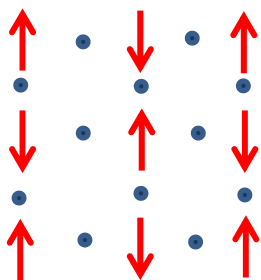
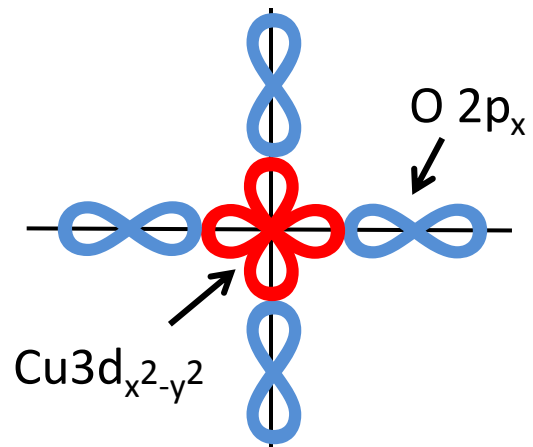
- Cu: neutral atom has closed s and p shells plus  $3d^{10} 4s^1$
- O : neutral atom has closed s shells plus  $2p^4$



In “parent” compound  $\text{YBa}_2\text{Cu}_3\text{O}_6$ , Cu is ++ ( $3d^9$ )  
 O is -- ( $2p^6$ , closed shell), so **one “hole” per  $\text{CuO}_2$  unit.**

(actually believed to be hybrid of Cu  $3d_{x^2-y^2}$  and O  $2p_{x,y}$  states)

In parent compound, holes form **Mott antiferromagnetic insulator:**

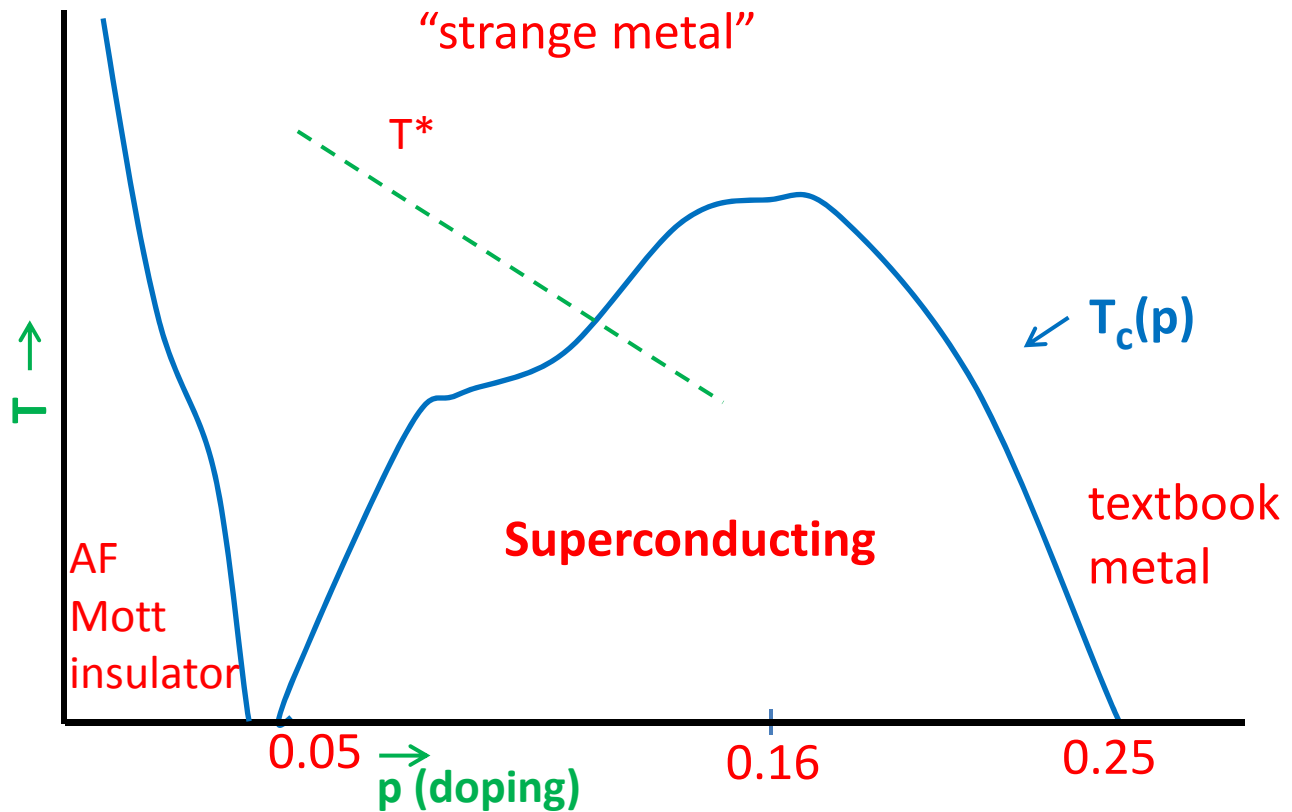


When extra O is added (in chains) some of the extra holes created migrate to planes:

$p \equiv$  number of extra holes per  $\text{CuO}_2$  unit.

Almost universal belief: **extra holes in  $\text{CuO}_2$  planes are main actors in superconductivity of cuprates.**

## THE “CANONICAL” CUPRATE PHASE DIAGRAM (IN ZERO MAGNETIC FIELD)



Note: (a) complete phase diagram not usually accessible in single system (including YBCO), so obtained by “pastiche”

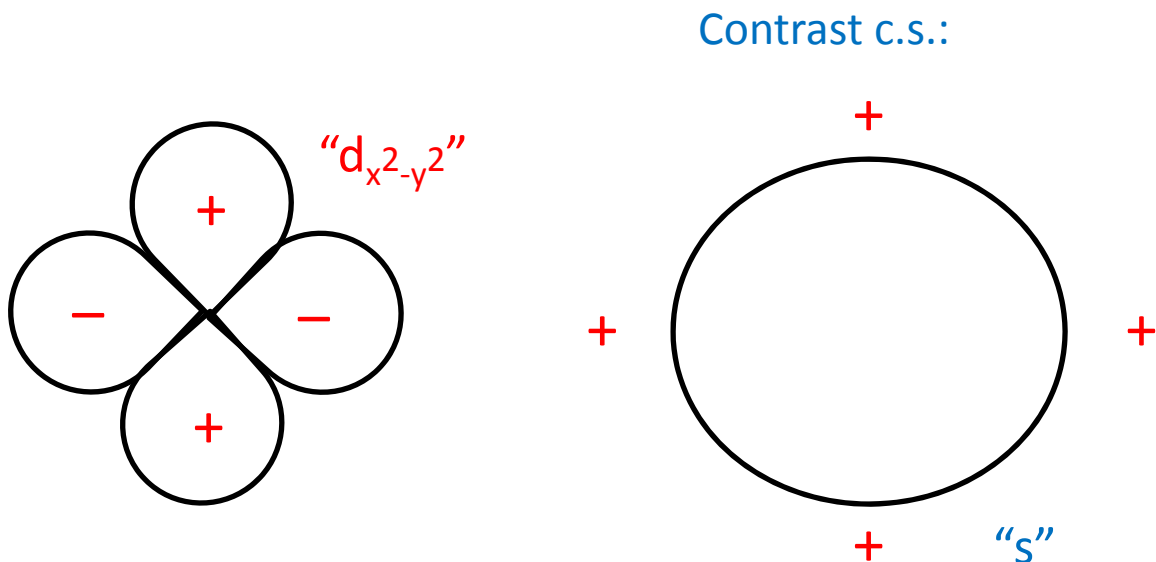
(b) in YBCO, both superfluid density and condensation energy peak to **right** of  $T_c^{(max)}$ .

(c) nature of  $T^*$  **line** unclear.



## A FEW THINGS WE (THINK WE) KNOW ABOUT THE SUPERCONDUCTING STATE OF YBCO (and other cuprates)

1. Main locus of superconductivity is **CuO<sub>2</sub> planes**.
2. Mechanism of superconductivity is (as in traditional superconductors) formation and (pseudo-) Bose condensation of **Cooper pairs**.
3. Phonons (mostly) unimportant.
4. Primary mechanism of formation of Cooper pairs is **single-plane** (or at most single – multilayer).
5. Nature of Cooper pairs:
  - (a) size:  $\sim 15\text{-}30 \text{ \AA}$  (contrast  $\sim 10^4 \text{ \AA}$  for Al!)
  - (b) formed from time-reversed states (as in c.s.\*)
  - (c) spin state is singlet ( $\uparrow\downarrow - \downarrow\uparrow$ ) (as in c.s.)
  - (d) orbital state:



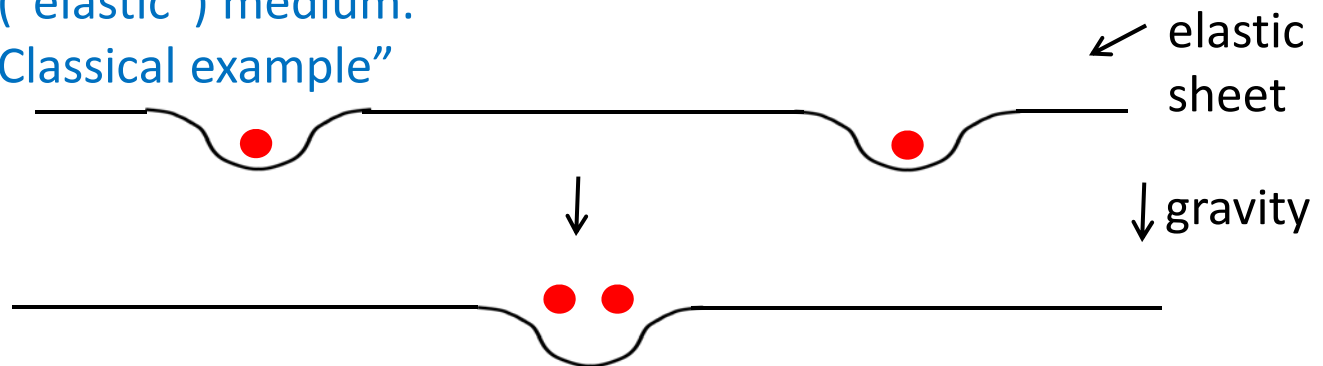
\*conventional superconductor

## THE \$64K QUESTION: WHAT IS THE “MECHANISM” OF FORMATION OF COOPER PAIRS?

Scenario no. 1: Start with (nearly) **noninteracting** electrons.  
provide mechanism of **attraction**.

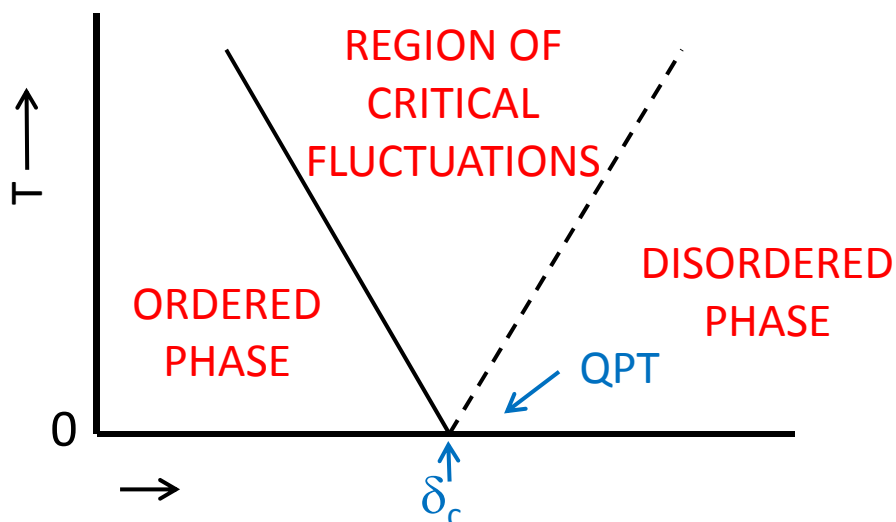
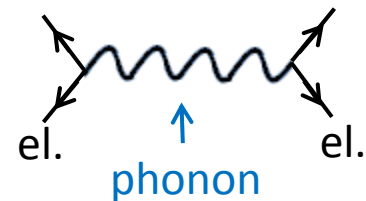
One familiar way of doing this: couple linearly to deformable (“elastic”) medium.

Classical example”



QM version of this is **exchange of virtual low-energy excitation** e.g. in traditional superconductors, a phonon:

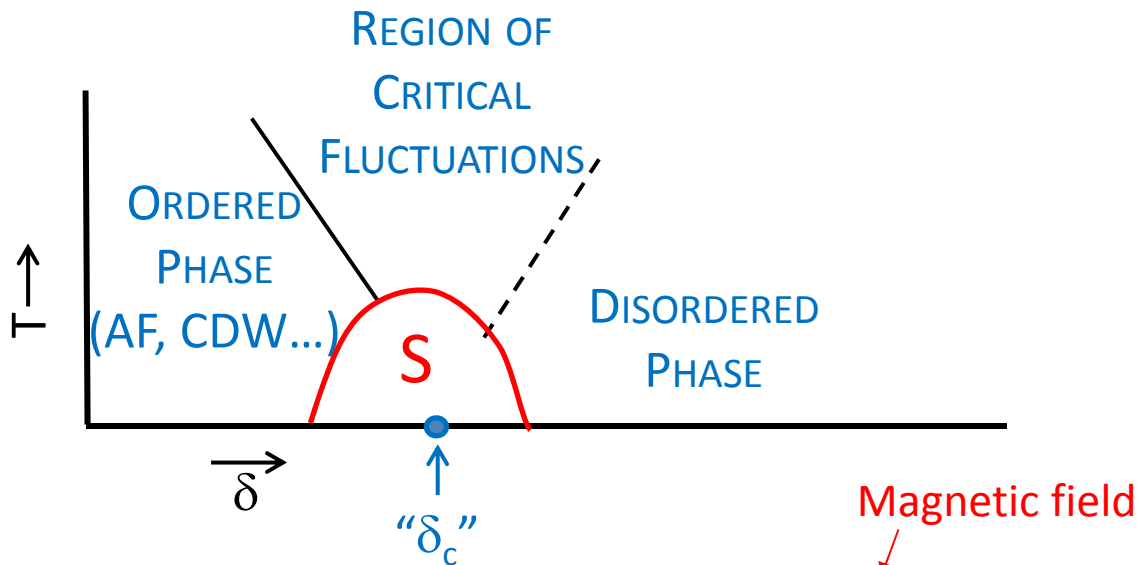
A plausible source of low-energy excitations : “quantum phase transition” (QPT)



$\delta$  (control parameter, e.g. pressure, magnetic field, doping....)

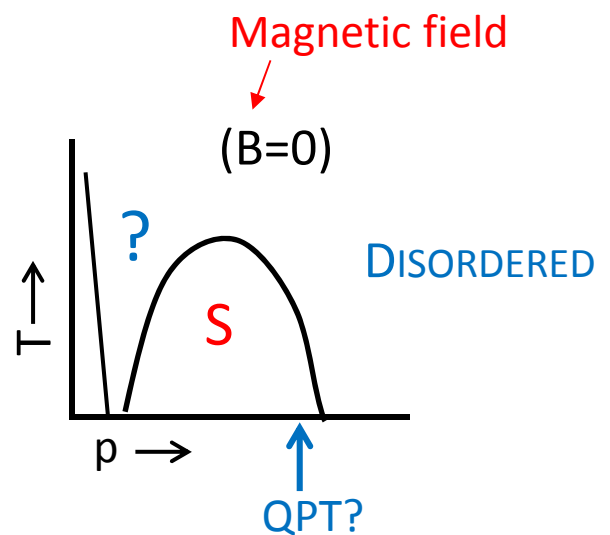


## A UBIQUITOUS PHENOMENON IN QUASI-2D SYSTEMS (HEAVY FERMIONS, TM CHALCOGENIDES, FERROPNICRIDES...)

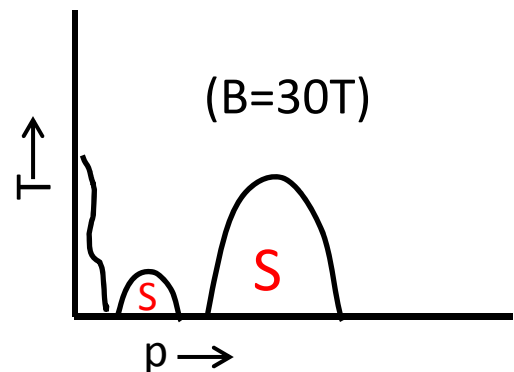


So, in cuprates,

- (1) is there a QPT underlying the superconducting dome?
- (2) if so, what is the nature of the ordered phase (and why is it so difficult to see directly)?
- (3) is the mechanism of superconductivity the exchange of low-energy fluctuations associated with the QPT?



Very recent input: in high magnetic fields superconductivity dome splits  $\Rightarrow$  **two** different ordered phases??



Scenario no. 2: Start with **strongly interacting** electrons (i.e. with strong Coulomb repulsion), and by forming Cooper pairs **reduce Coulomb repulsion**. (e.g. by enhancing screening).

In any case, Coulomb energy is a sum of contributions from different  $q, \omega$ . So:

(a) at the N $\rightarrow$ S transition, is Coulomb energy saved or expended?

(b) in either case, in which regions of  $q$  and  $\omega$  does most of the saving/expenditure occur?

Can in principle answer by electron energy loss spectroscopy (EELS) experiments – now starting.

SOME MAJOR UNKNOWNNS ABOUT CUPRATE (and other high-temperature) SUPERCONDUCTIVITY:

1. Why is 2-dimensionality so important?
2. Why is proximity to a QPT so important?
3. Why is multiplicity of  $\text{CuO}_2$  planes so important?
4. Will we ever find a robust room-temperature superconductor
  - (a) in a cuprate or cuprate-related material
  - (b) somewhere completely different?

