

Does the thermopower solve the riddle
of high temperature superconductivity?

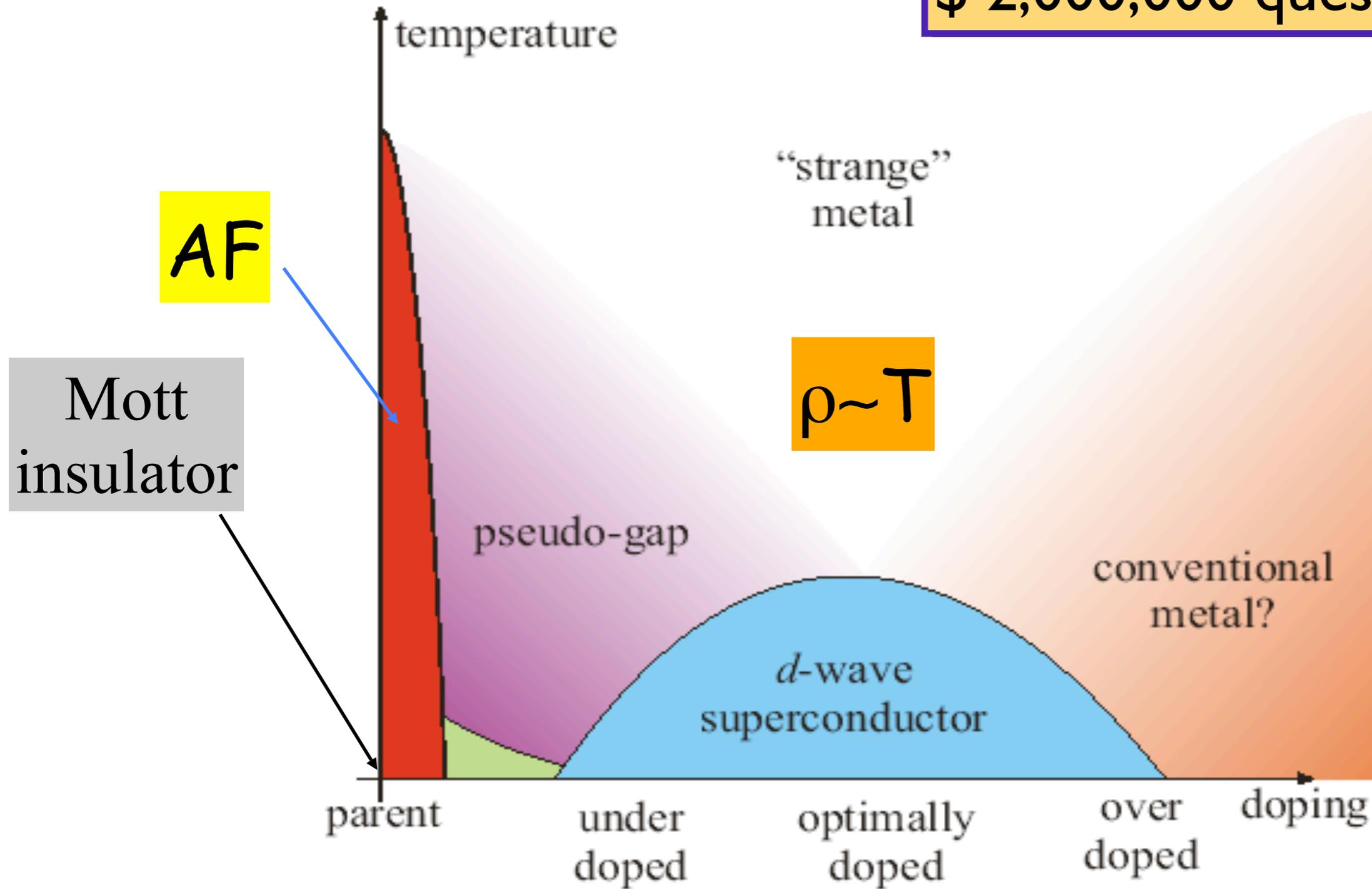
Thanks to: T.-P. Choy, R. G. Leigh, S.
Chakraborty, S. Hong

(PRL, 99, 46404 (2007);

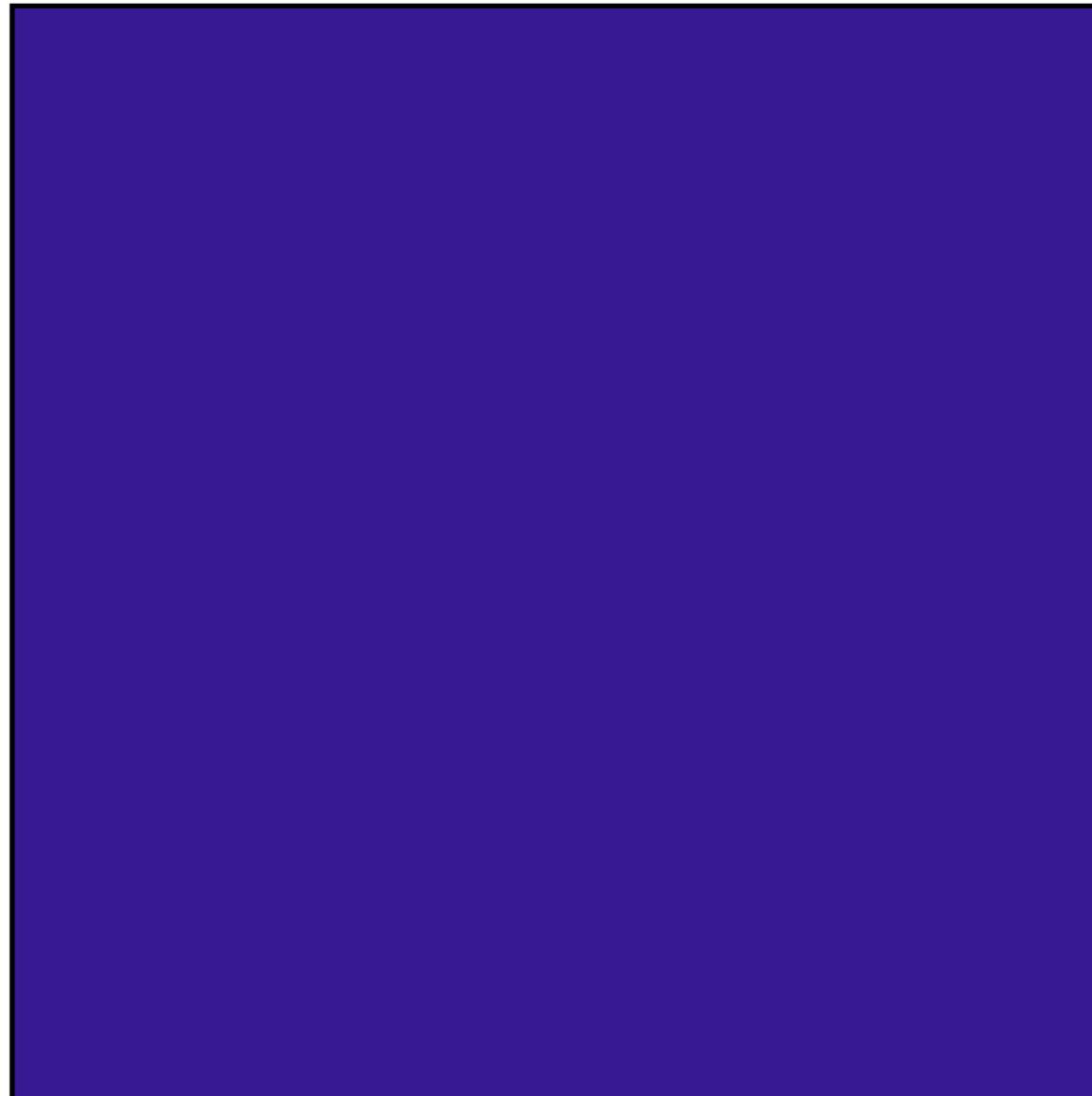
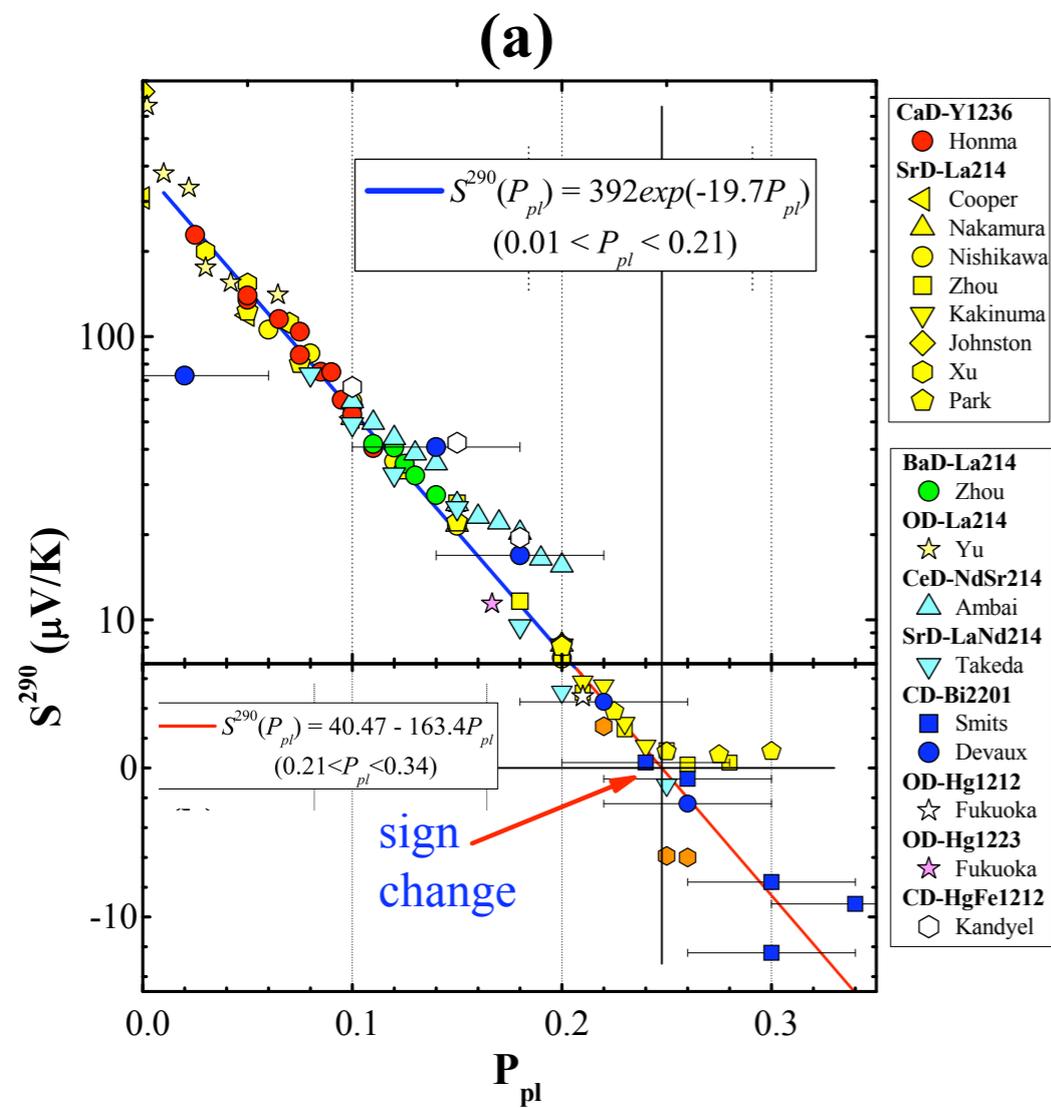
PRB, 77, 14512 (2008); ibid, 77, 104524 (2008))

Why is the T_c region dome-shaped?

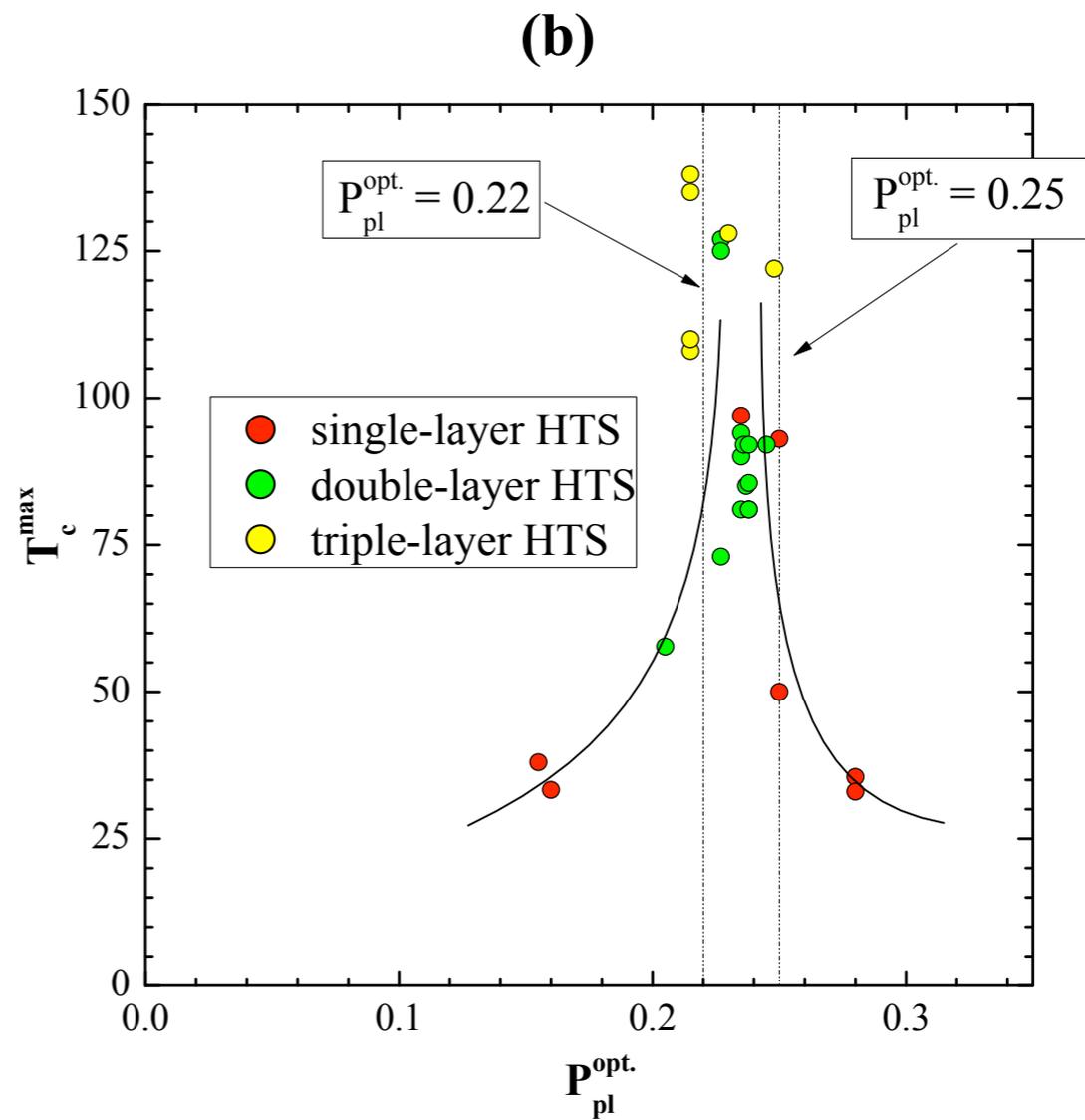
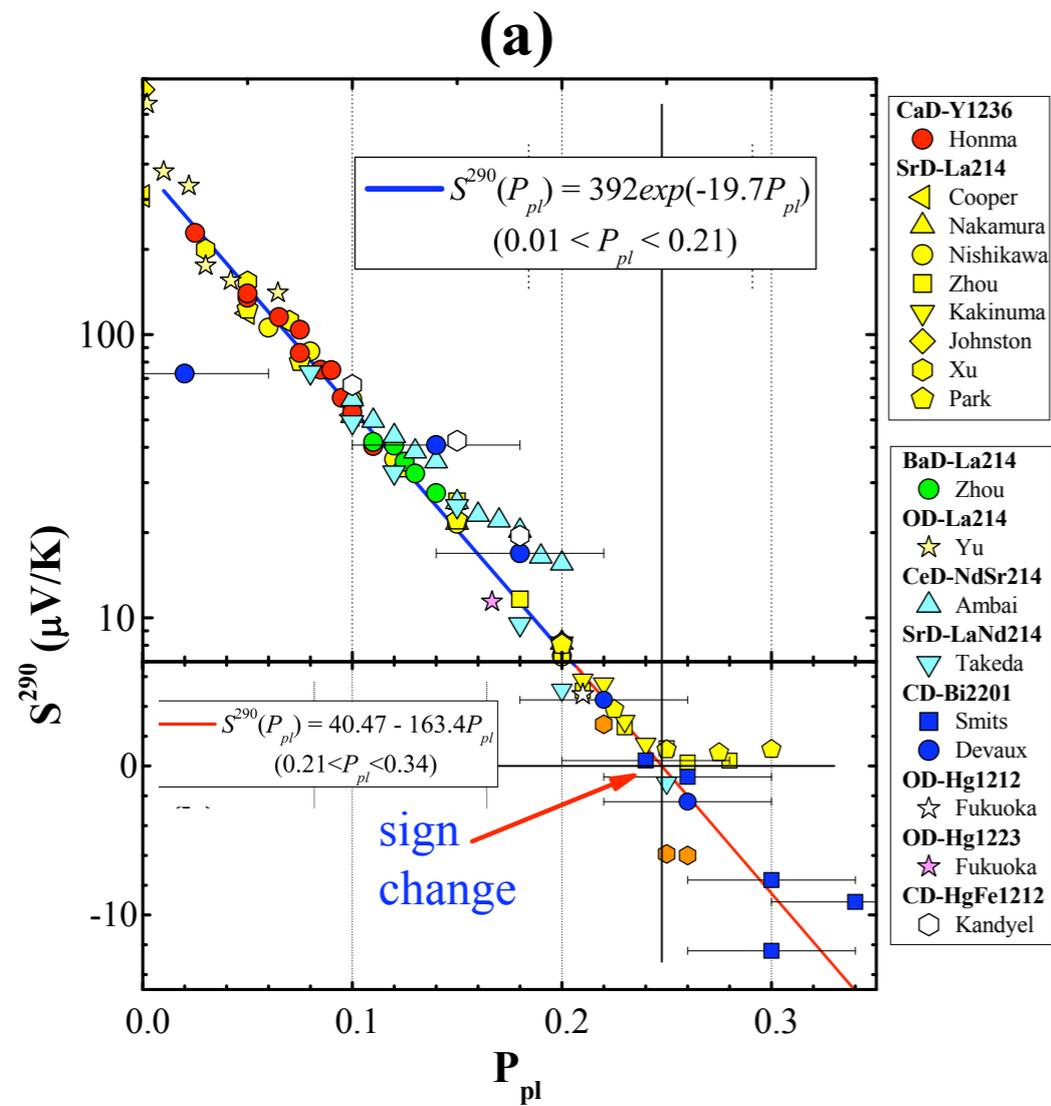
\$ 2,000,000 question?



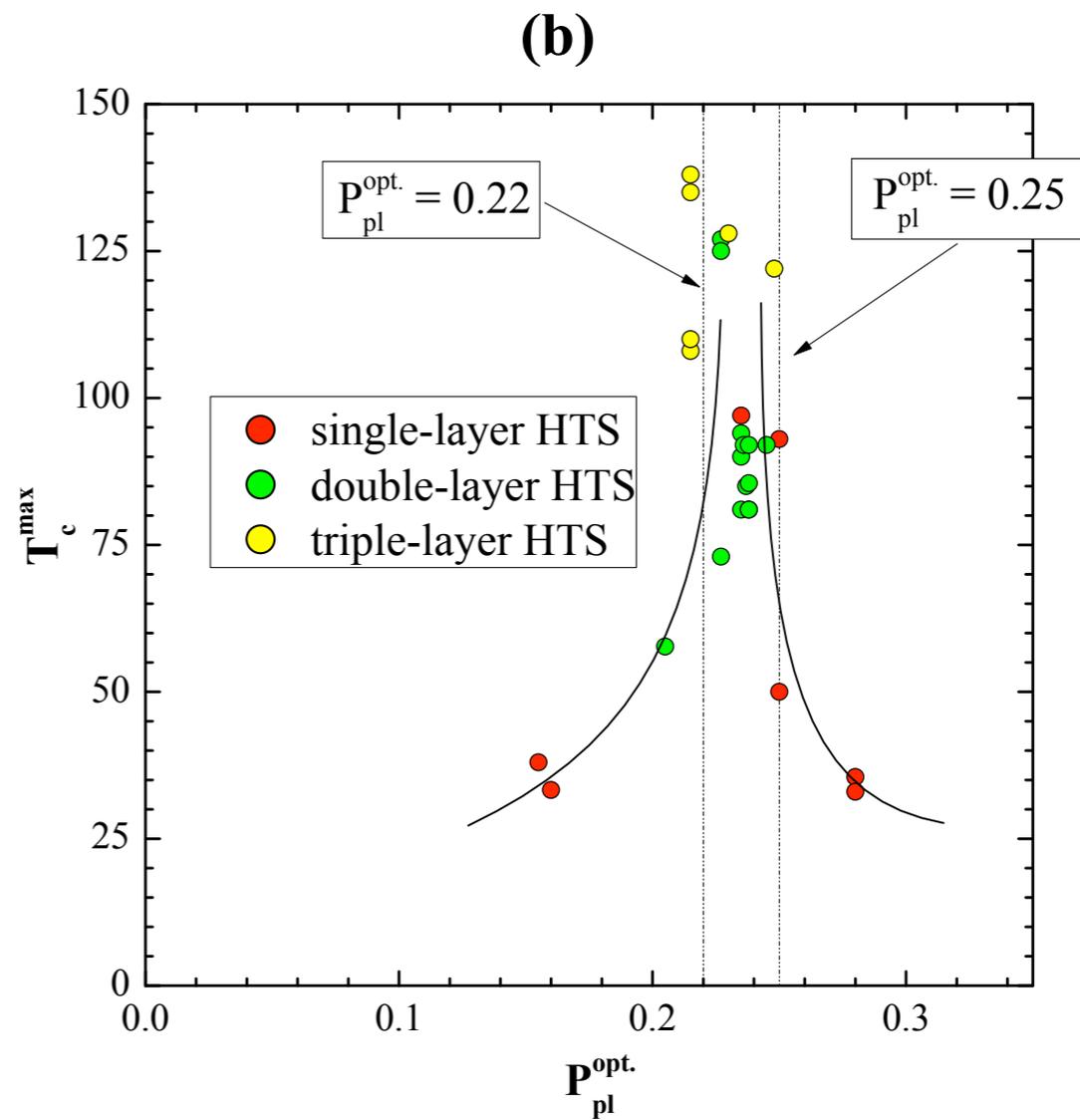
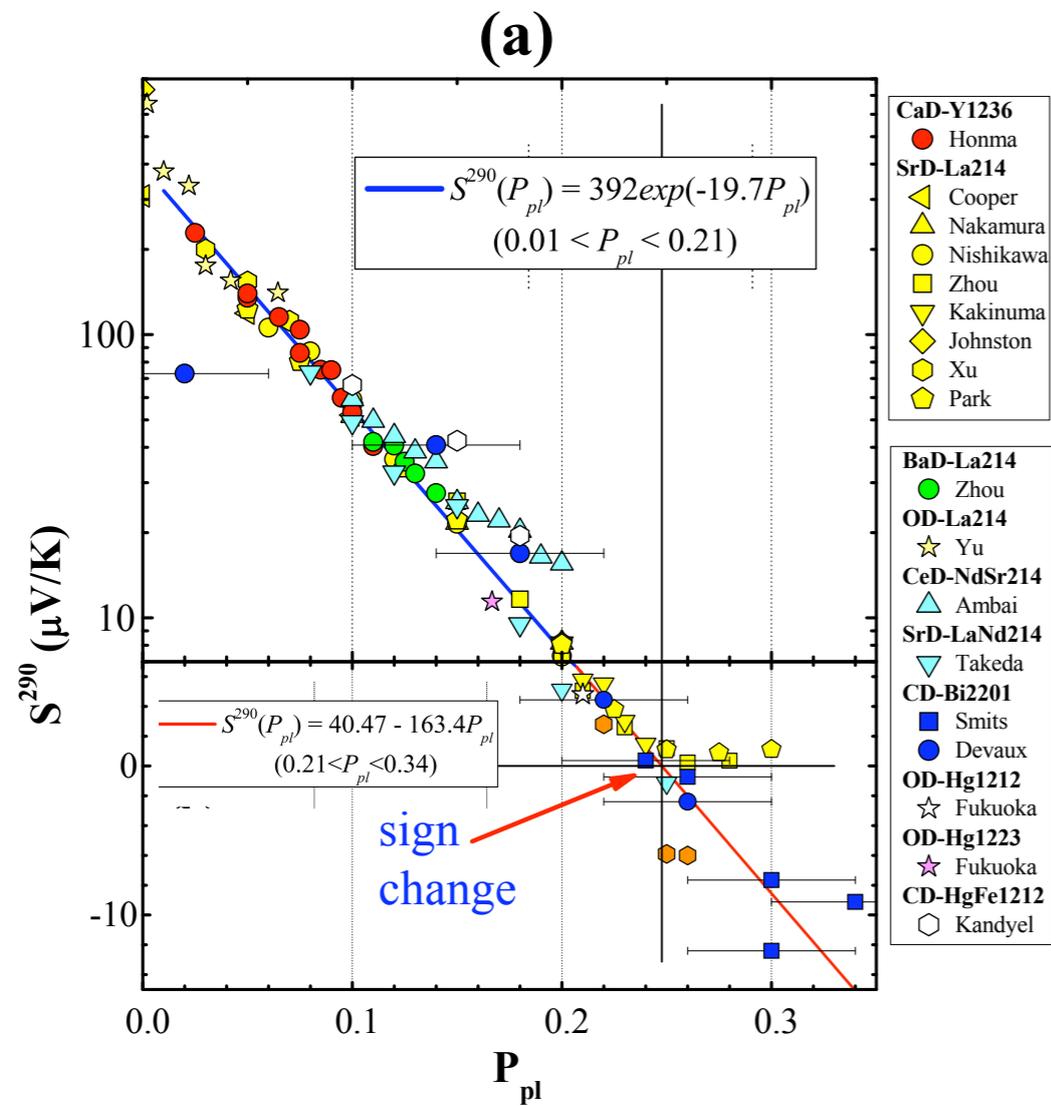
Universal sign change of thermopower



Universal sign change of thermopower

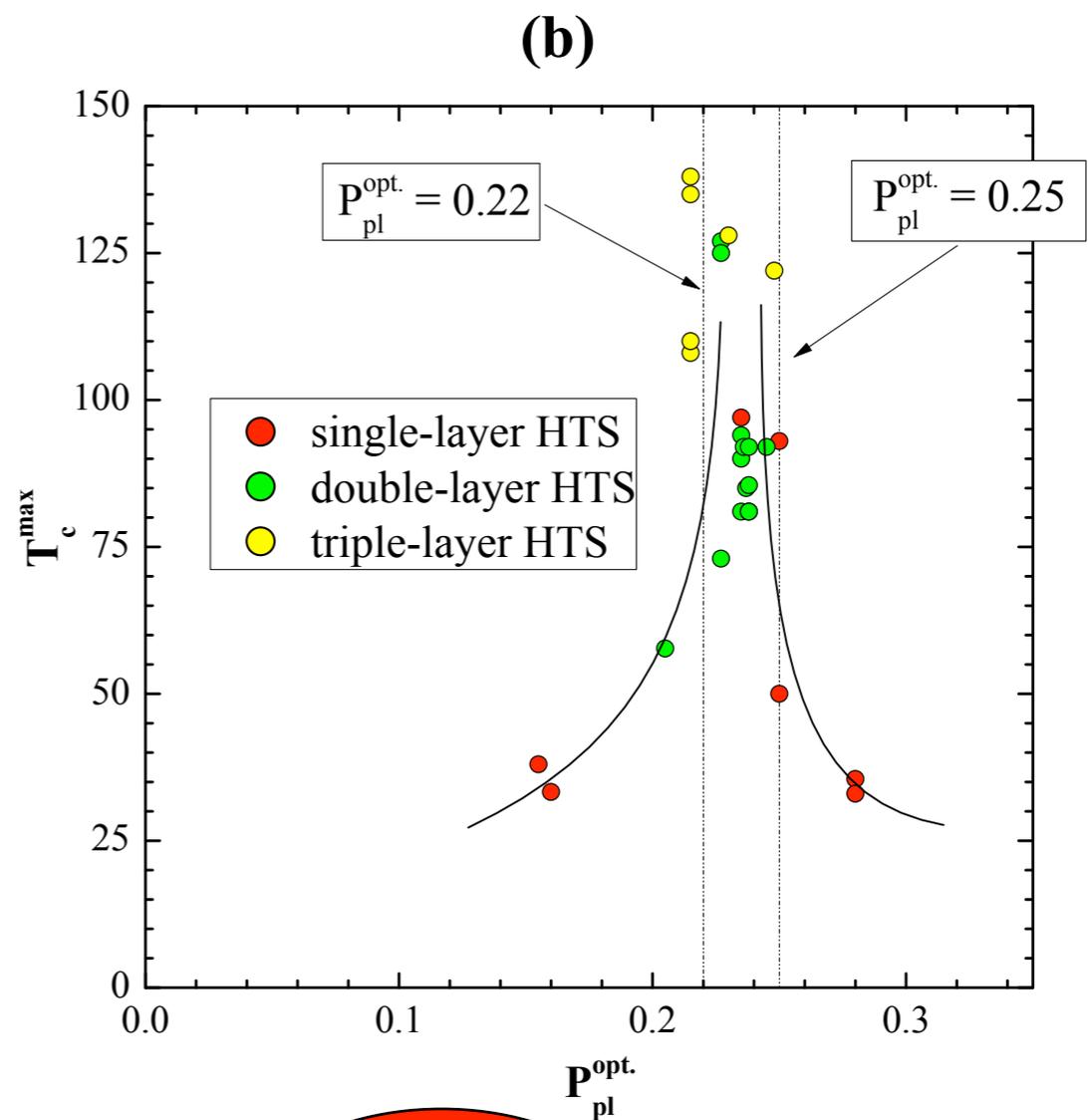
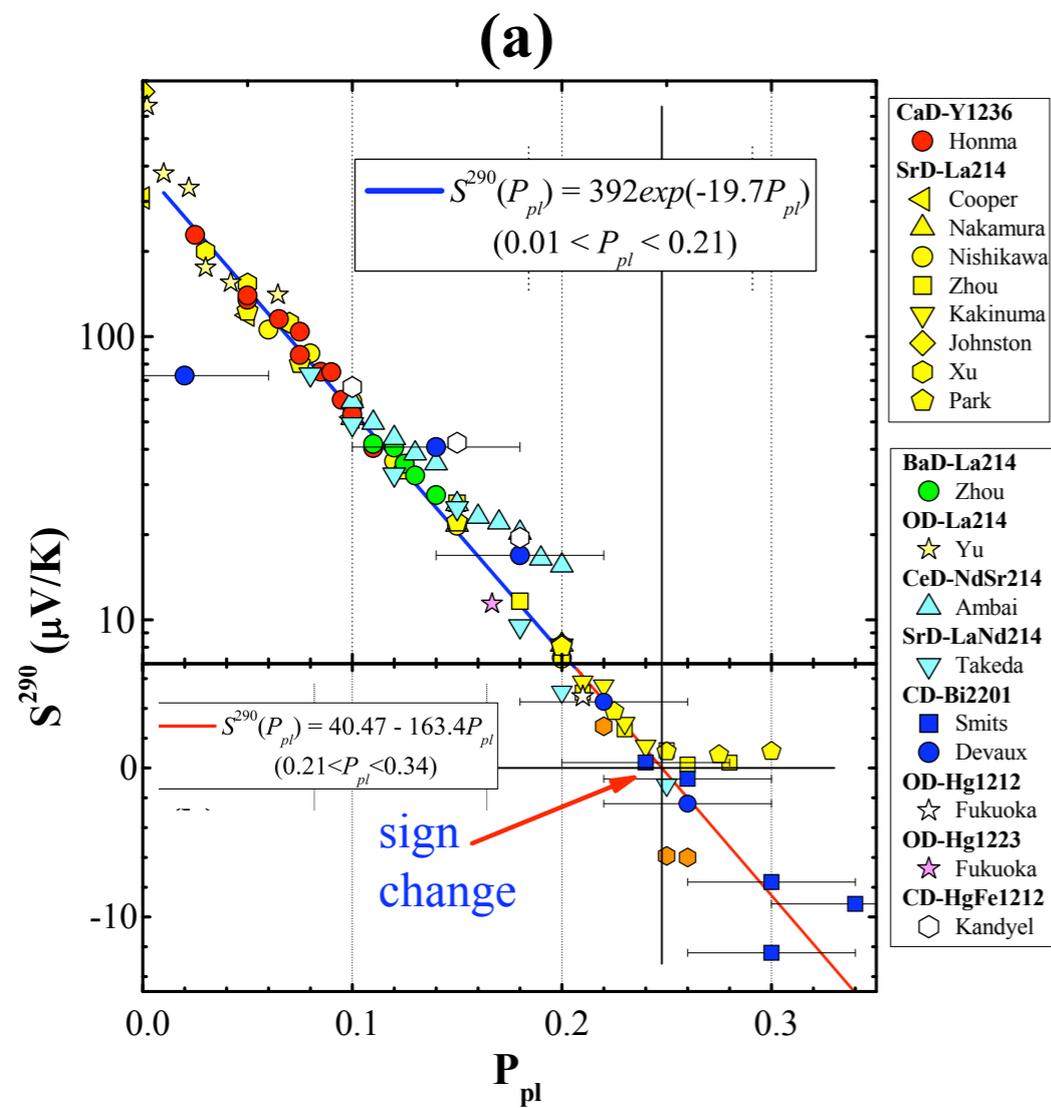


Universal sign change of thermopower



$$1 - \frac{T_c}{T_c^{\text{max}}} = 82.6(x - 0.16)^2.$$

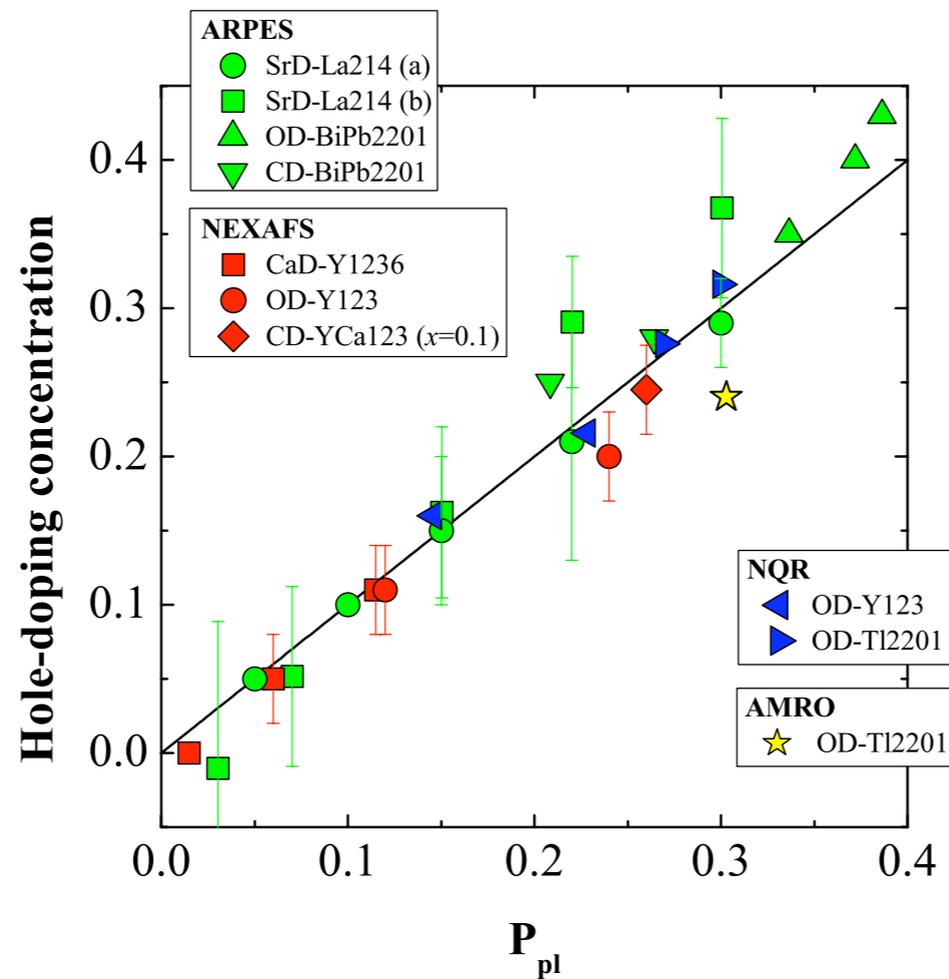
Universal sign change of thermopower



~~$1 - \frac{T_c}{T_{c,\text{max}}} = 2.6(x - 16)^2$~~

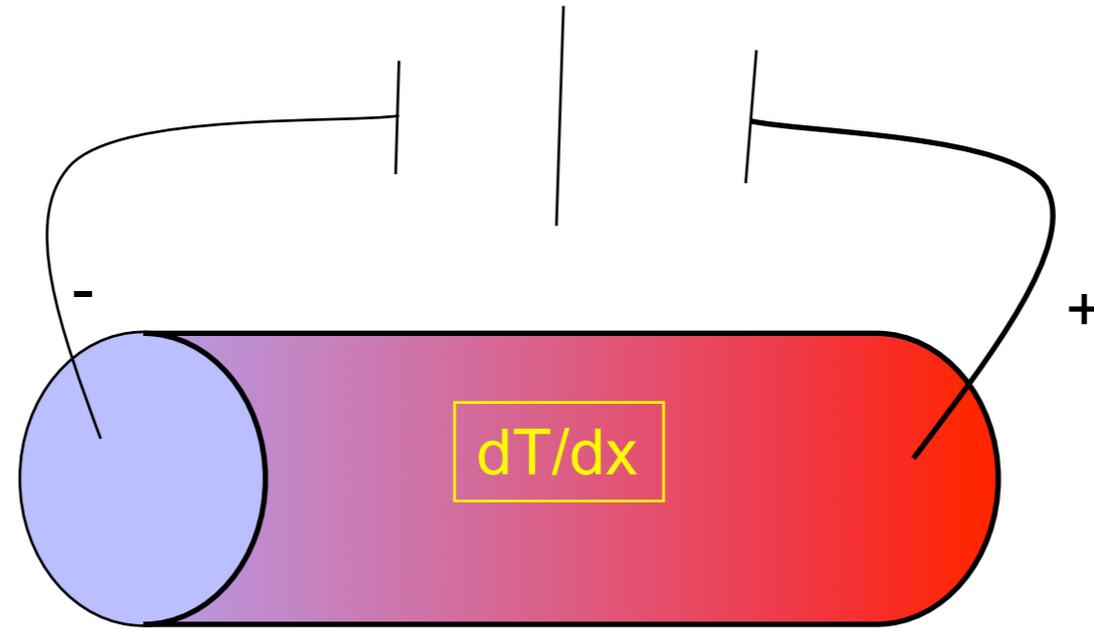
How valid is the thermopower doping scale?

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Why?

Mottness



$$S = V / \Delta T$$

entropy per carrier

particle-number conservation

Thermopower Primer

$$S = -\frac{k_B}{e} \beta \frac{L_{12}}{L_{11}}$$

$$L_{ij} = \int_{-\infty}^{\infty} d\omega \left(-\frac{\partial f(\omega)}{\partial \omega} \right) \tau^i(\omega) \omega^{j-1}$$

$$\tau(\omega) = \frac{1}{N} \sum_{\mathbf{k}, \sigma} \left(\frac{\partial \epsilon_{\mathbf{k}}}{\partial k_x} \right)^2 A^2(\mathbf{k}, \omega)$$

spectral
function

1.) \mathcal{T} must be symmetric about the chemical potential for $S=0$

2.) but if A is momentum-independent, $S=0$ by particle-hole symmetry

G. Beni, Phys. Rev. B vol. 10, 2186
(1973).



Exact calculation
of S for atomic ($t=0$)
limit of Hubbard model

$$S = -\frac{k_B}{e} \ln \frac{2x}{1-x}$$

G. Beni, Phys. Rev. B vol. 10, 2186
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Exact calculation
of S for atomic ($t=0$)
limit of Hubbard model



band insulator
(free electrons)

$$S = -\frac{k_B}{e} \ln \frac{2x}{1-x}$$

$$\ln \frac{x}{2-x}$$

vanishes at
half-filling

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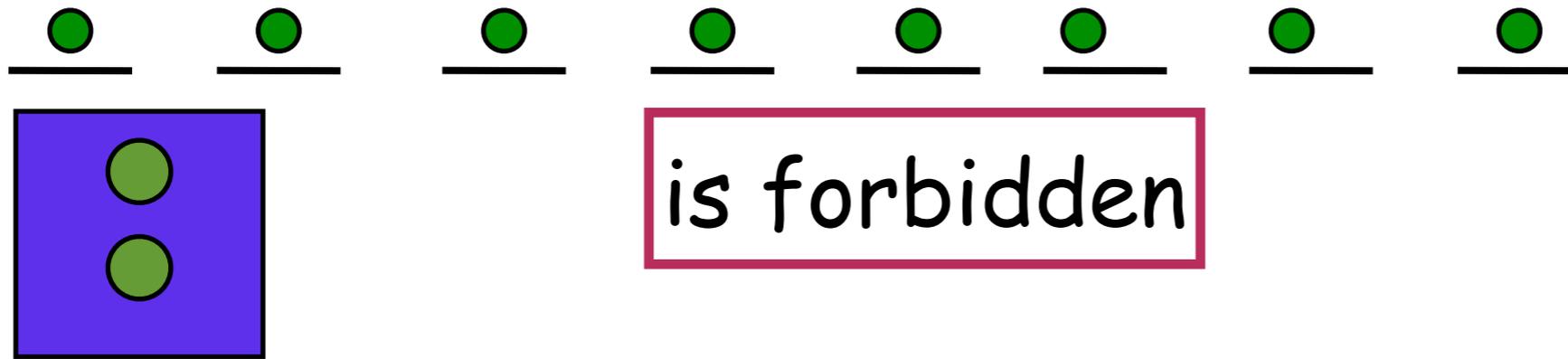


$S=0$ when $x=1/3$; WHY?

What is so
special about
 $2x$ and $1-x$?

Why is the atomic limit
of the Hubbard model
p-h symmetric at $x=1/3$?

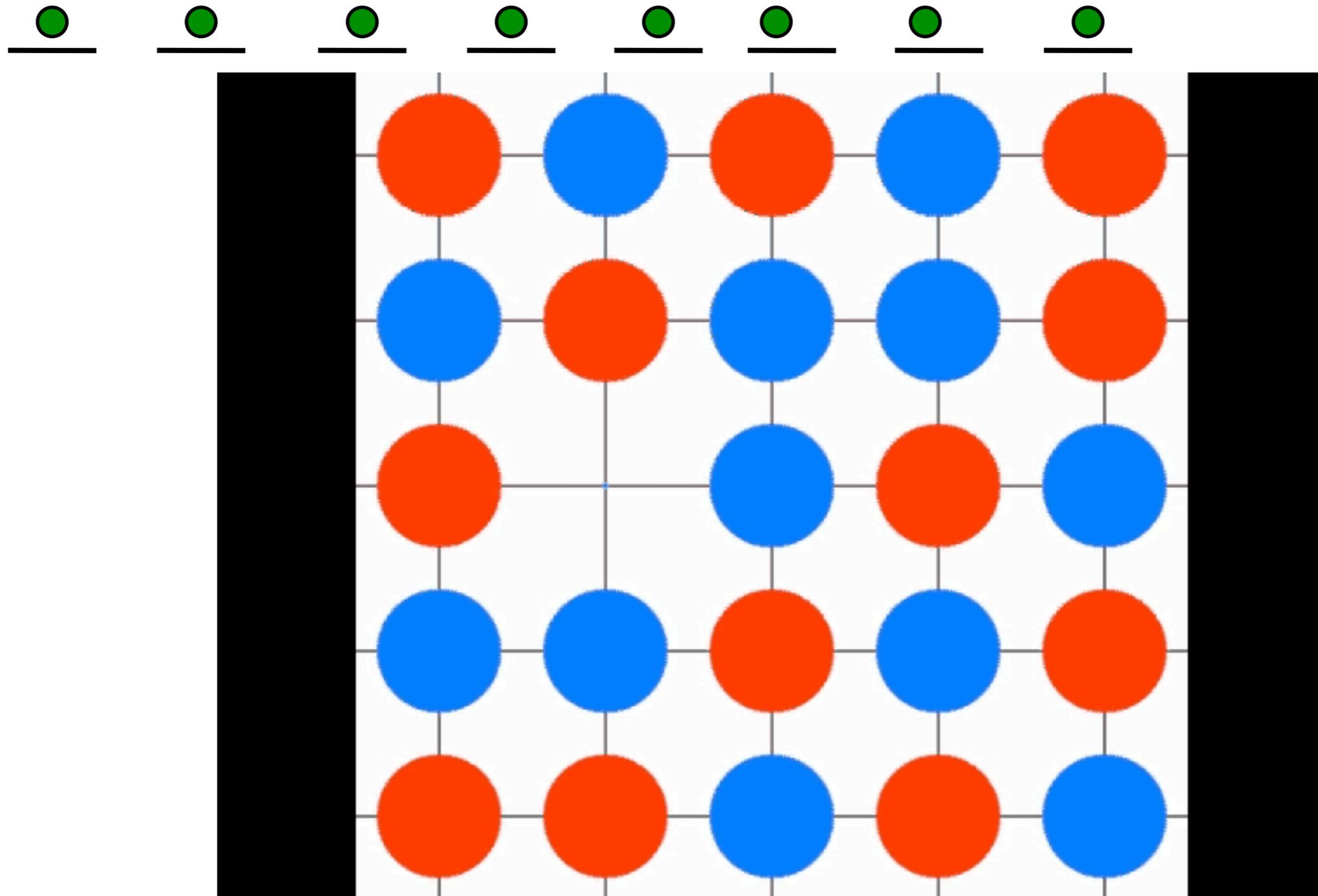
classical Mottness



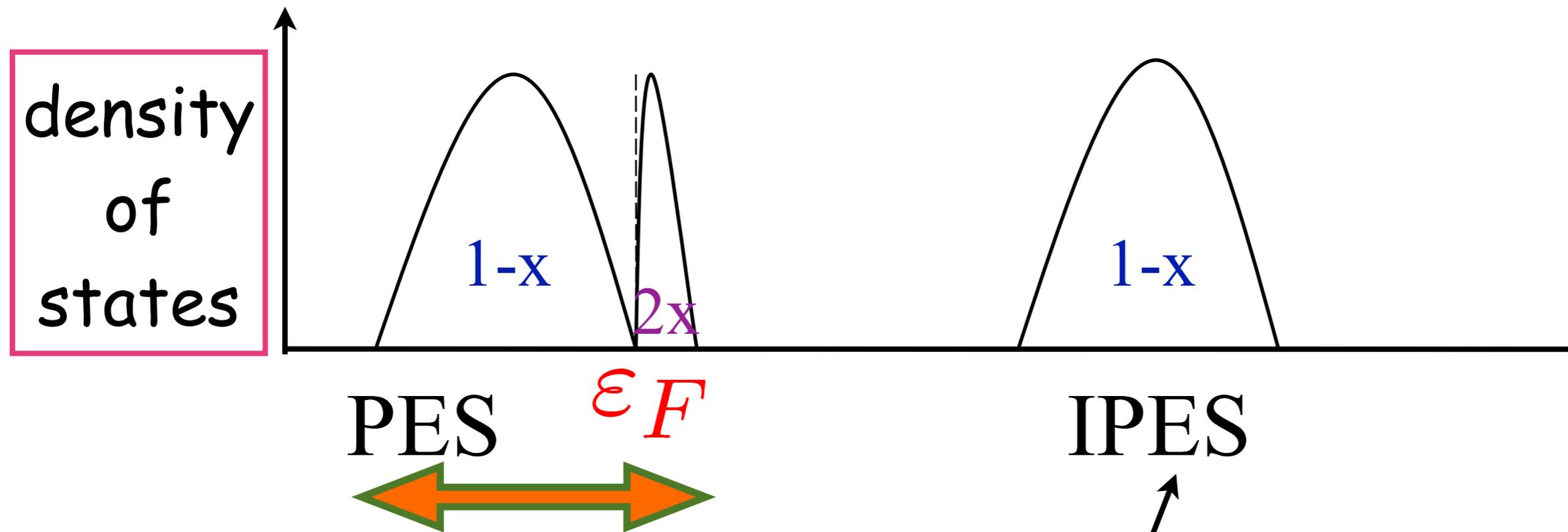
classical Motttness



classical Motttness



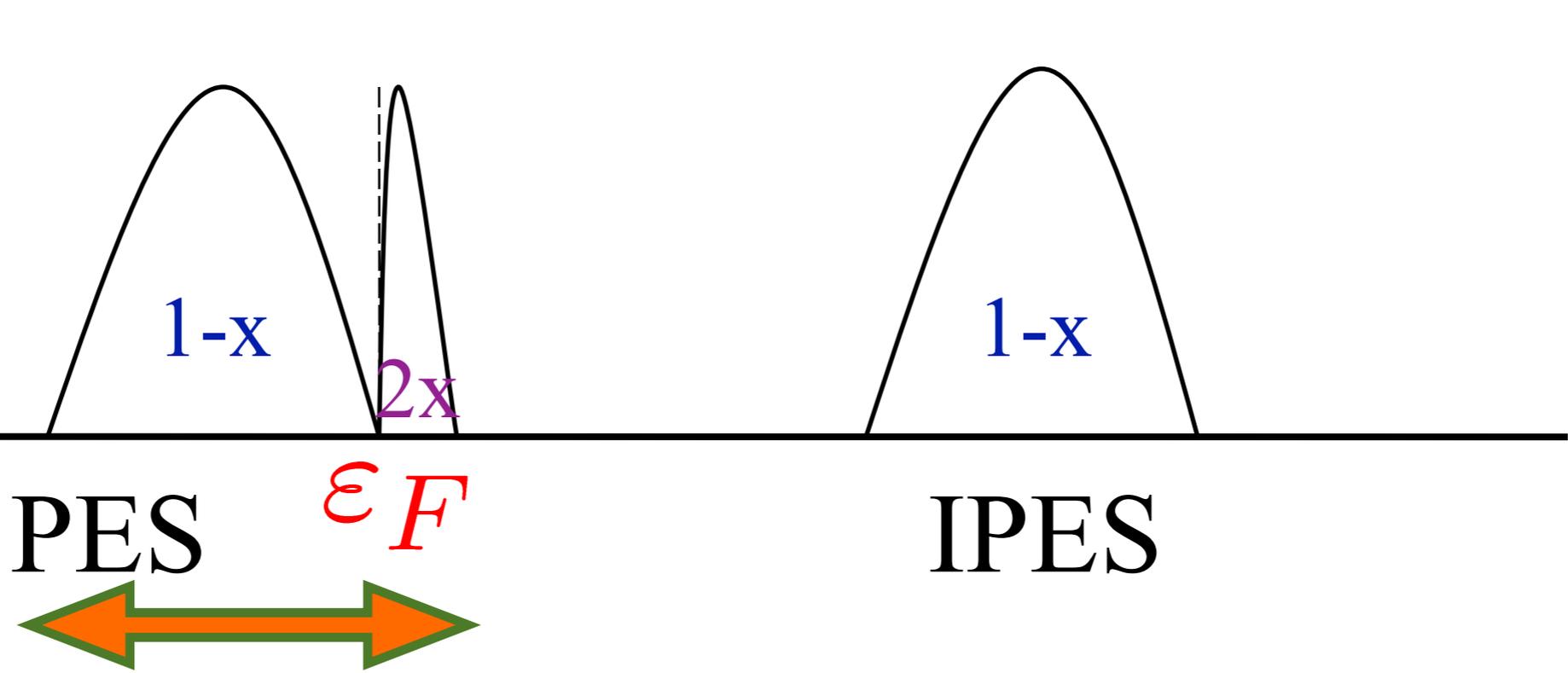
atomic limit: x holes



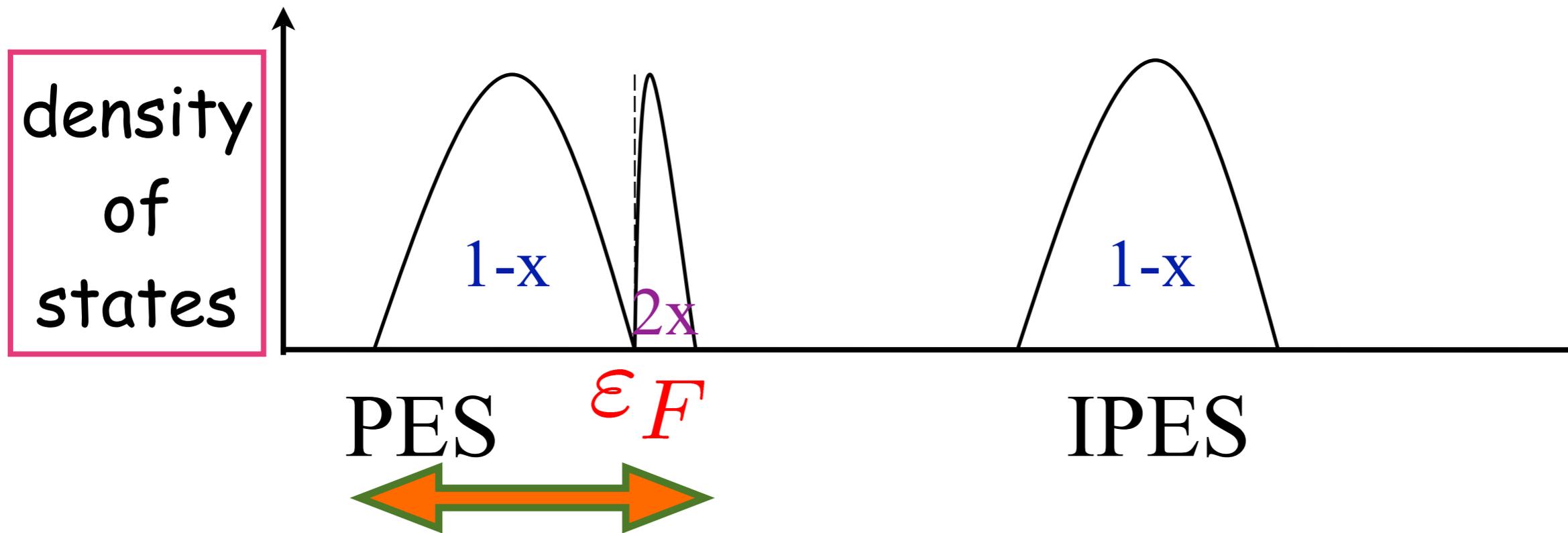
$$G_{\sigma}(\omega, k) = \frac{\frac{1}{2}(1+x)}{\omega - \mu + \frac{U}{2}} + \frac{\frac{1}{2}(1-x)}{\omega - \mu - \frac{U}{2}}$$

atomic limit: x holes

density of states



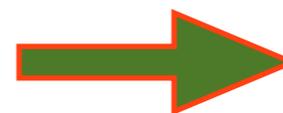
atomic limit: x holes



criterion for vanishing of thermopower

LESW above ϵ_F = LESW below ϵ_F

$$2x = 1 - x$$



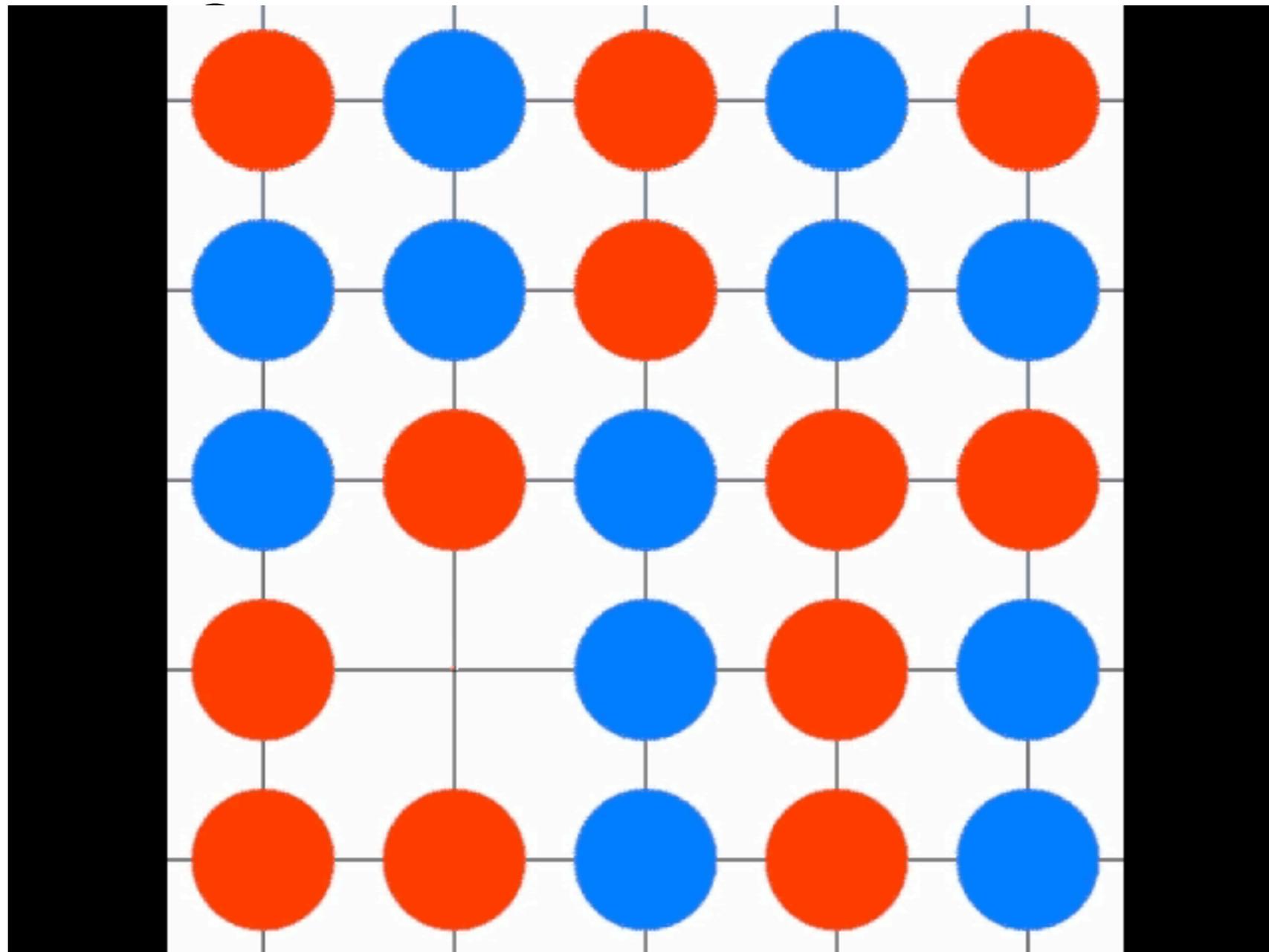
$$x = 1/3!$$

sign change occurs for $x < 1/3$

Why?

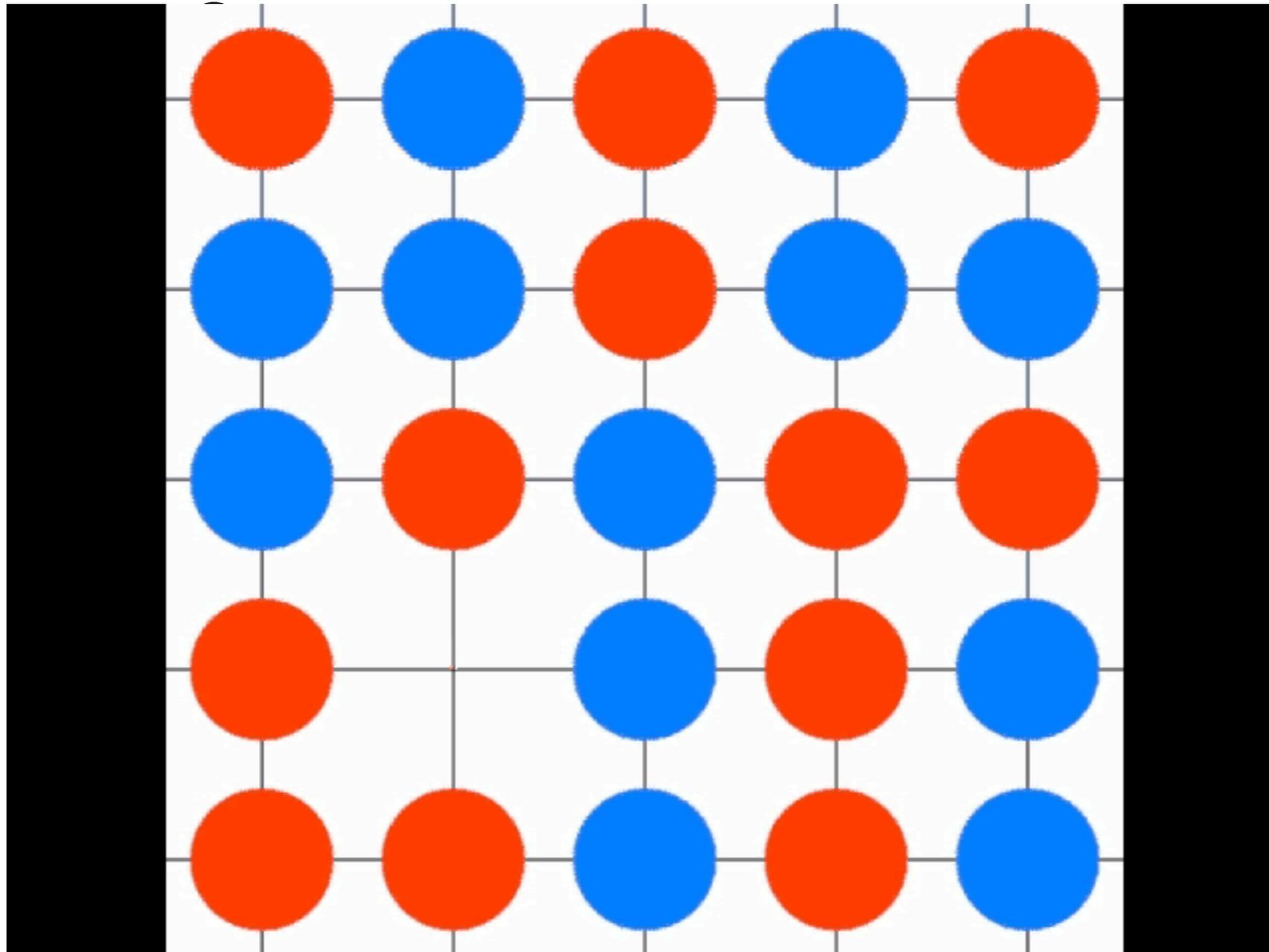
quantum Mottness: U finite

$$U \gg t$$



quantum Mottness: U finite

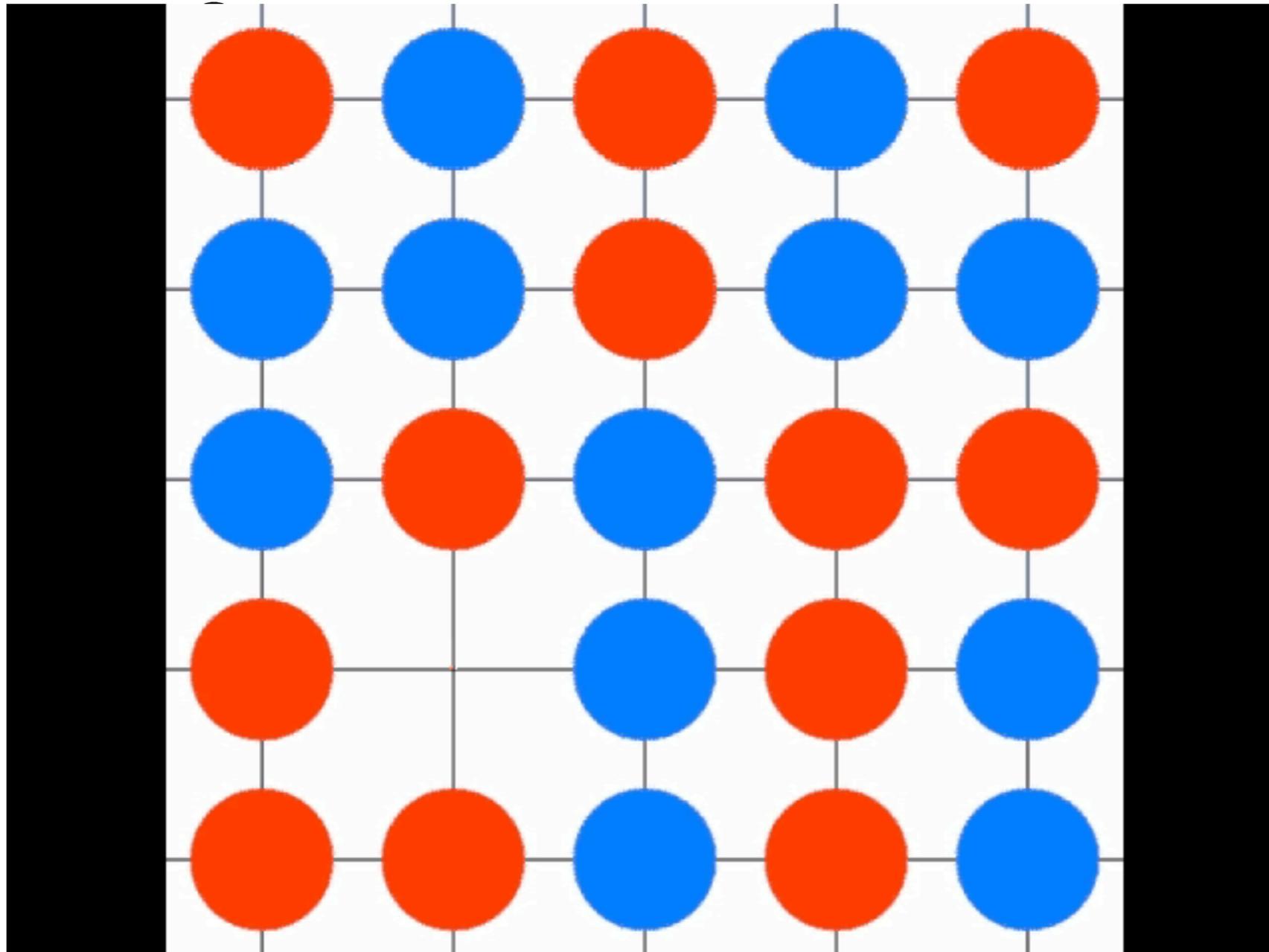
$$U \gg t$$



double occupancy in ground state!!

quantum Mottness: U finite

$$U \gg t$$



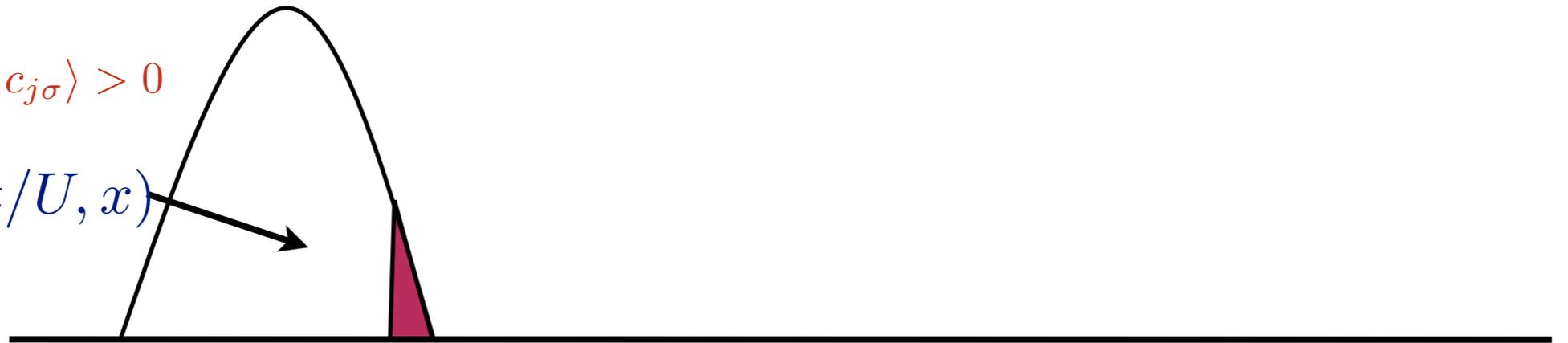
double occupancy in ground state!!

$$W_{\text{PES}} > 1 + x$$

Harris & Lange, 1967

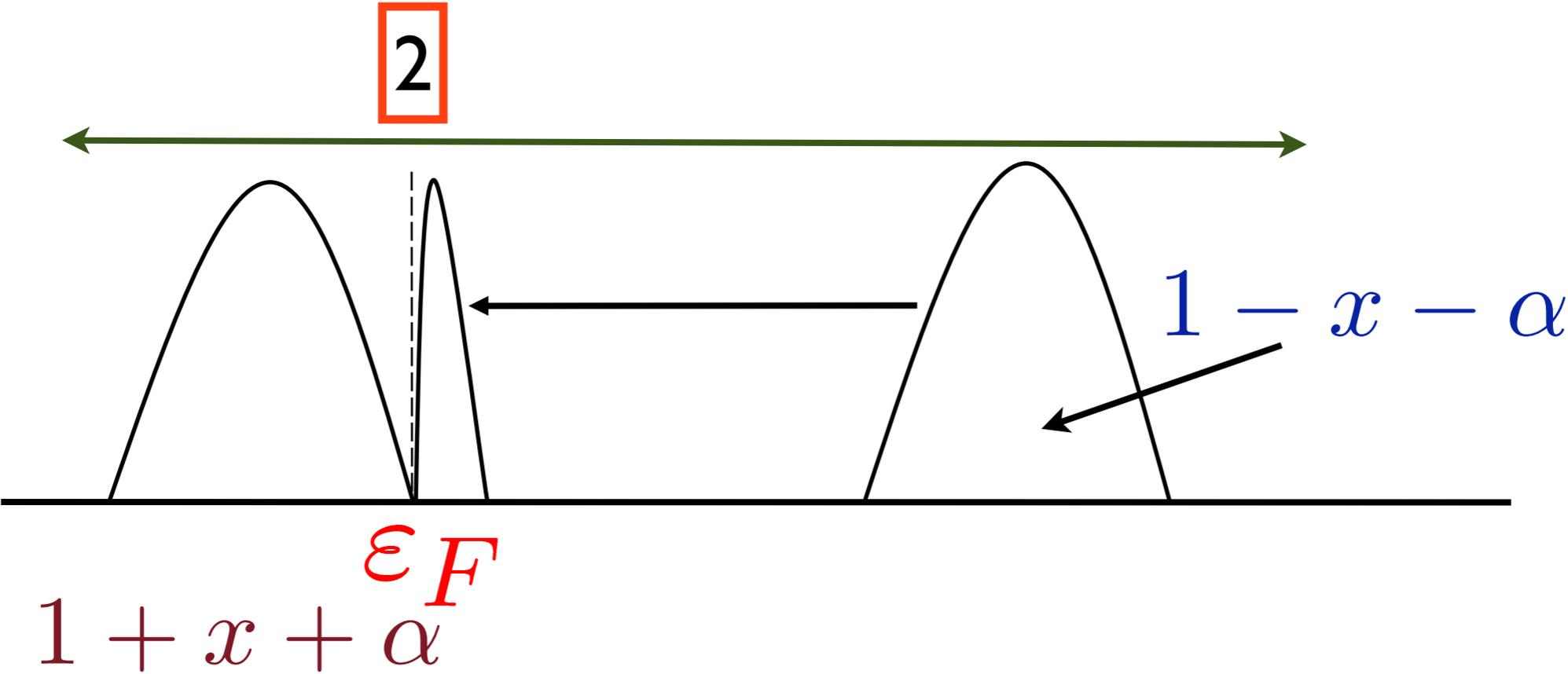
$$\alpha = \frac{t}{U} \sum_{ij} \langle c_{i\sigma}^\dagger c_{j\sigma} \rangle > 0$$

$$1 + x + \alpha(t/U, x)$$



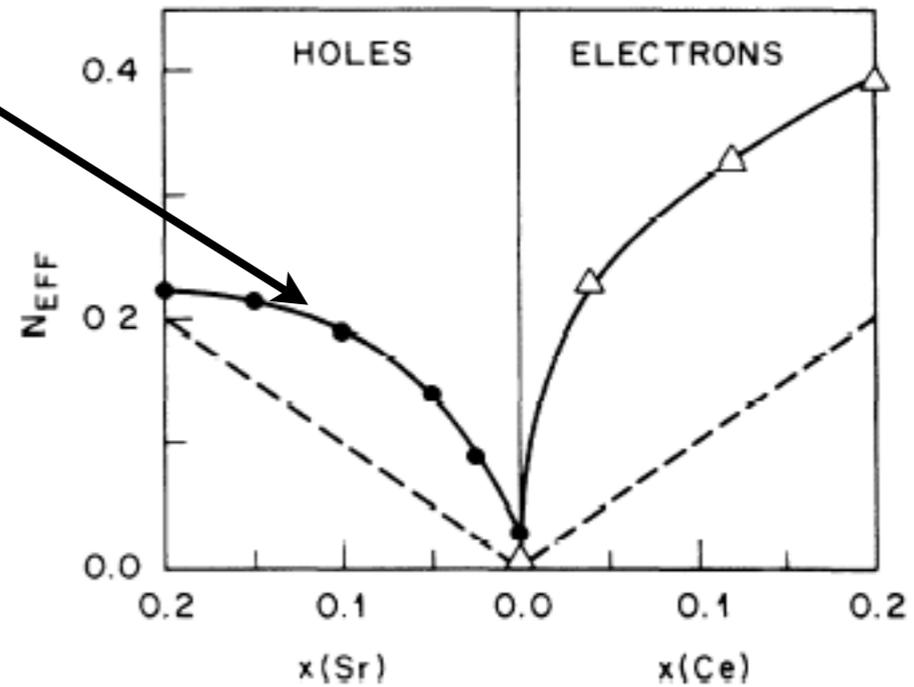
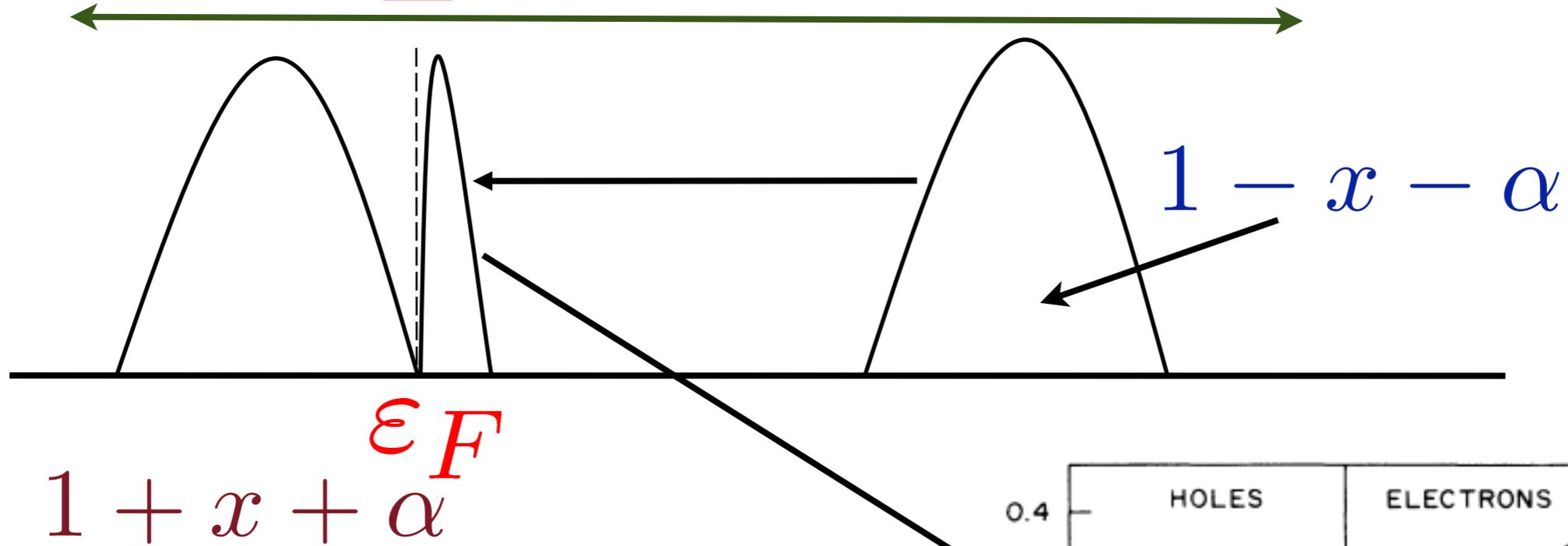
What is the new
symmetry condition
for the LHB ?

re-establish static band picture



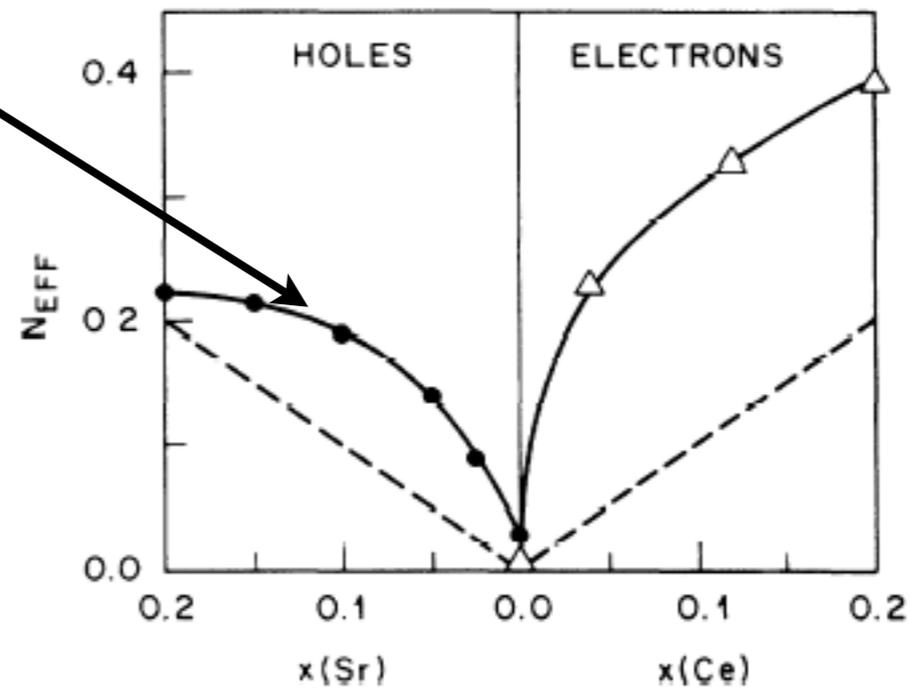
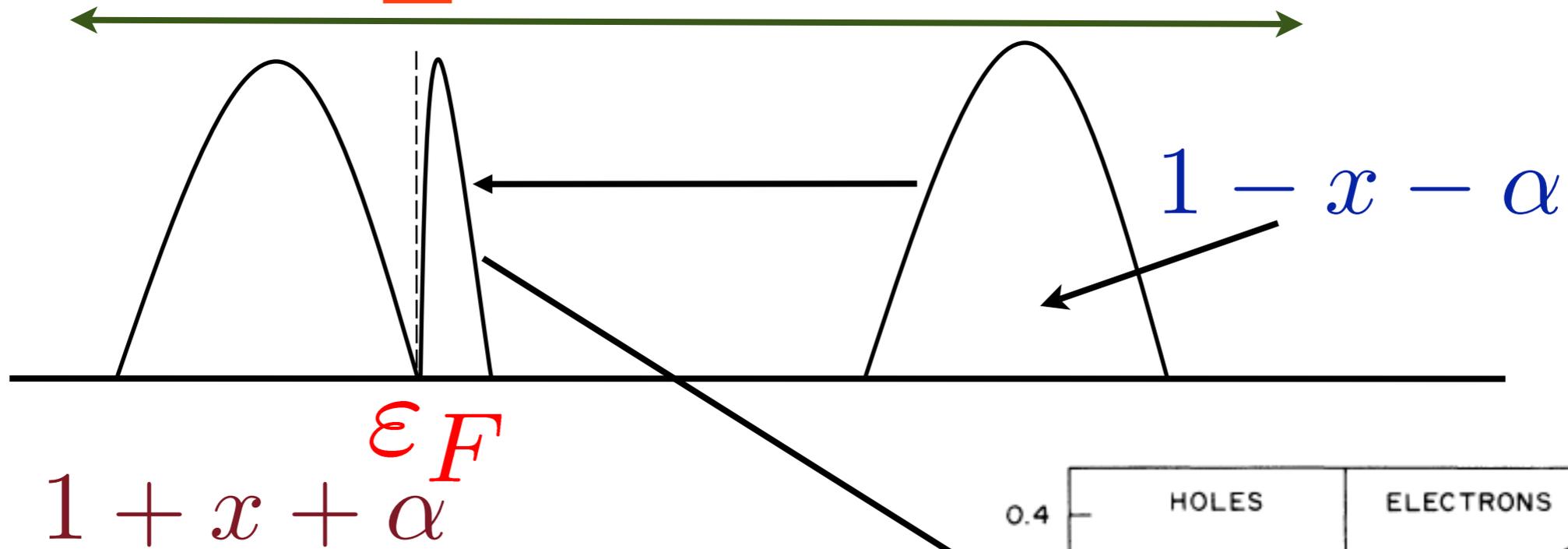
re-establish static band picture

2



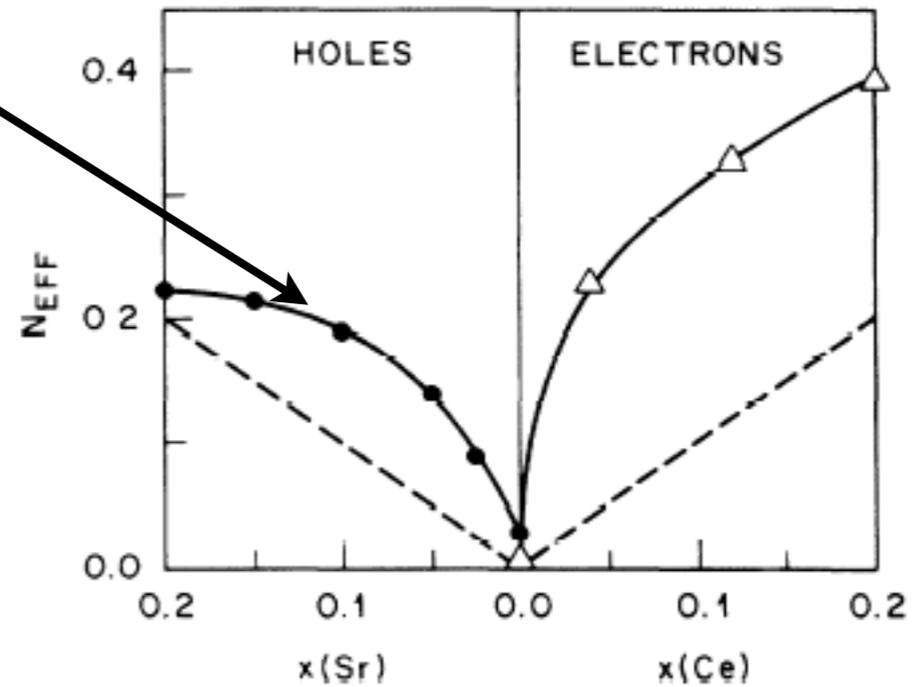
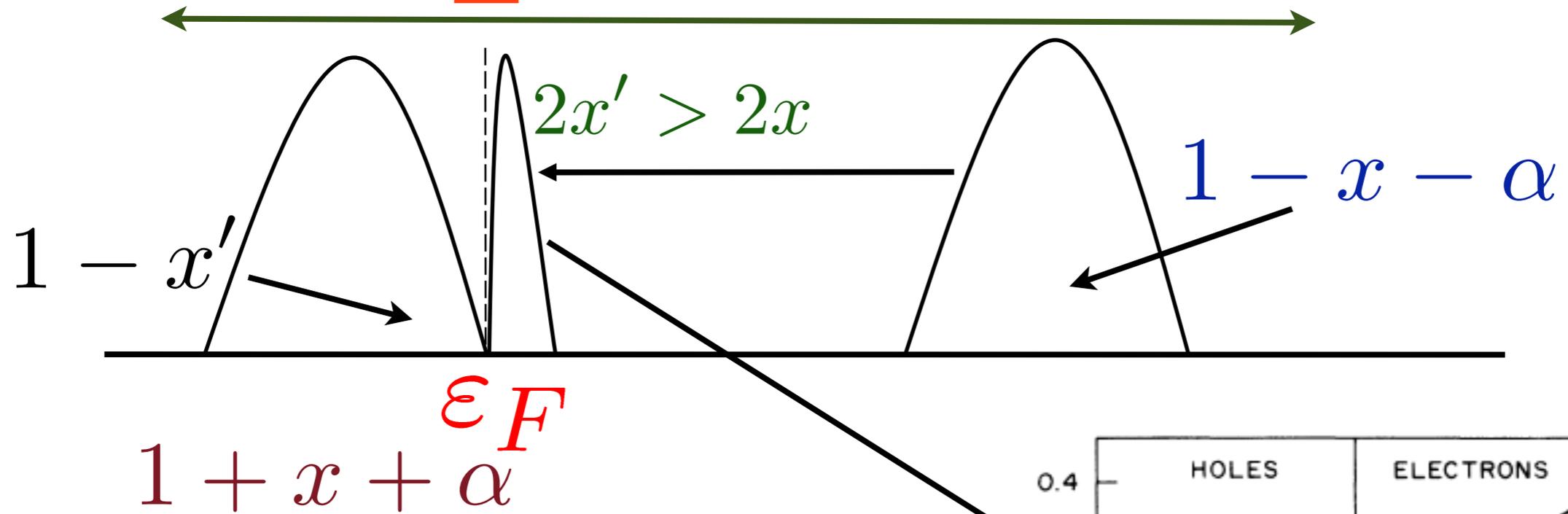
re-establish static band picture

2 re-definition: $x' = x + \alpha$



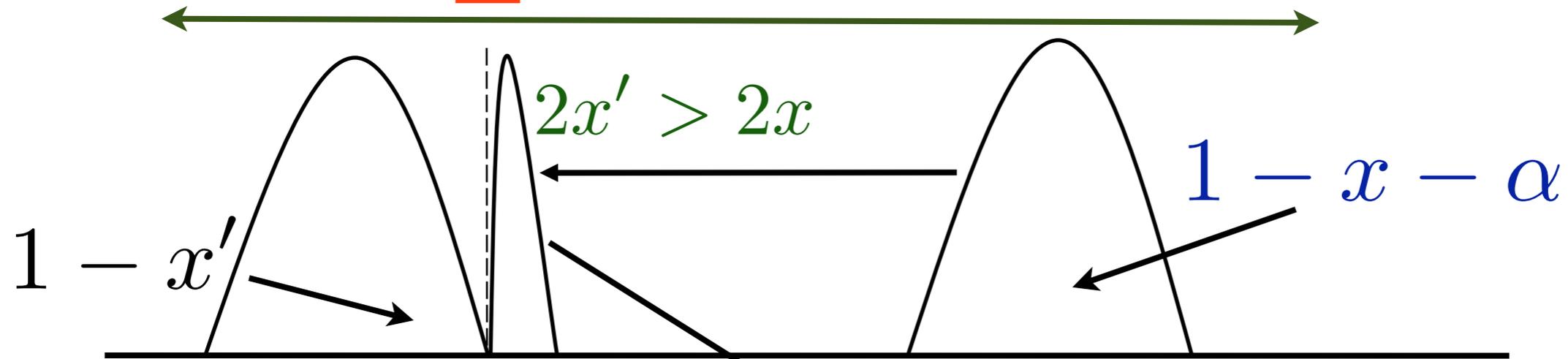
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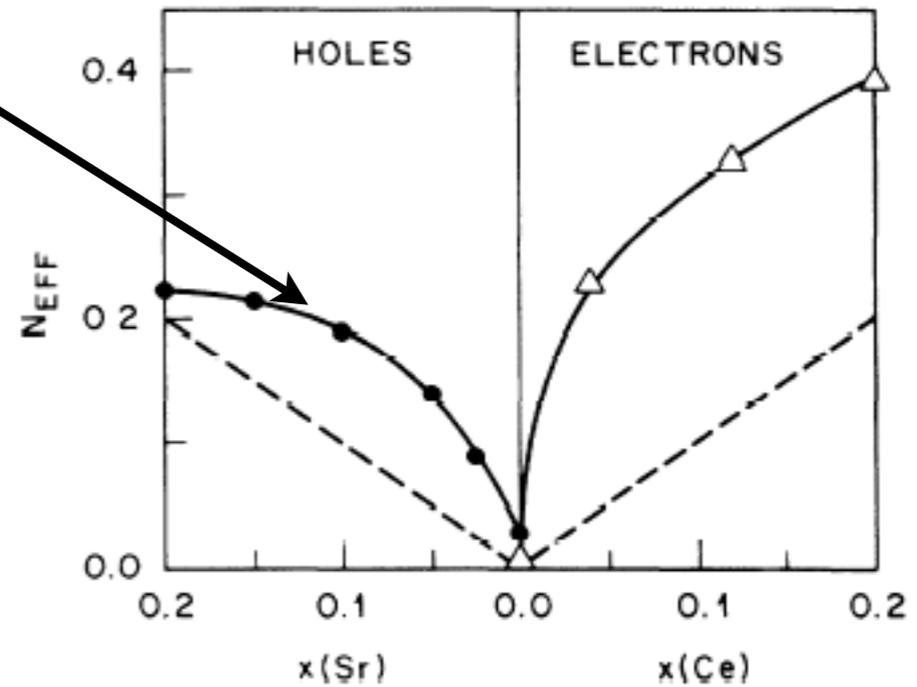
2 re-definition: $x' = x + \alpha$



$1 + x + \alpha$

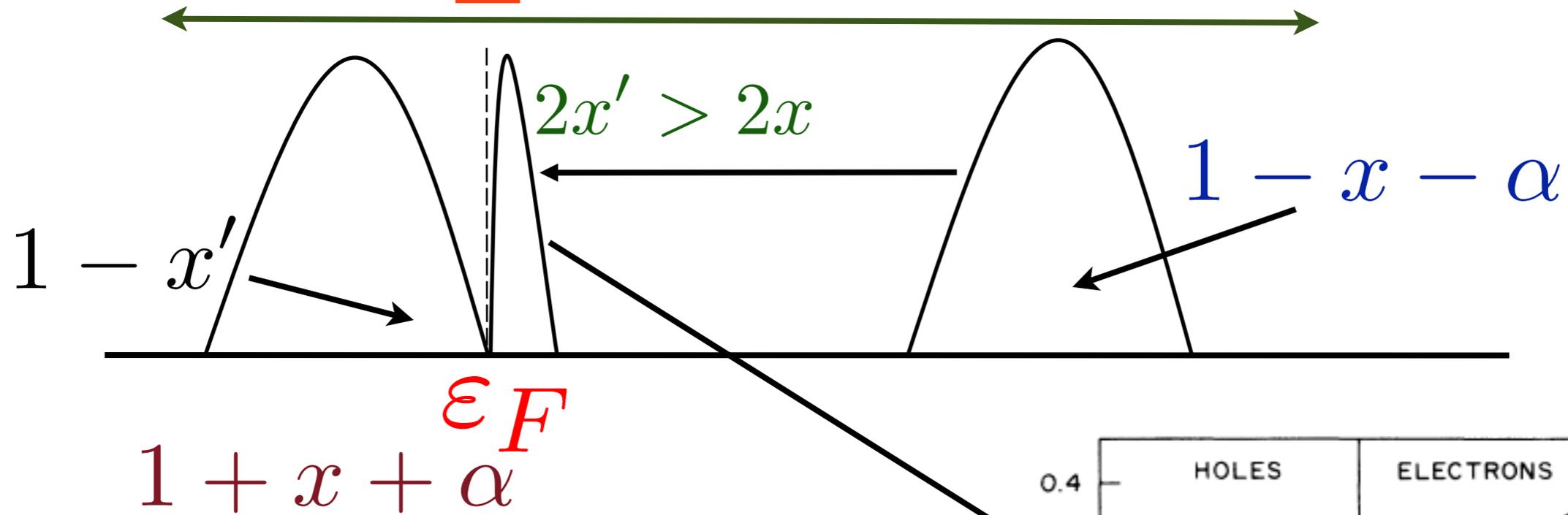
New Symmetry Condition

$2x' = 1 - x'$



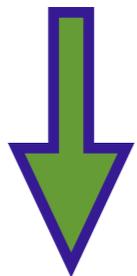
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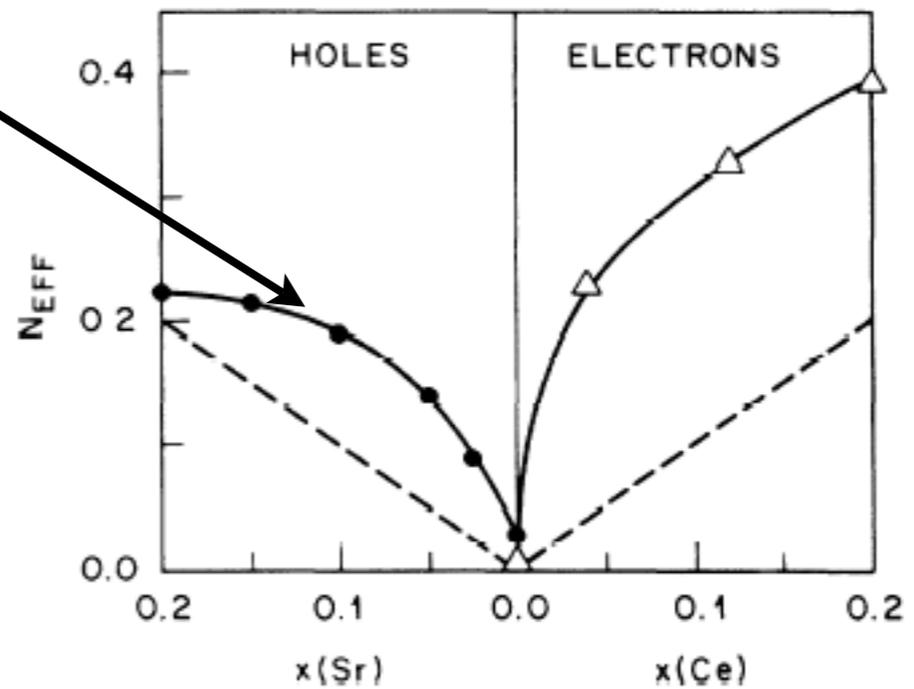


New Symmetry Condition

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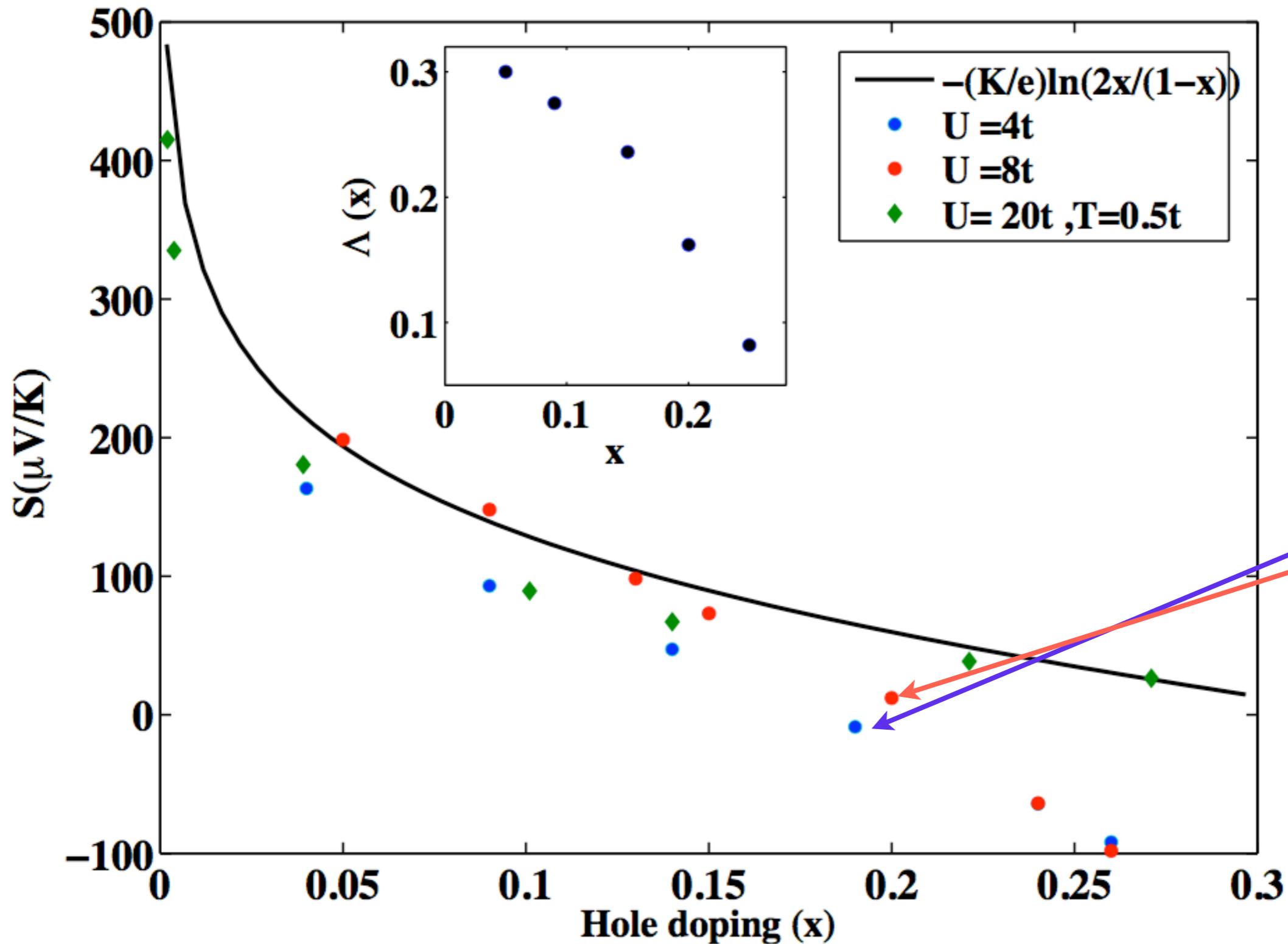


$$x_c = \frac{1}{3} - \alpha < \frac{1}{3}$$



Hubbard Model: CDMFT

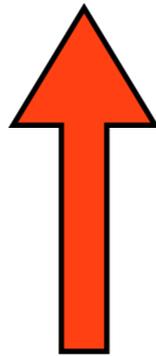
$T = 0.1t, t = 0.5 \text{ eV}$



sign change

Why is T_c so high?

$$2x' = 1 - x'$$



high-low energy mixing

Is our key claim correct?

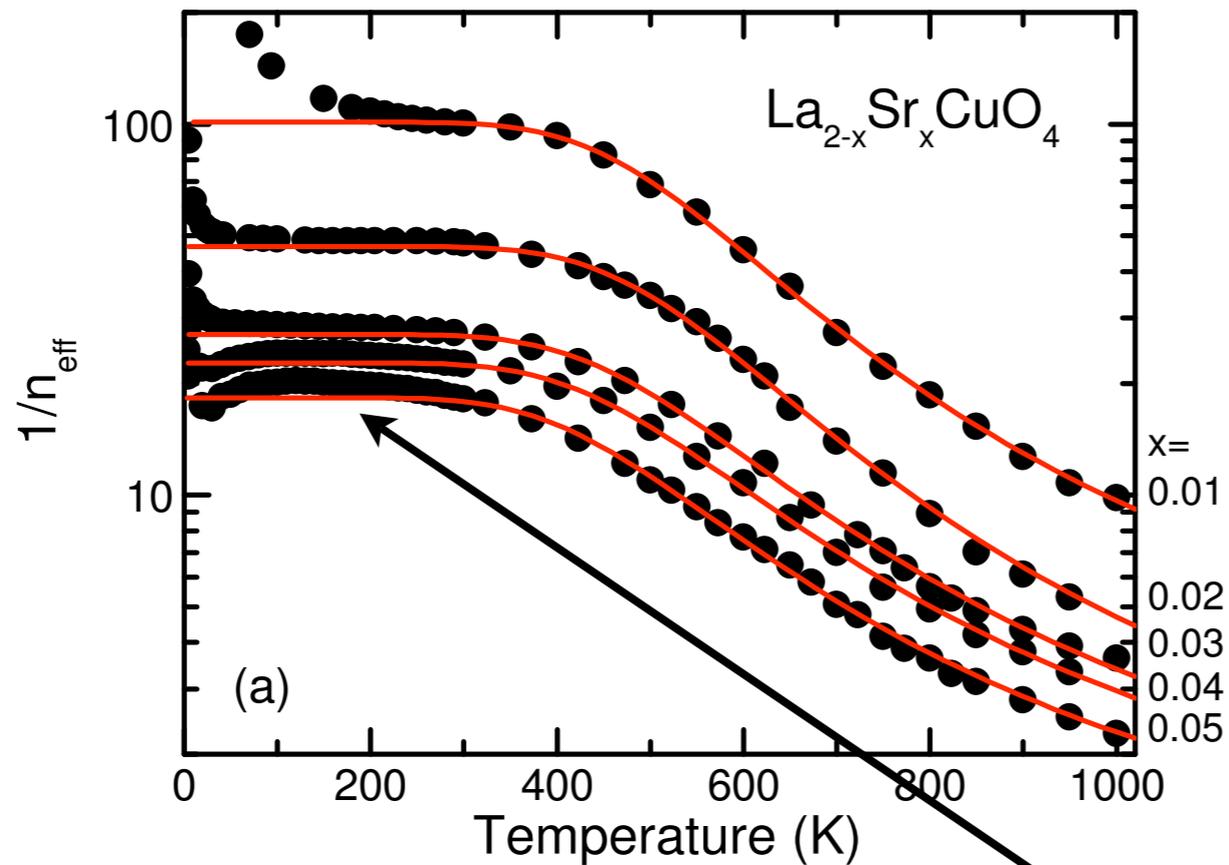
$$x' = x + \alpha$$

Is our key claim correct?

$$x' = x + \alpha$$

Does the electron filling
have a dynamical
component?

direct evidence

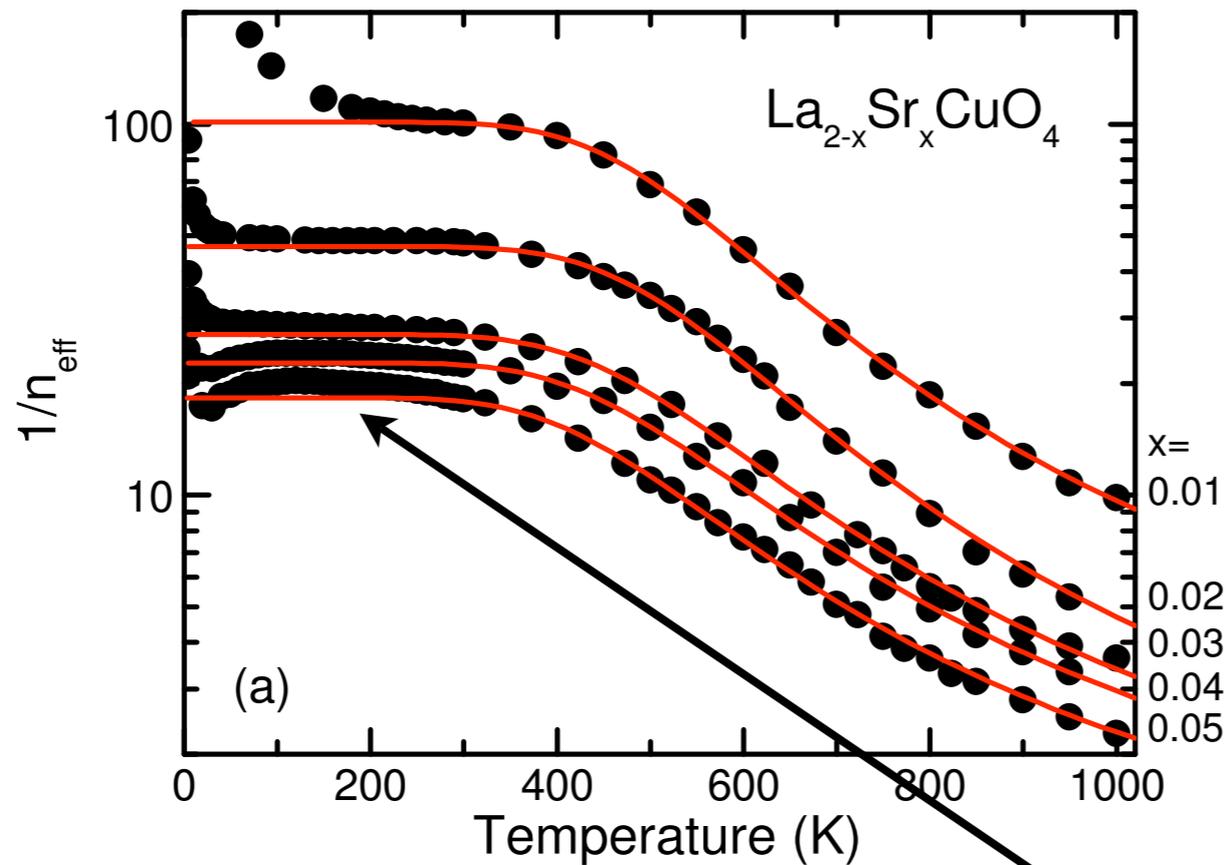


Ono, et al., Phys. Rev. B 75, 024515
(2007)

$$n_{\text{Hall}}(x, T) = n_0(x) + n_1(x) \exp(-\Delta(x)/T), \quad \text{PRL, vol. 97, 247003 (2006).}$$

direct evidence

charge carrier density:

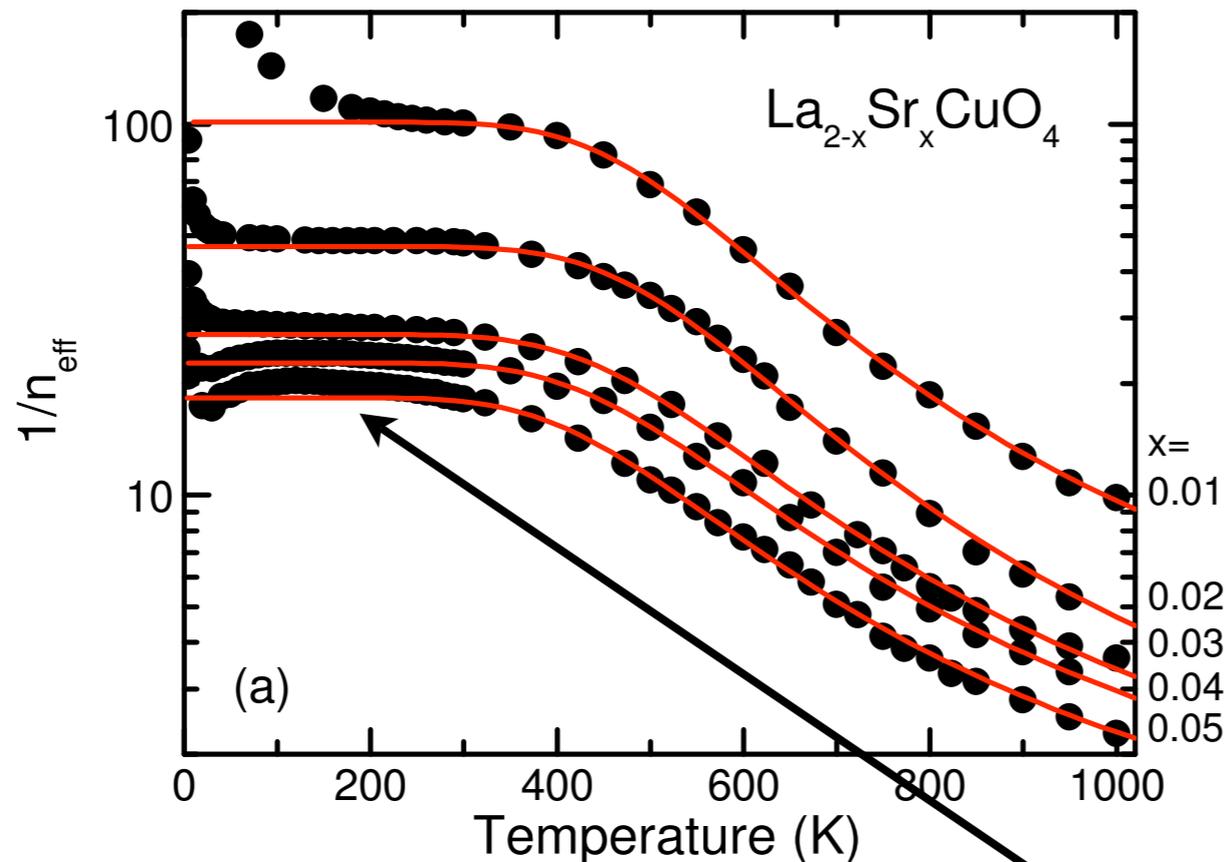


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exponentially suppressed: confinement

$$n_{\text{Hall}}(x, T) = n_0(x) + n_1(x) \exp(-\Delta(x)/T),$$

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gapped excitation

Two-fluid model

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Two-fluid model

$$n_{\text{Hall}}(x, T) = n_0(x) + n_1(x) \exp(-\Delta(x)/T),$$

How?



$$x' = x + \alpha$$

gapped excitation

Effective Theories:

$S(\phi)$ at half-filling

Integrate
Out high
Energy fields

$$\phi = \phi_L + \phi_H$$

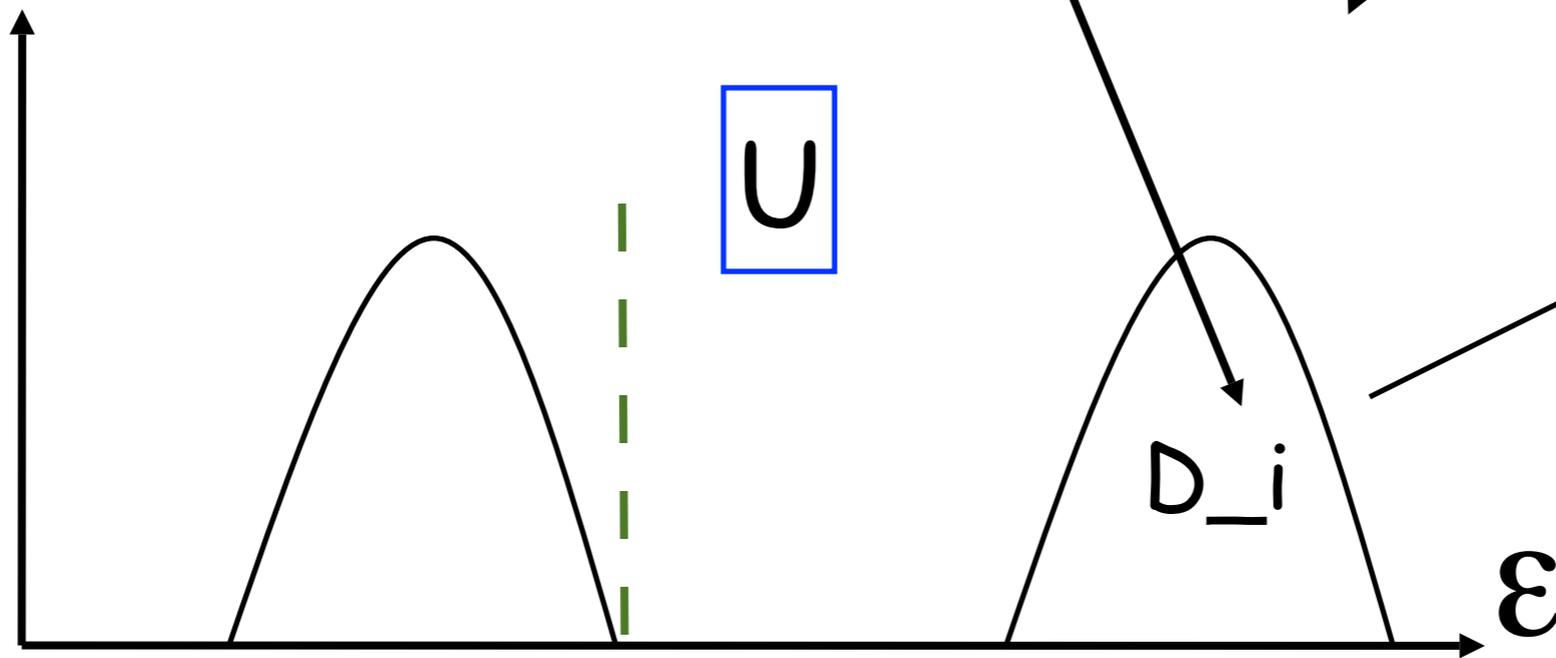
$$e^{-S_{\text{eff}}[\phi_L]} = \int d\phi_H \exp -S(\phi_L, \phi_H)$$

Low-energy theory of M I

Extend the Hilbert space:
Associate with U-scale a new
Fermionic oscillator

charge $2e$ boson

$N(\omega)$



$$U D_i^\dagger D_i$$

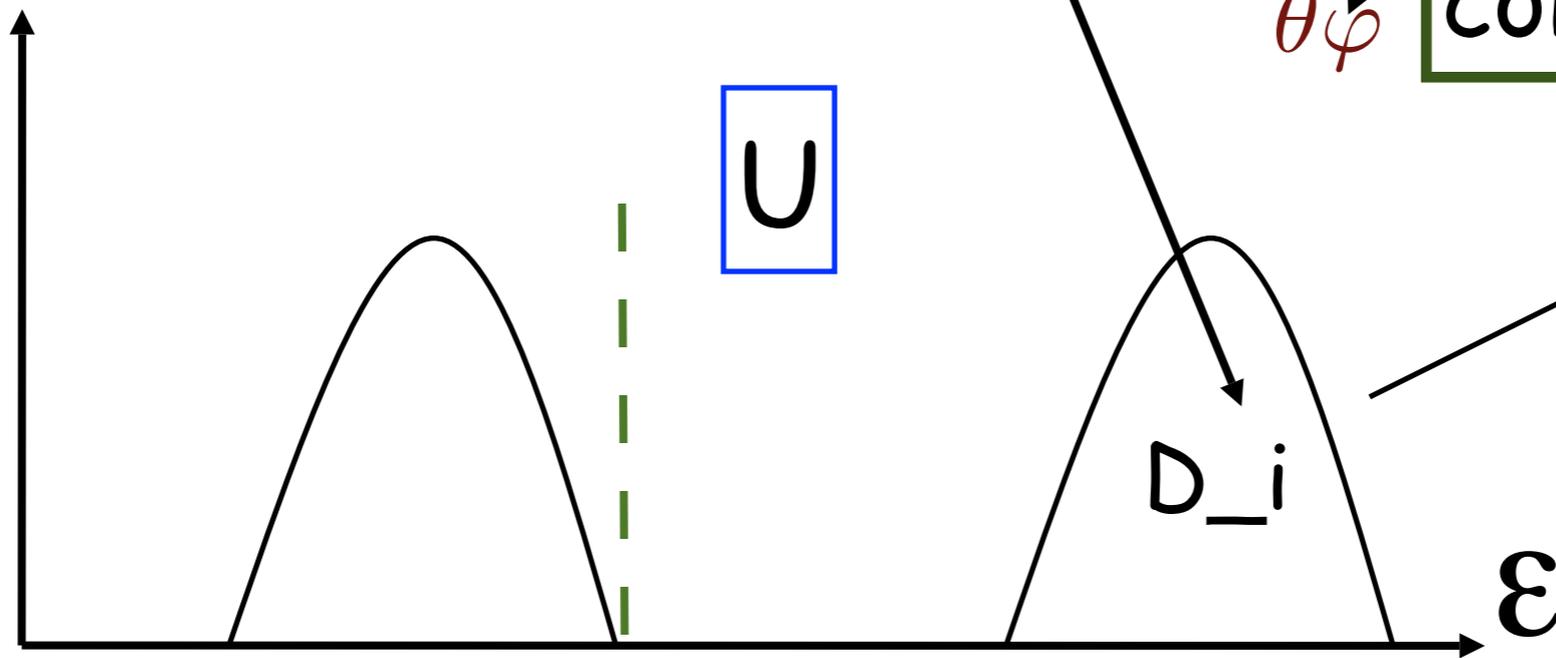
Extend the Hilbert space:
Associate with U-scale a new
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$\bar{\theta}\varphi$

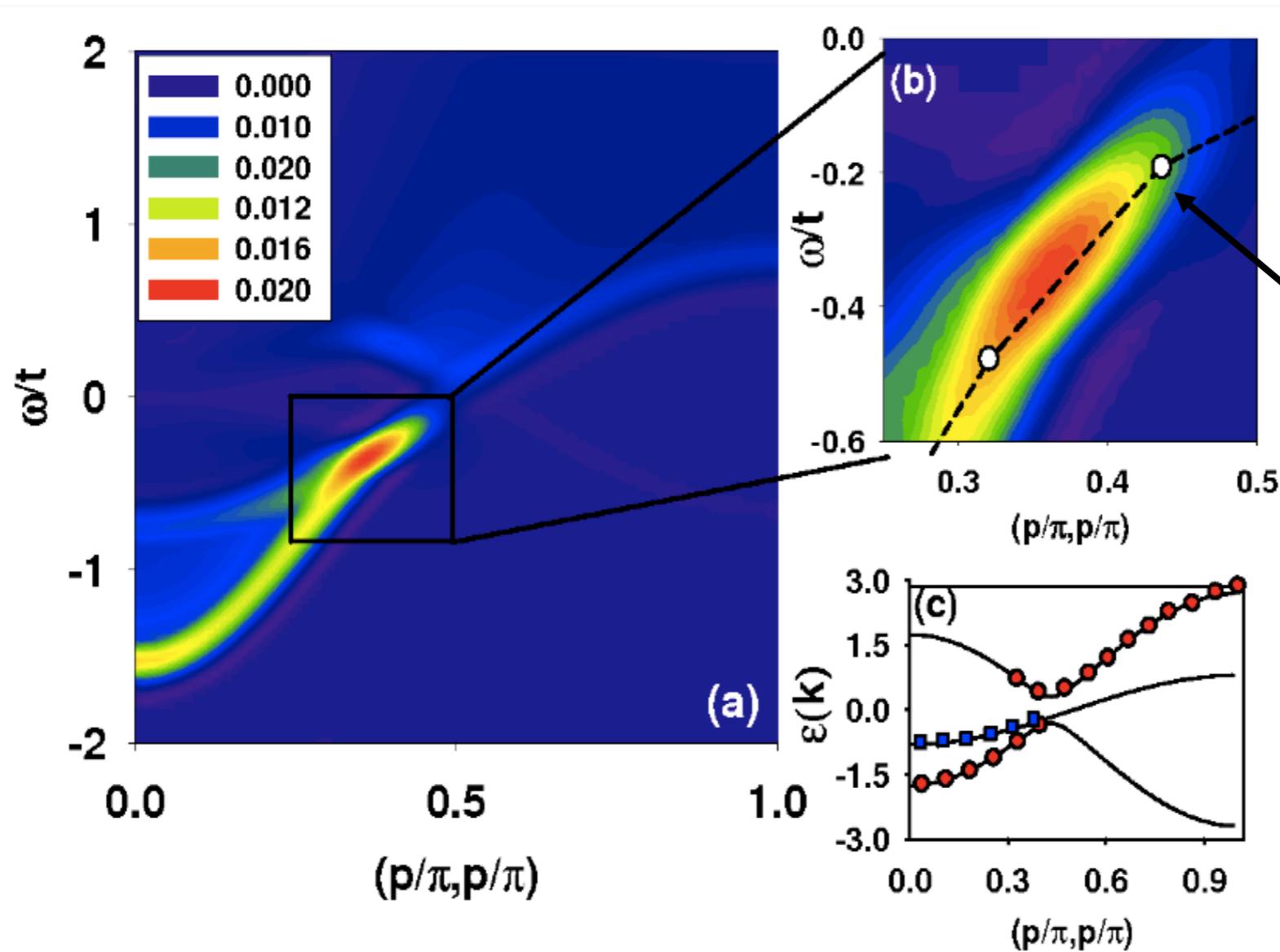
constraint field

$N(\omega)$



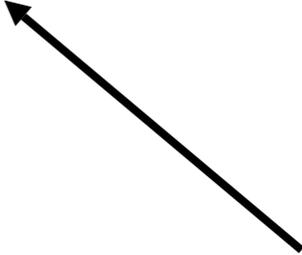
$$U D_i^\dagger D_i$$

Electron spectral function

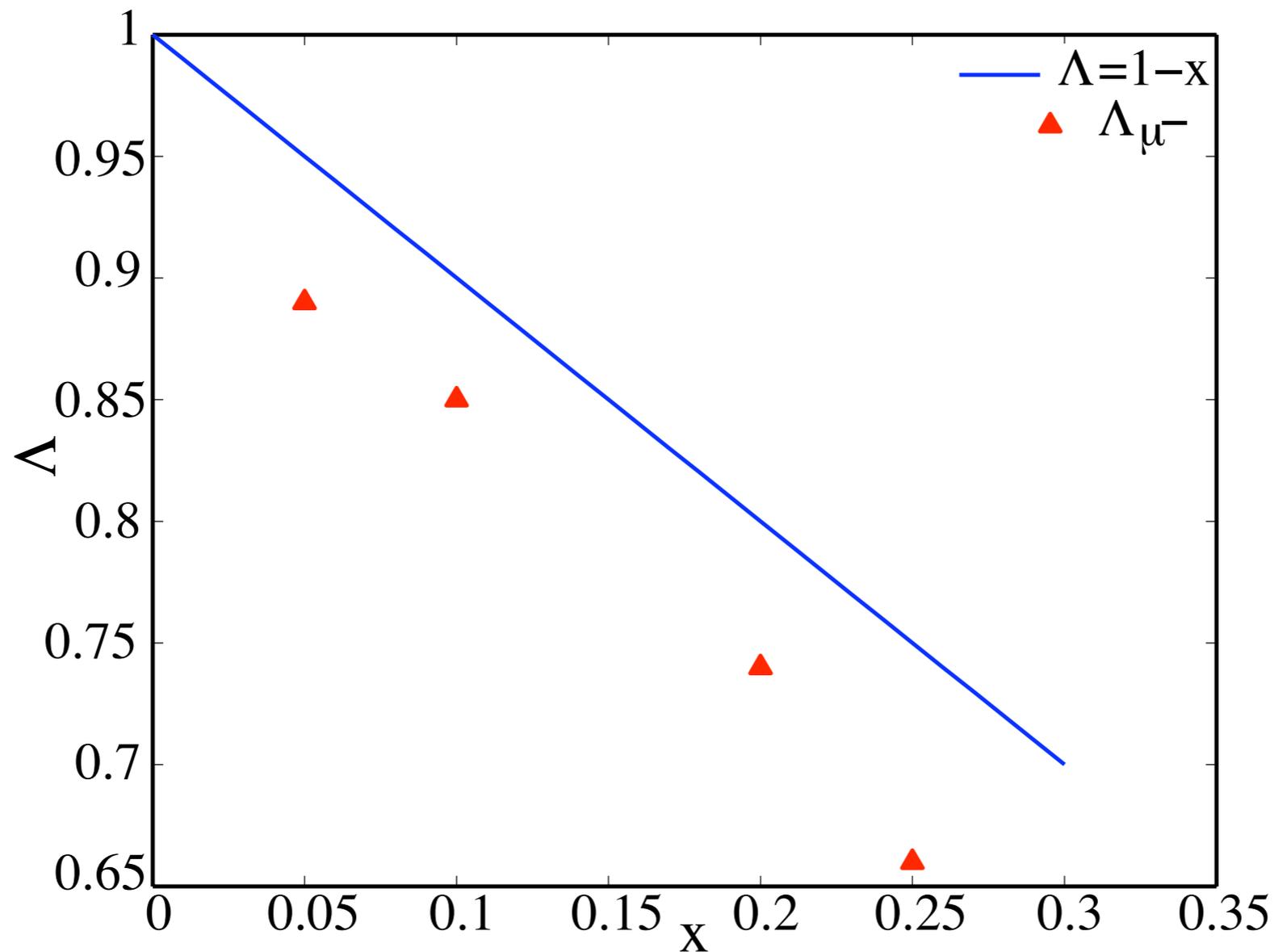


$$t^2/U \sim 60 \text{ meV}$$

Electron spectral function

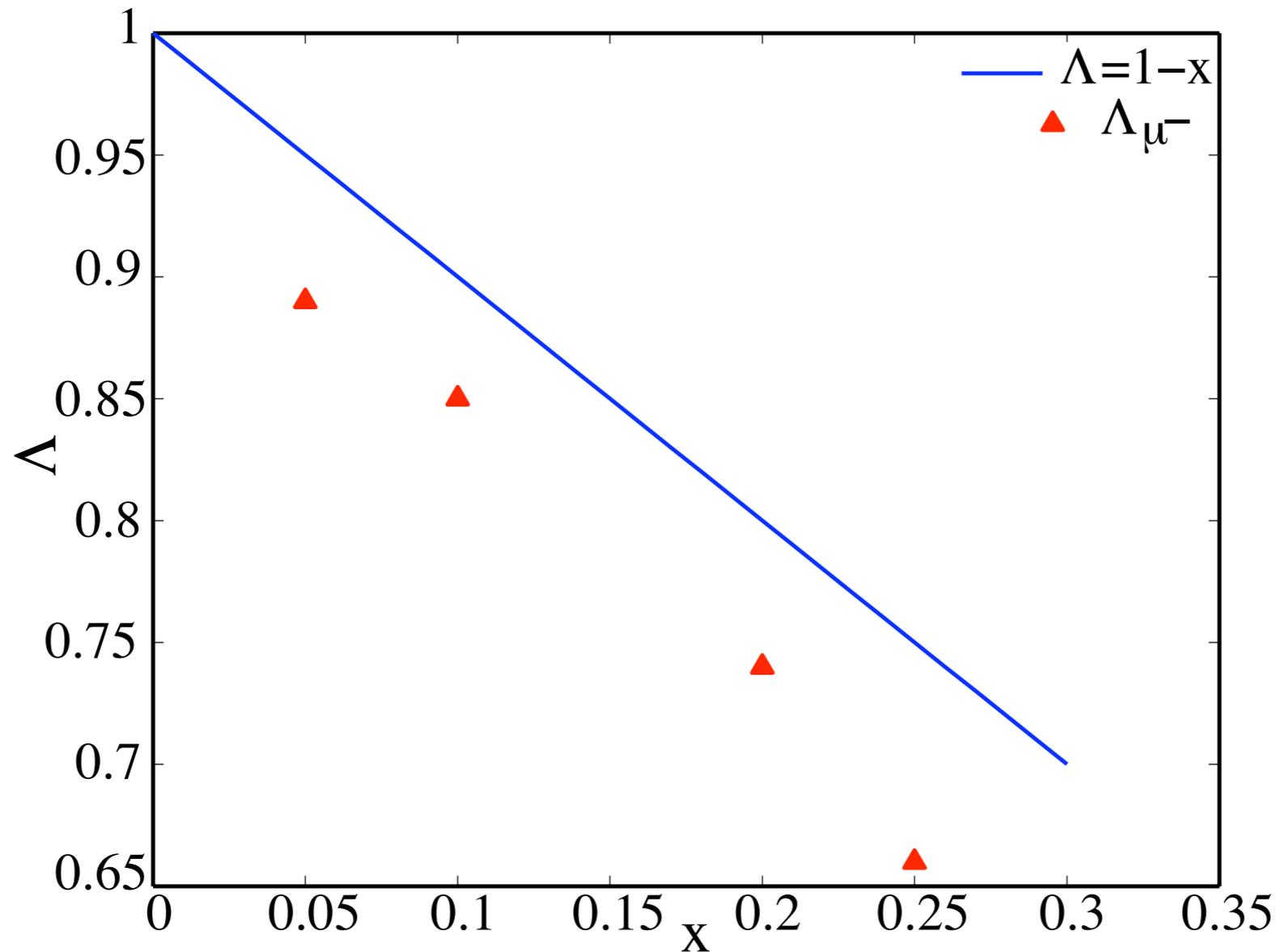

$$t^2/U \sim 60 \text{meV}$$

Electron spectral function



$\Delta^2/U \sim 60 \text{ meV}$

Electron spectral function



$\Delta^2/U \sim 60 \text{ meV}$

Conserved charge:
$$Q = \sum_i c_i^\dagger c_i + 2 \sum_i \varphi_i^\dagger \varphi_i$$

Origin of two bands

Two charge e excitations

$$c_{i\sigma}$$

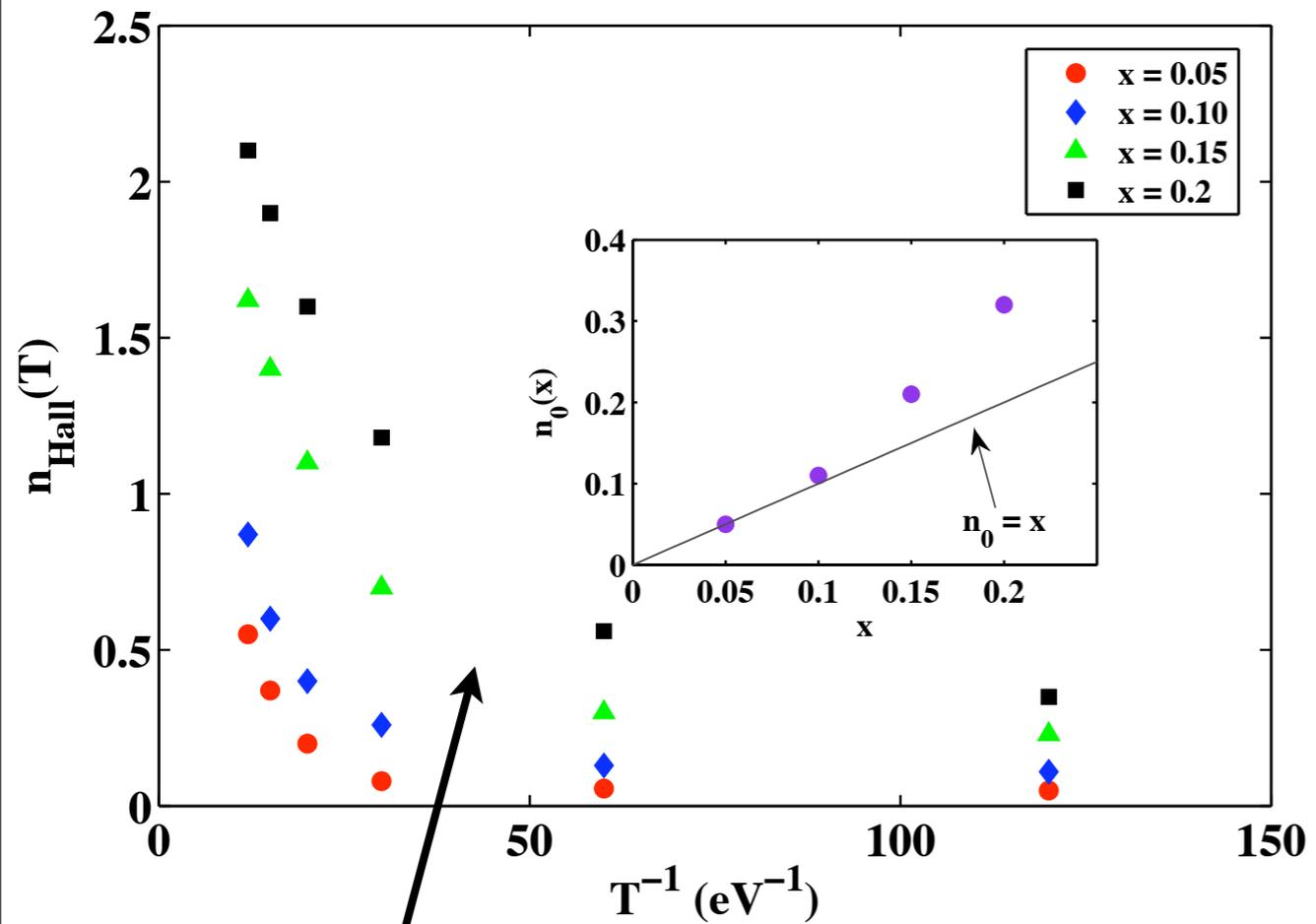
φ_i is confined (no kinetic energy)

$$\varphi_i^\dagger c_{i\bar{\sigma}}$$

New bound state

Pseudogap

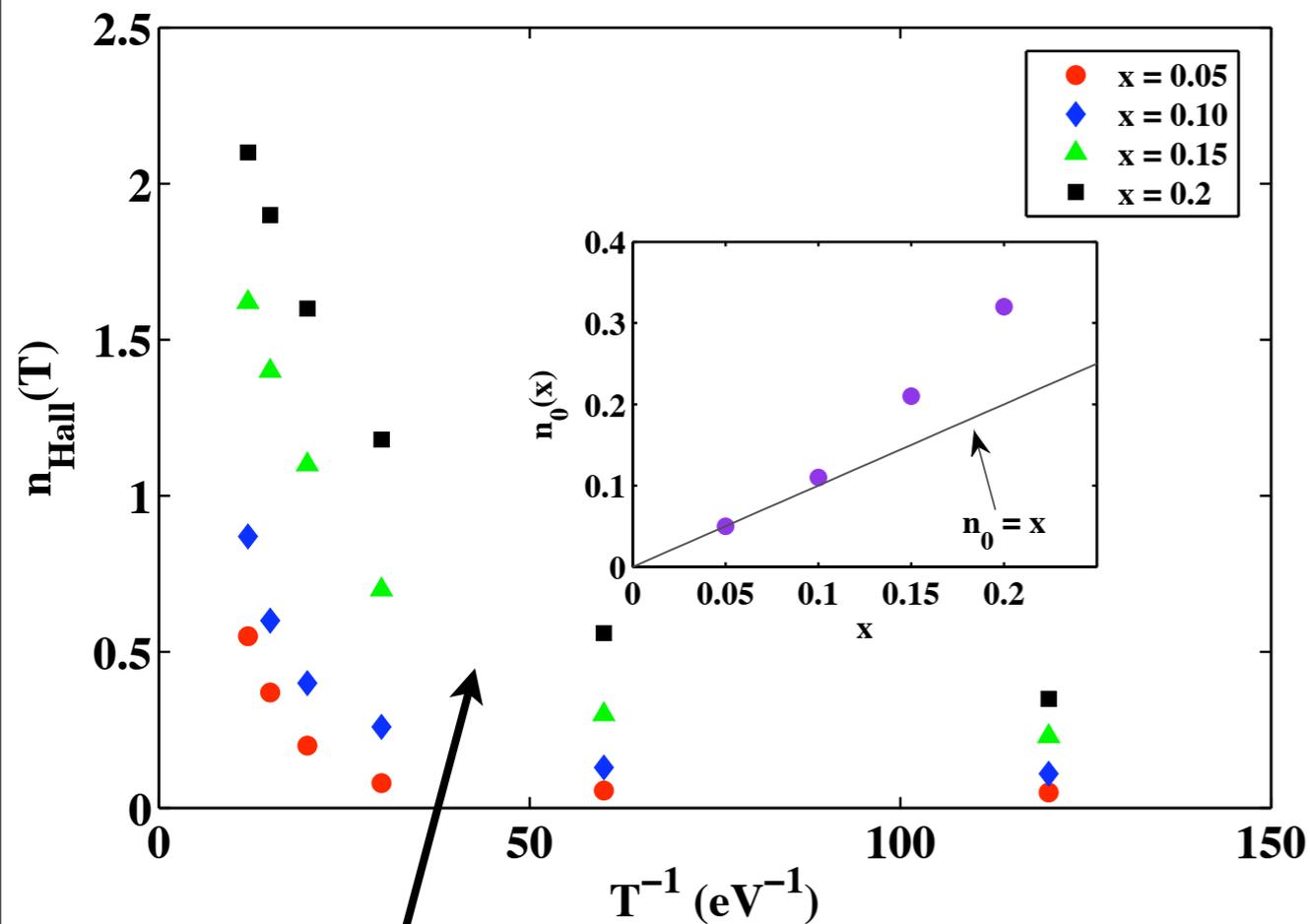
Our Theory



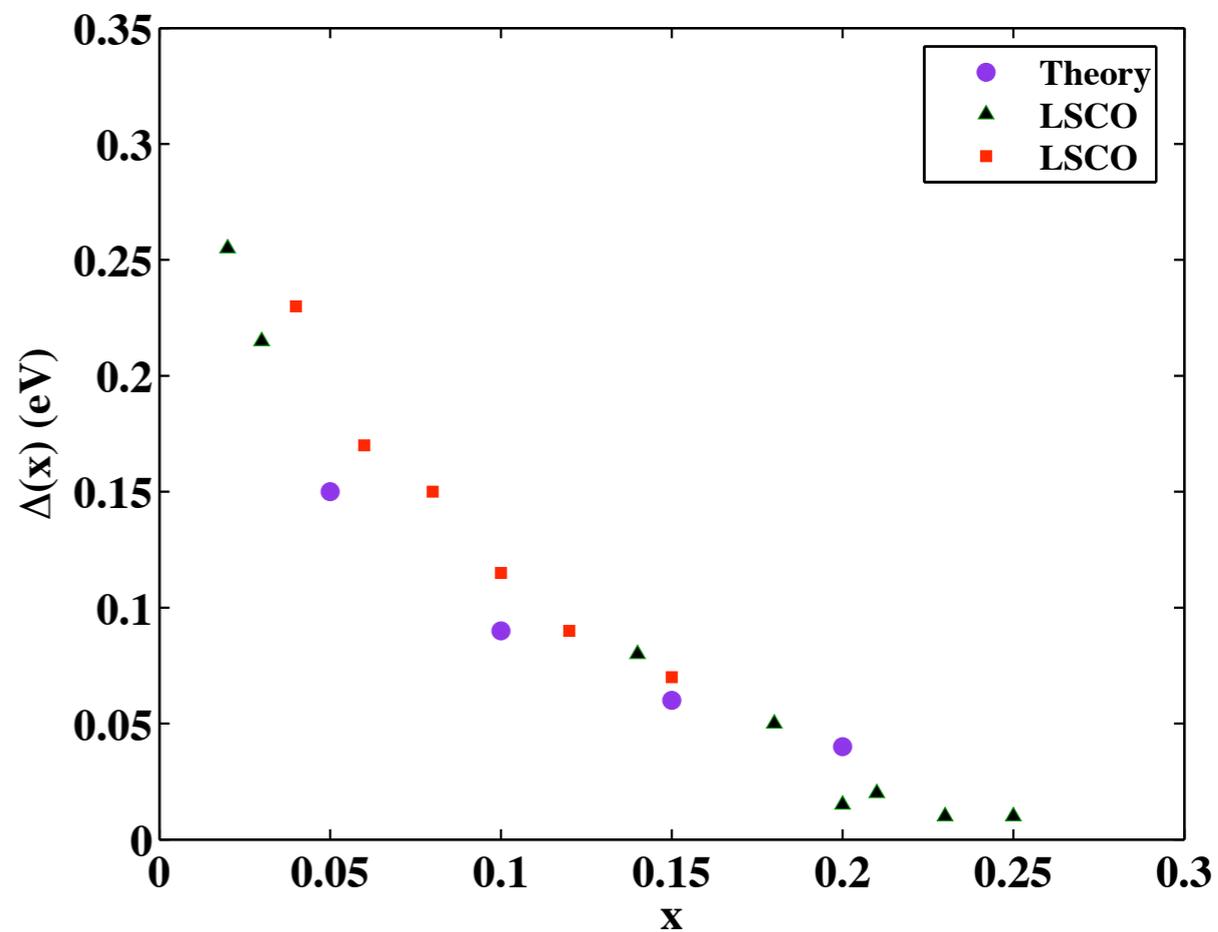
exponential
T-dependence

Our Theory

gap

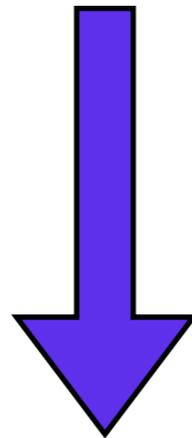


exponential
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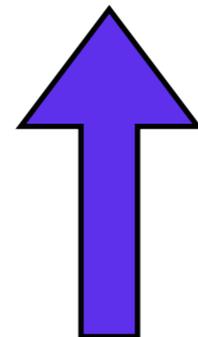


no model-dependent
free parameters: just
 t/U

thermopower ala
Kelvin: $\partial S / \partial n$

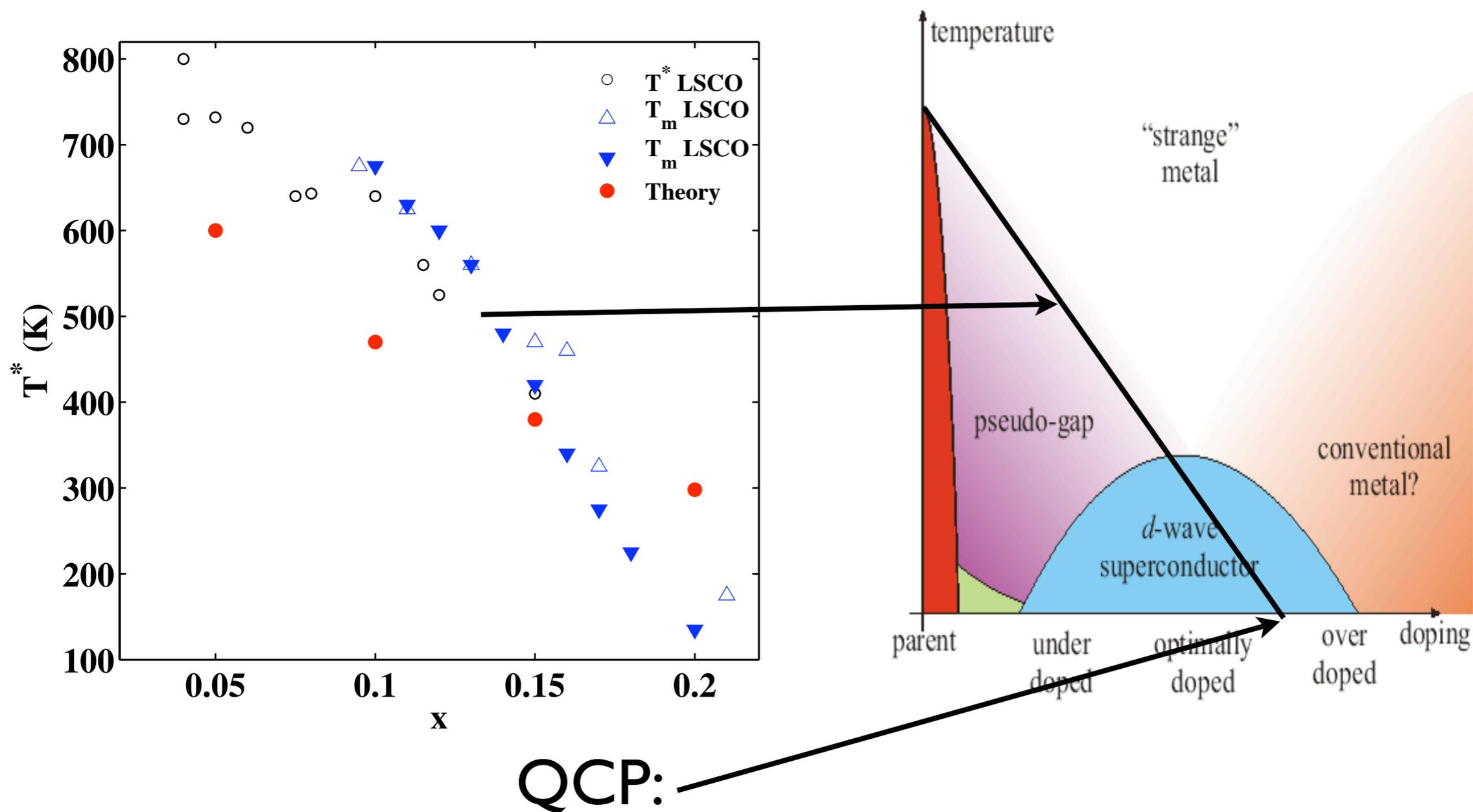


thermopower vanishes
when the entropy is maximized:
quantum phase transition at optimal T_c



high-low energy mixing

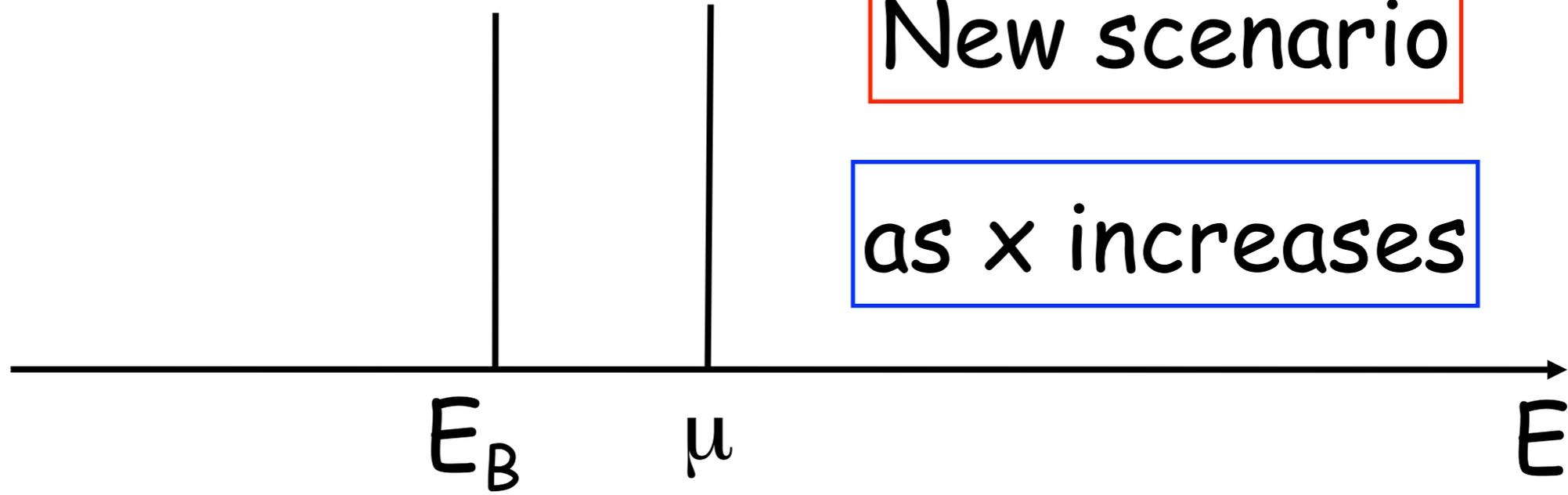
strange metal: breakup (deconfinement) of bound states



T-linear resistivity

New scenario

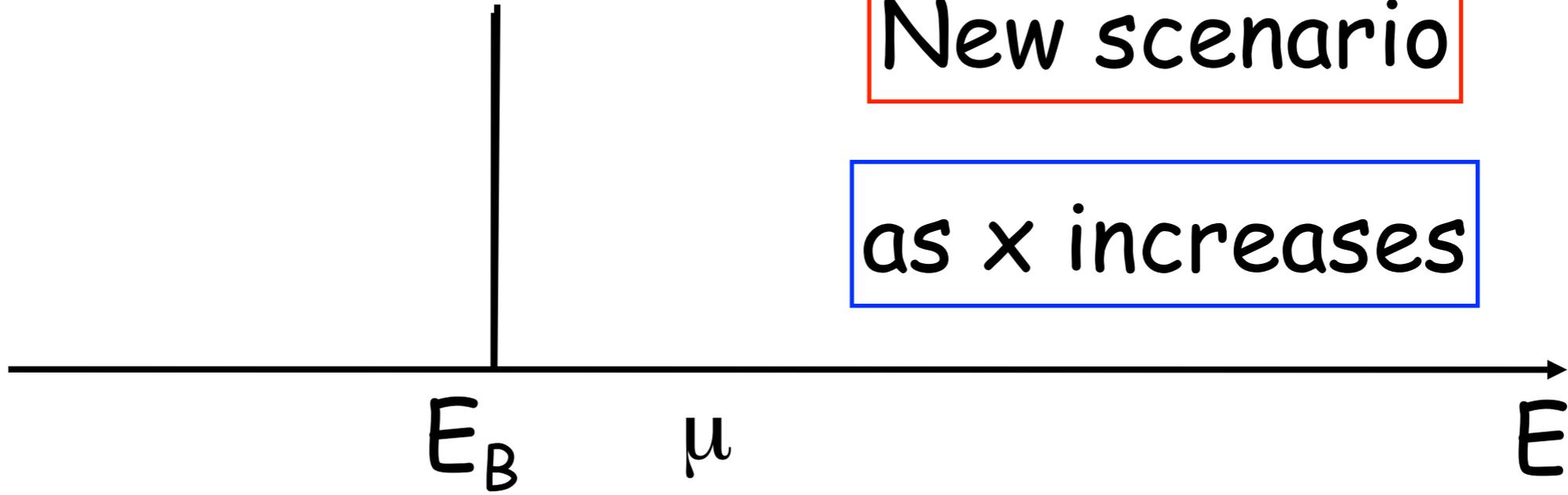
as x increases



T-linear resistivity

New scenario

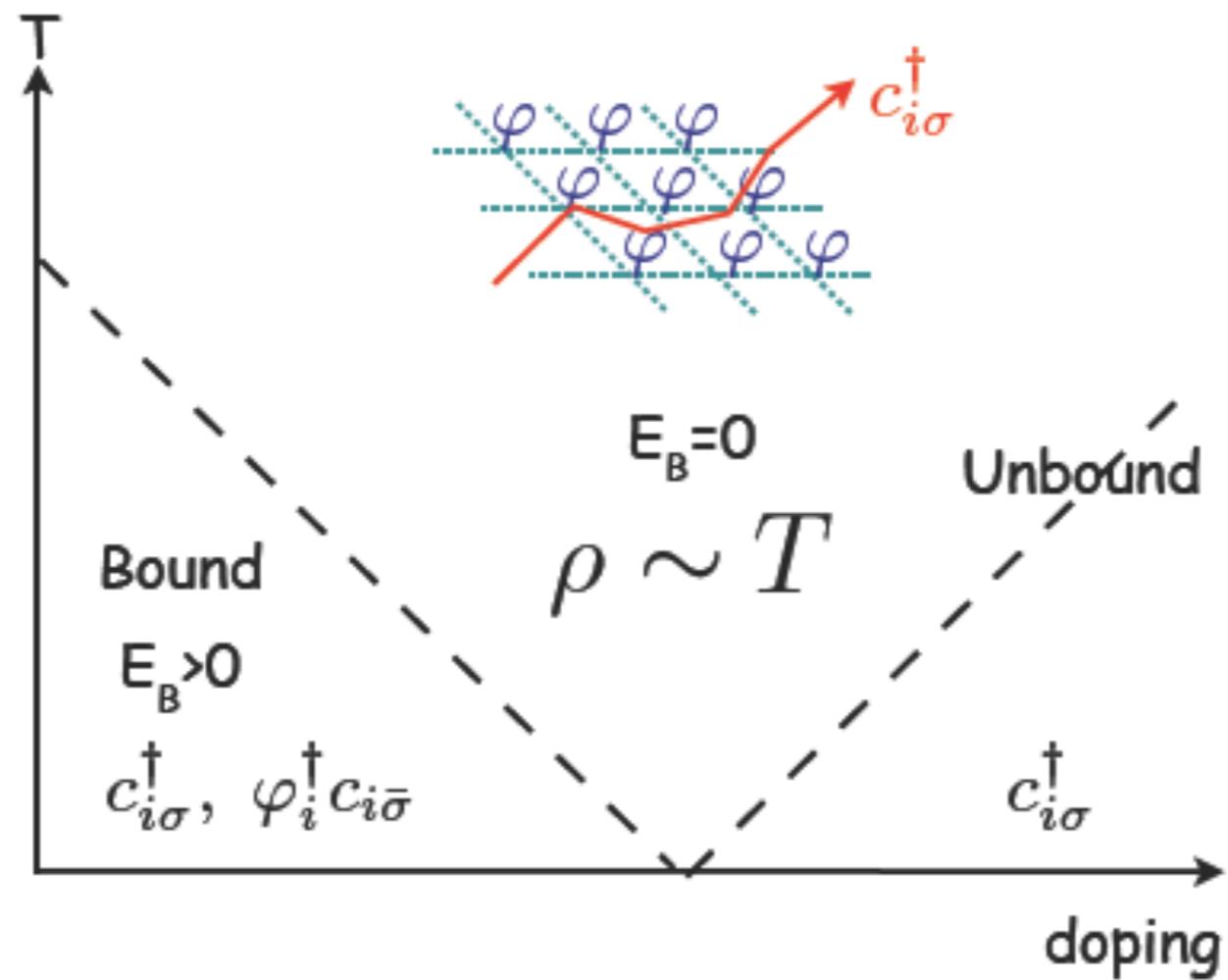
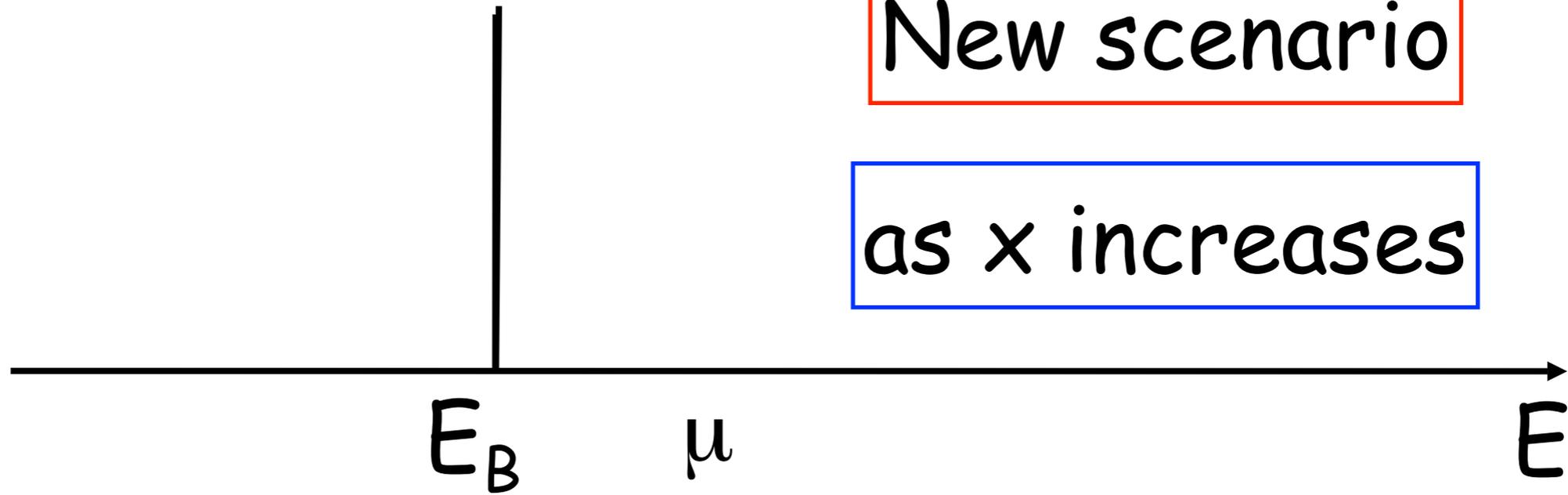
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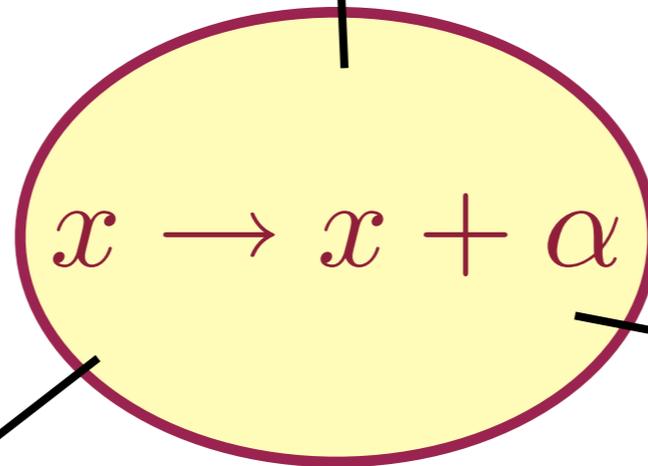
as x increases



Predictions:

QO oscillations:

$$V_{\text{hp}} - V_{\text{ep}} = 2(x + \alpha)$$



Superfluid density

$$\rho_s \propto x + \alpha$$

optical conductivity:

$$n_{\text{eff}} \propto (x + \alpha) > x$$

Thanks to R. G. Leigh and Ting-Pong Choy, Shiladitya Chakraborty, Seungmin Hong and DMR-NSF